

**$K^- d \rightarrow \pi \Lambda N$ reaction
with in-flight kaons
for studying the ΛN interaction**

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Introduction

- Low energy scattering amplitudes for 2-body systems are parametrized by scattering length a and effective range r .

- We want to explore the values of $a_{\Lambda n}$, $r_{\Lambda n}$ and how large is Isospin Symmetry Breaking (ISB) of the ΛN system, $a_{\Lambda n}/a_{\Lambda p}$ and $r_{\Lambda n}/r_{\Lambda p}$.

		Λp	Λn
a [fm]	(Spin) singlet	$-2.43^{+0.16}_{-0.25}$	—
	triplet	$-1.56^{+0.19}_{-0.22}$	—
r [fm]	singlet	$2.21^{+0.16}_{-0.36}$	—
	triplet	$3.7^{+0.6}_{-0.6}$	—

Experimental data^[1]

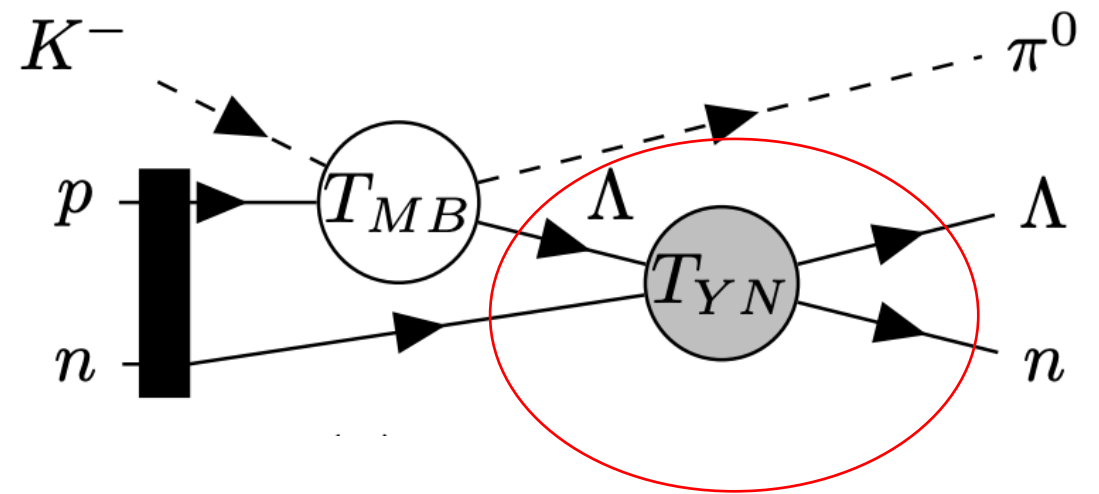
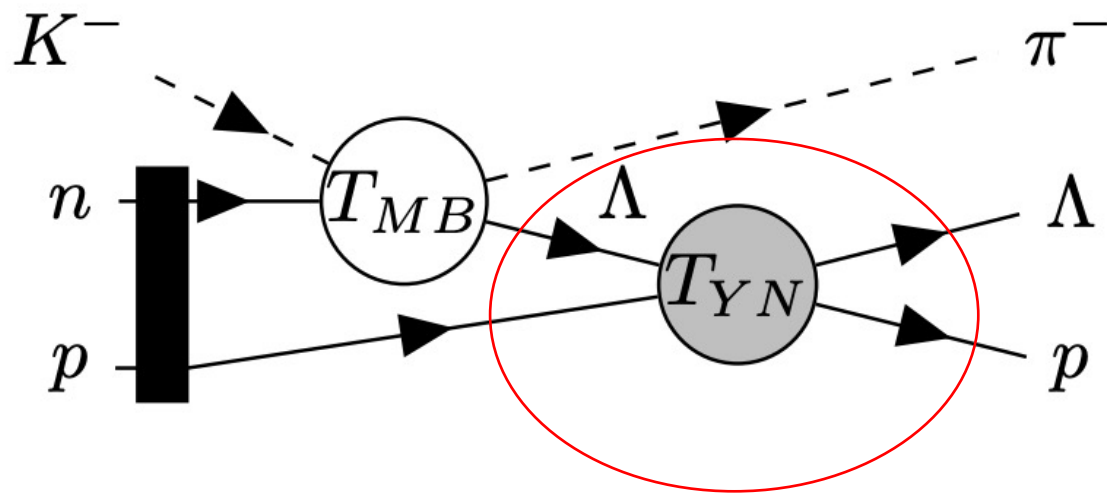
[1] A. Budzanowski *et al.* (HIRES Collaboration), Phys. Lett. B 687, 31 (2010)

Overview of Methods

- Calculate the ΛN invariant mass spectra of $K^- d \rightarrow \pi^- \Lambda p$ and $K^- d \rightarrow \pi^0 \Lambda n$ reaction near the mass threshold.
- Incident K^- momentum is 1000 MeV/c (p-wave and spin-flip effects)
(cf. our previous study^[2]: zero momentum)
- When $a_{n/p} \equiv a_{\Lambda n} / a_{\Lambda p}$, $r_{n/p} \equiv r_{\Lambda n} / r_{\Lambda p}$ are used as parameters, how much does cross section ratio $\sigma_{n/p}$ vary?

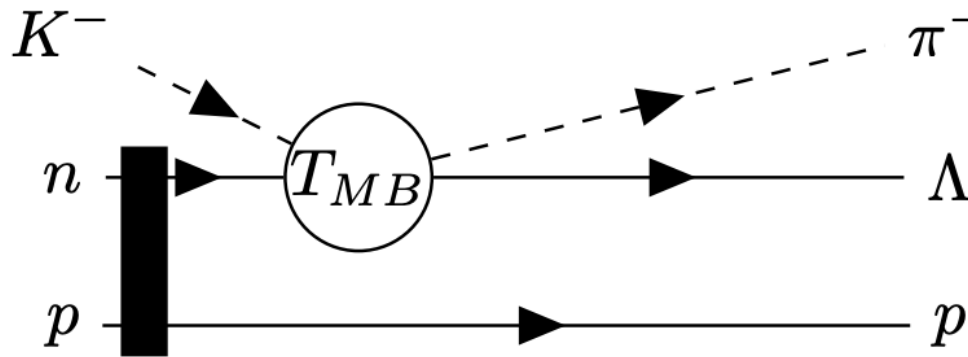
Scattering processes (Foreground)

Foreground(our target) diagram for each reaction

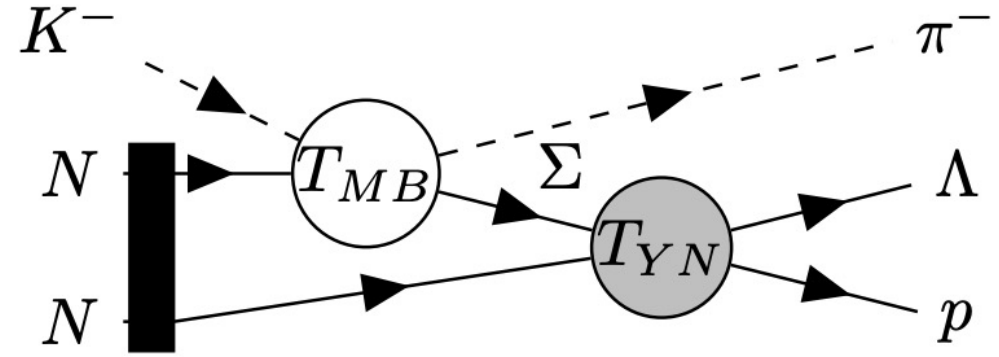


Scattering processes (Backgrounds)

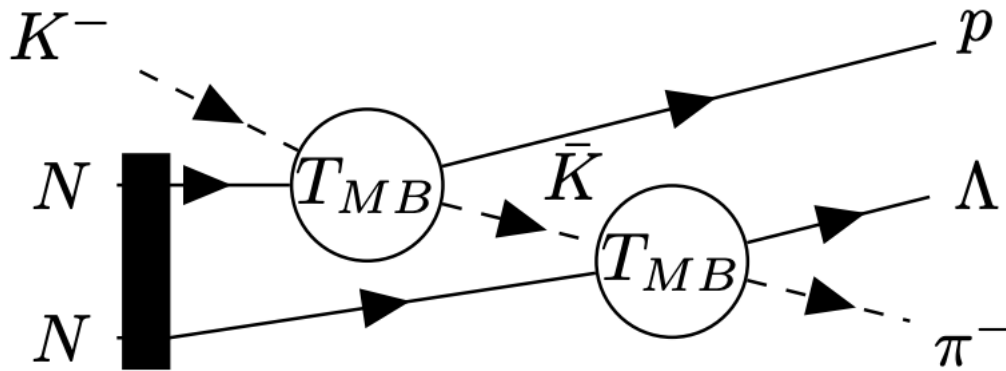
Background diagrams for the $K^- d \rightarrow \pi^- \Lambda p$ reaction



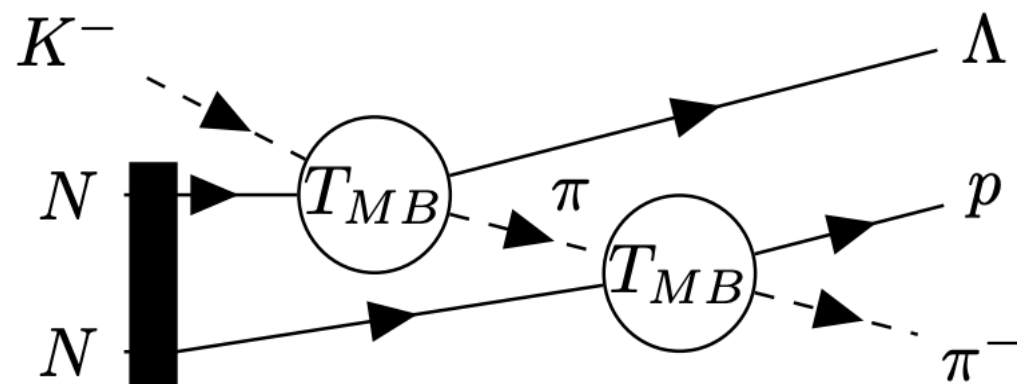
impulse



Σ exchange



\bar{K} exchange



π exchange

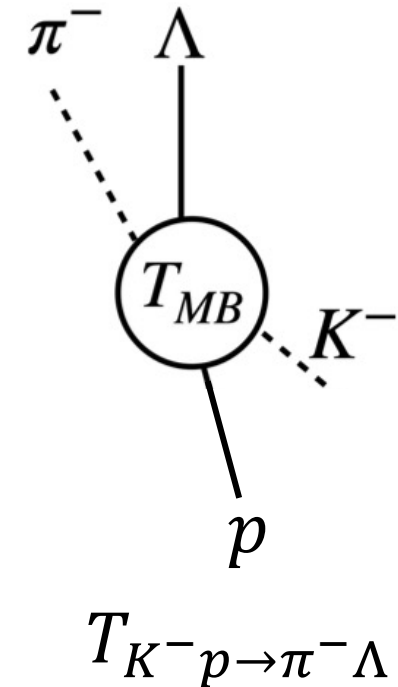
Meson-Baryon amplitude: T_{MB}

- Partial wave expansion (s-wave + p-wave)
- $\bar{K}N$ amplitudes ($\bar{K}N \rightarrow \bar{K}N, \pi Y$)

Chiral unitary approach^[3,4,5]

(amplitudes for each isospin state)

- πN amplitudes SAID data^[6]



[3] N. Kaiser, P. B. Siegel, and W. Weise, Nucl. Phys. A 594, 325 (1995).

[4] E. Oset, A. Ramos, Nucl. Phys. A 635, 99 (1998)

[5] D. Jido, E. Oset, A. Ramos, Phys. Rev. C 66, 055203 (2002)

[6] SAID partial-wave analysis, https://said.phys.gwu.edu/analysis/pin_analysis.html

Λ -Nucleon amplitude: $T_{\Lambda N}$

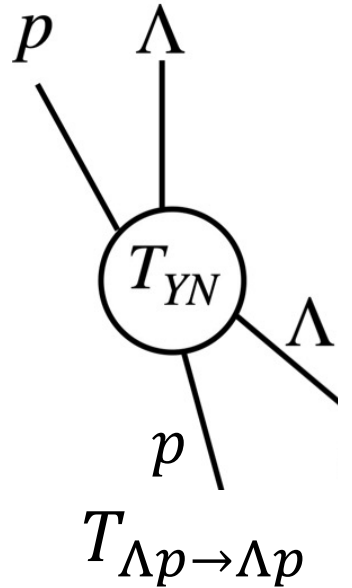
- Near the mass threshold ($M_{\Lambda N} \sim M_{\Lambda} + M_N$), ΛN amplitudes are described by effective range expansion,

$$T_{\Lambda N \rightarrow \Lambda N} = \left(-\frac{1}{a_{\Lambda N}} + \frac{1}{2} r_{\Lambda N} p_{\Lambda}^2 - i p_{\Lambda} \right)^{-1} \quad p_{\Lambda} : \text{momentum of } \Lambda$$

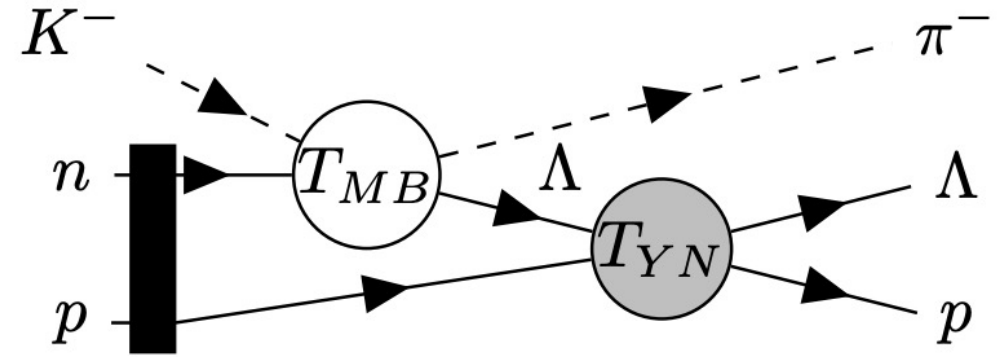
- Spin-singlet and spin-triplet states for the ΛN system

$$T_{\Lambda N \rightarrow \Lambda N}^{singlet} = T_{\Lambda N \rightarrow \Lambda N}(a^{singlet}, r^{singlet})$$

$$T_{\Lambda N \rightarrow \Lambda N}^{triplet} = T_{\Lambda N \rightarrow \Lambda N}(a^{triplet}, r^{triplet})$$



Spin in amplitude



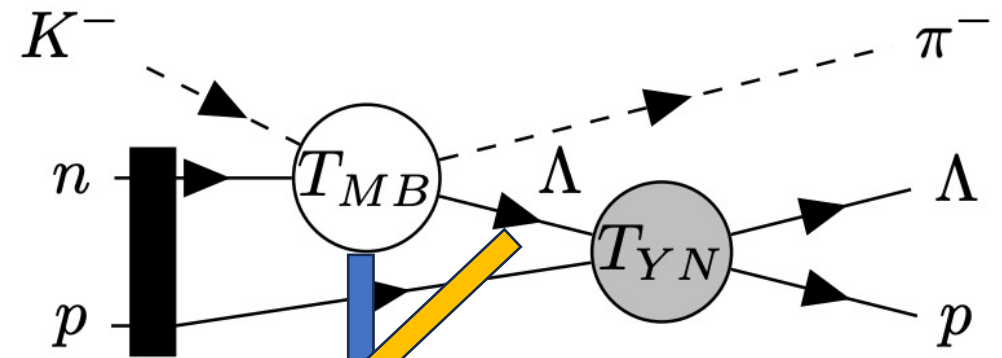
Spin part in the amplitude of the foreground

$$T_{spin} = \frac{1}{4} (3T_{\Lambda N}^s + T_{\Lambda N}^t) T_{K^- n \rightarrow \pi^- \Lambda} S_d$$

$$+ \frac{1}{4} (T_{\Lambda N}^s - T_{\Lambda N}^t) \sigma_{\Lambda} T_{K^- n \rightarrow \pi^- \Lambda} S_d (\sigma_p)^T$$

(S_d : spin of deuteron)

Amplitude of foreground



Amplitude of the foreground

propagator

Momentum conservation

$$\vec{p}_d + \vec{p}_{K^-} = \vec{q} + \vec{p}_{\pi^-}$$

$$T = T_{spin} \times \int \frac{d^3 \vec{q}}{(2\pi)^3} \frac{2M_\Lambda}{q_0^2 - \vec{q}^2 - M_\Lambda + i\epsilon} \varphi(|\vec{q} + \vec{p}_{\pi^-} - \vec{p}_{K^-}|)$$

(q : momentum of the intermediate Λ)

(φ : deuteron wave function in momentum space)

Cross section of each term ($K^- d \rightarrow \pi^- \Lambda p$)

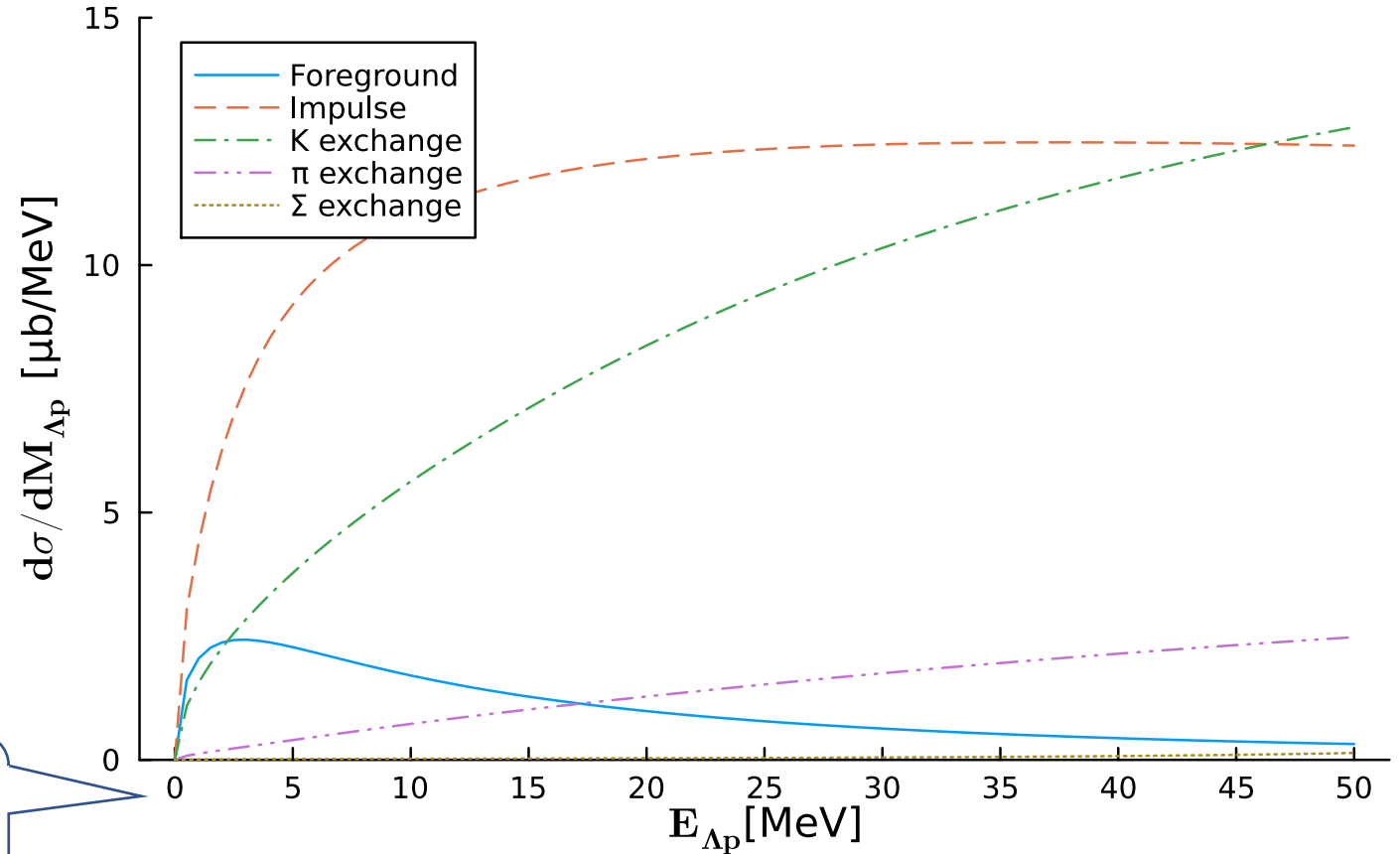
- Cross section of the reaction

$$\frac{d\sigma}{dM_{\Lambda N}} = (\textit{kinetic term})$$

$$\times \int |T|^2 dV$$

T : scattering amplitude
 dV : phase space of the reaction

Λp threshold
 $(M_{\Lambda} + M_p)$



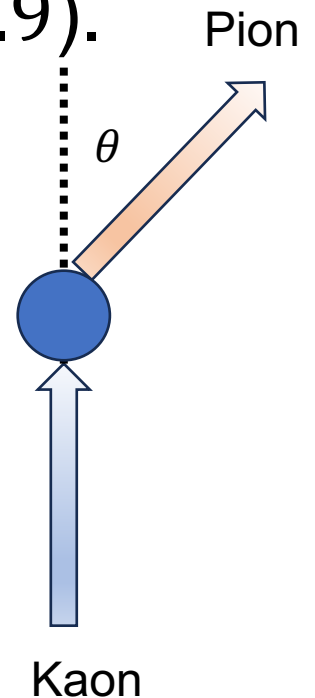
Angular restriction of Pion (background reduction①)

We restrict pion angle to the forward direction ($\cos \theta \geq 0.9$).

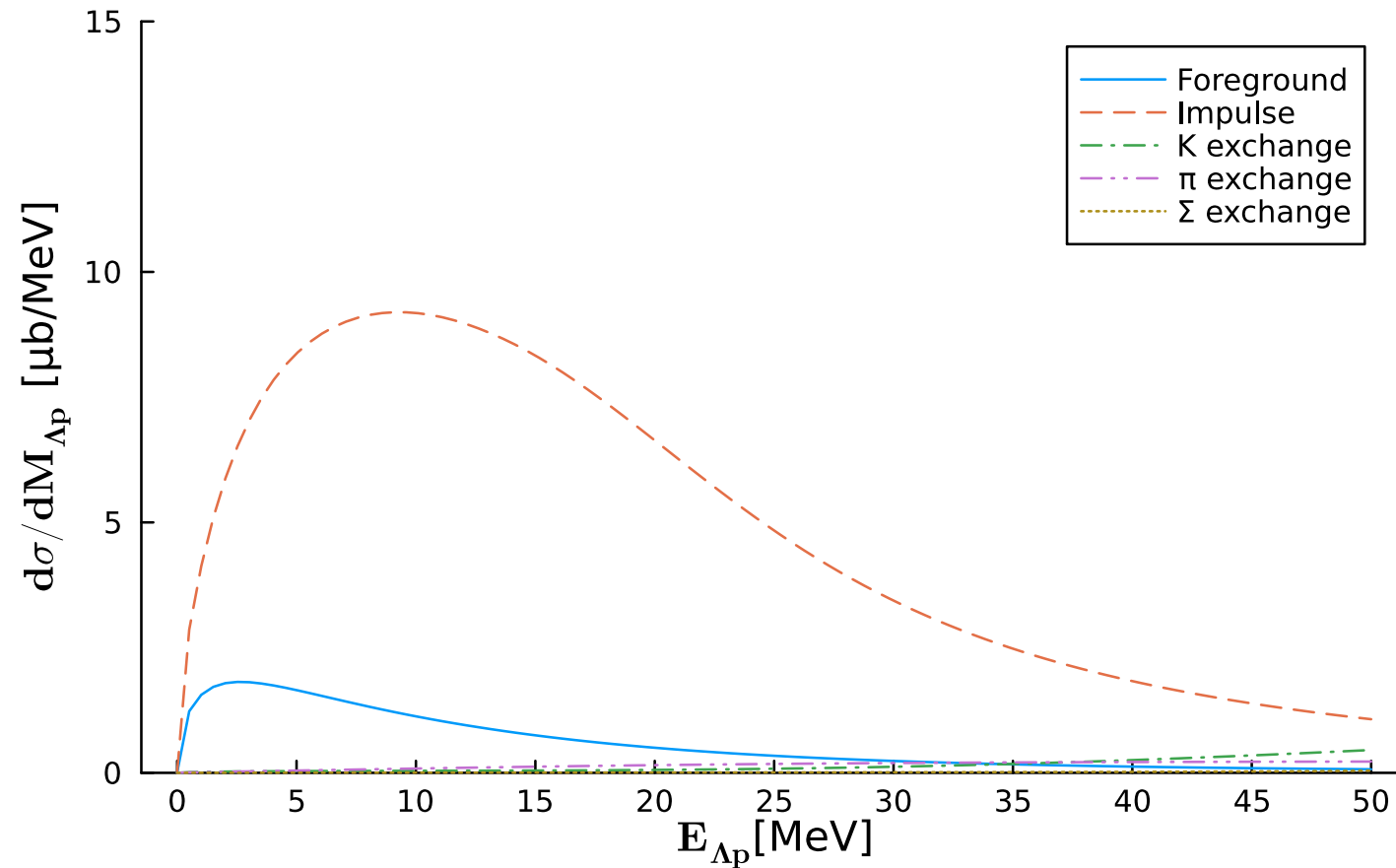
1. Reduction of background processes
2. Separation of parameters (spin selection rule)

4 parameters $a_{n/p}^s, r_{n/p}^s, a_{n/p}^t, r_{n/p}^t$

Results become dependent solely on $a_{n/p}^t, r_{n/p}^t$ (triplet)



Reduction of meson exchange (background reduction①)



Restriction
Forward pion,
 $\cos \theta \geq 0.9$

$$\frac{d\sigma}{dM_{\Lambda N}} = (\text{kinetic}) \times \int_{\cos \theta \geq 0.9} |T|^2 dV$$

Reduction of
backgrounds
(K, π exchange)

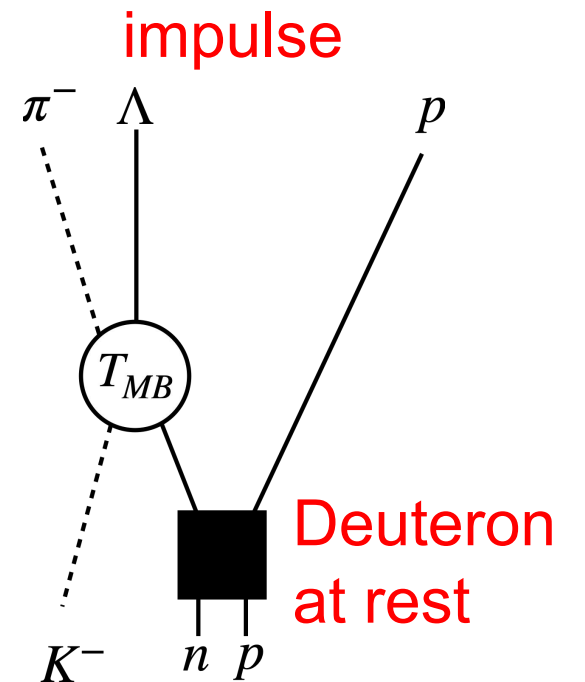
Momentum restriction of Nucleon

(background reduction②)

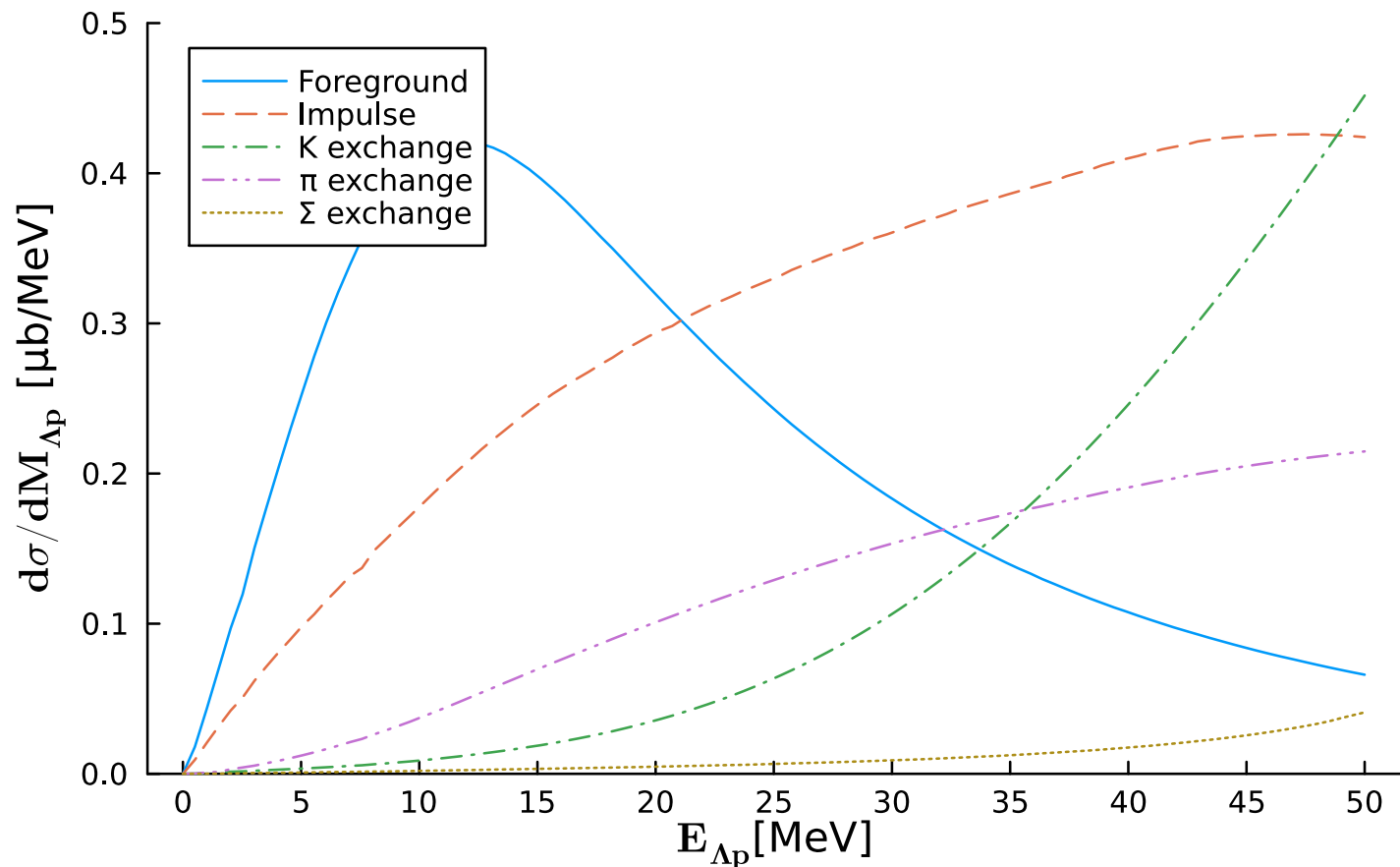
- We pick up events where nucleon momentum is large.

$$p_{Nucleon} \geq 150 \text{ MeV}/c$$

- Impulse diagram will be reduced by this nucleon momentum selection.



Reduction of impulse (background reduction②)



Reduction of background
(impulse)

Restriction

- ① Pion angle,
 $\cos \theta \geq 0.9$
- ② Nucleon momentum,
 $p_N \geq 150 \text{ MeV}/c$

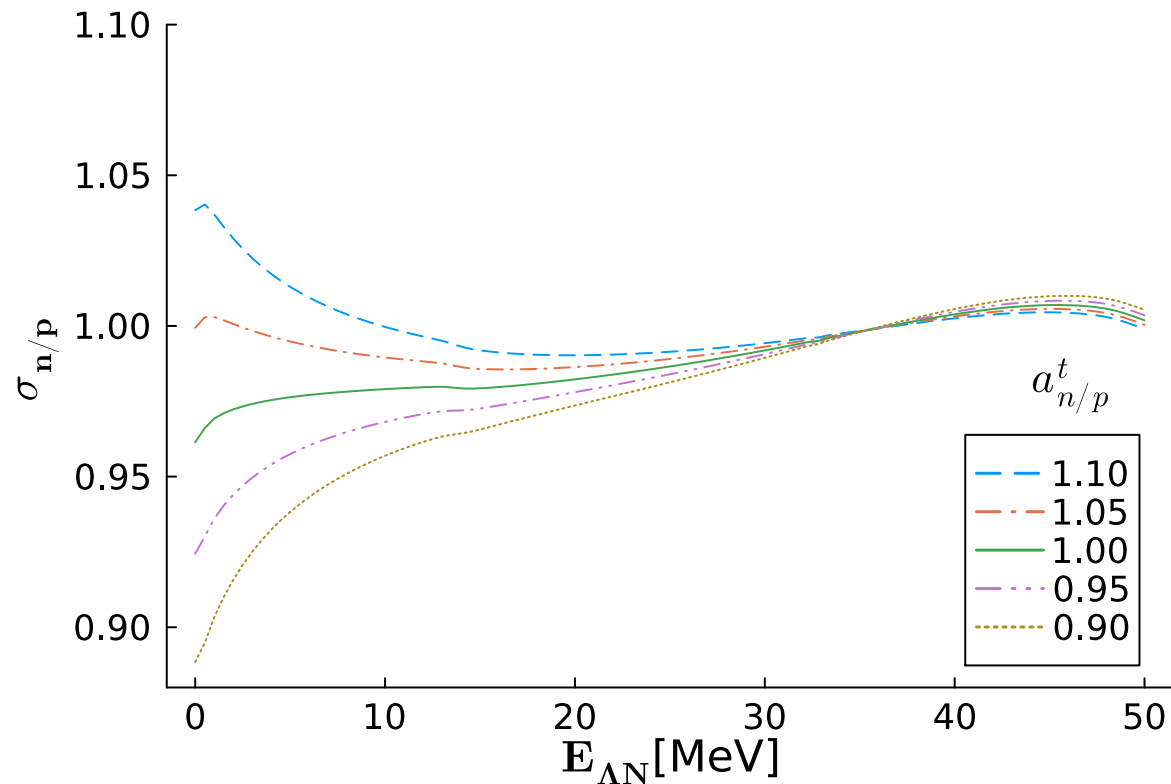
Cross section ratio

- If isospin symmetry were exact,
the ratio of scattering cross section would satisfy

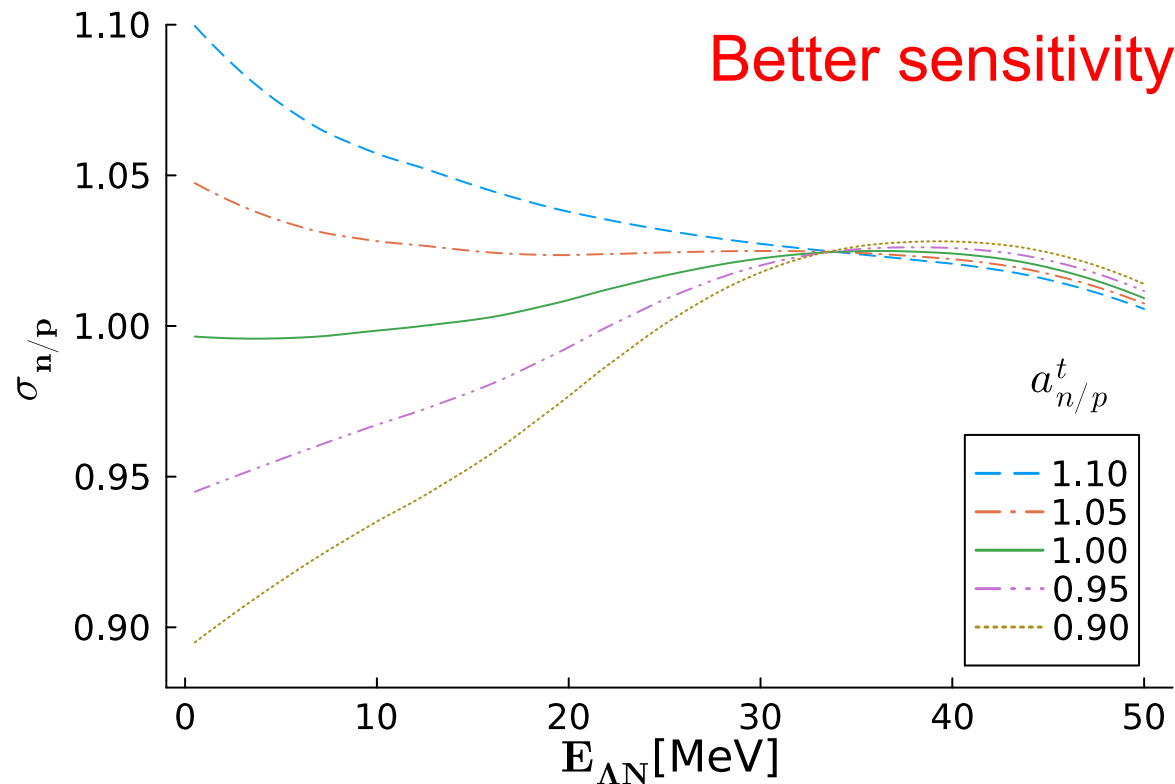
$$\sigma_{n/p} \equiv 2 \times \frac{\sigma_{\pi^0 \Lambda n}}{\sigma_{\pi^- \Lambda p}} = 1$$

- Deviation from exact ratio(=1) and numerical result
reflects the ISB of the ΛN system.

Cross section ratio




Restriction
Pion angle, $\cos \theta \geq 0.9$



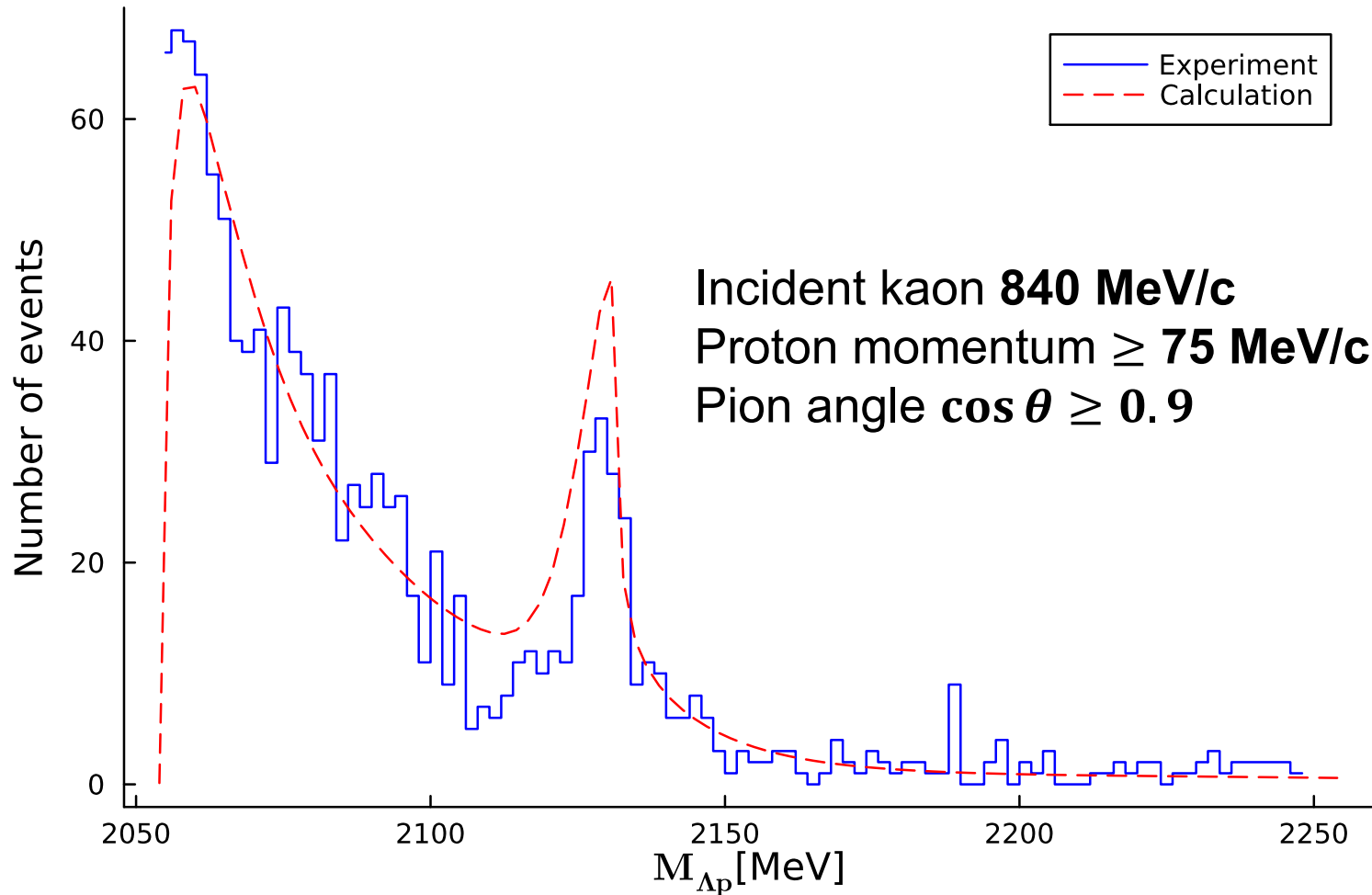
Restriction
① Pion angle, $\cos \theta \geq 0.9$
② Nucleon momentum, $p_N \geq 150 \text{ MeV}/c$

Summary

- We calculated scattering cross section when incident K^- have momenta (p-wave and spin-flip effects).
- Angular restriction of pion, $\cos \theta \geq 0.9$
momentum restriction for nucleon, $p_N \geq 150 \text{ MeV}/c$  Reduction of backgrounds
- ISB of cross section ratio $\sigma_{n/p}$ varies $\sim 10\%$
if ISB of $a_{n/p}$ and $r_{n/p}$ are $\sim 10\%$.

Additional slides

Comparison with an old experiment



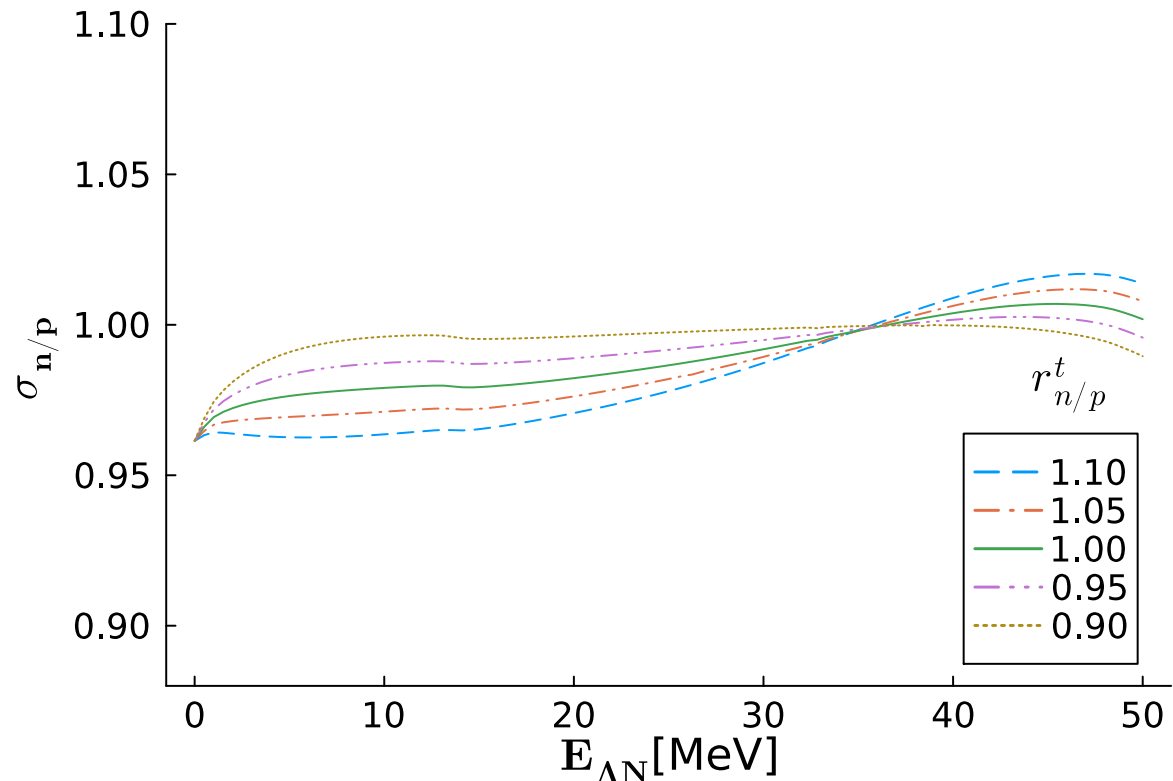
- $K^- d \rightarrow \pi^- \Lambda p$ reaction
- An experimental data is by reference [A1]
- The parameter of Σ exchange term

$$a_{\Sigma N}^t = 1.68 - 2.35i \text{ [A2]}$$

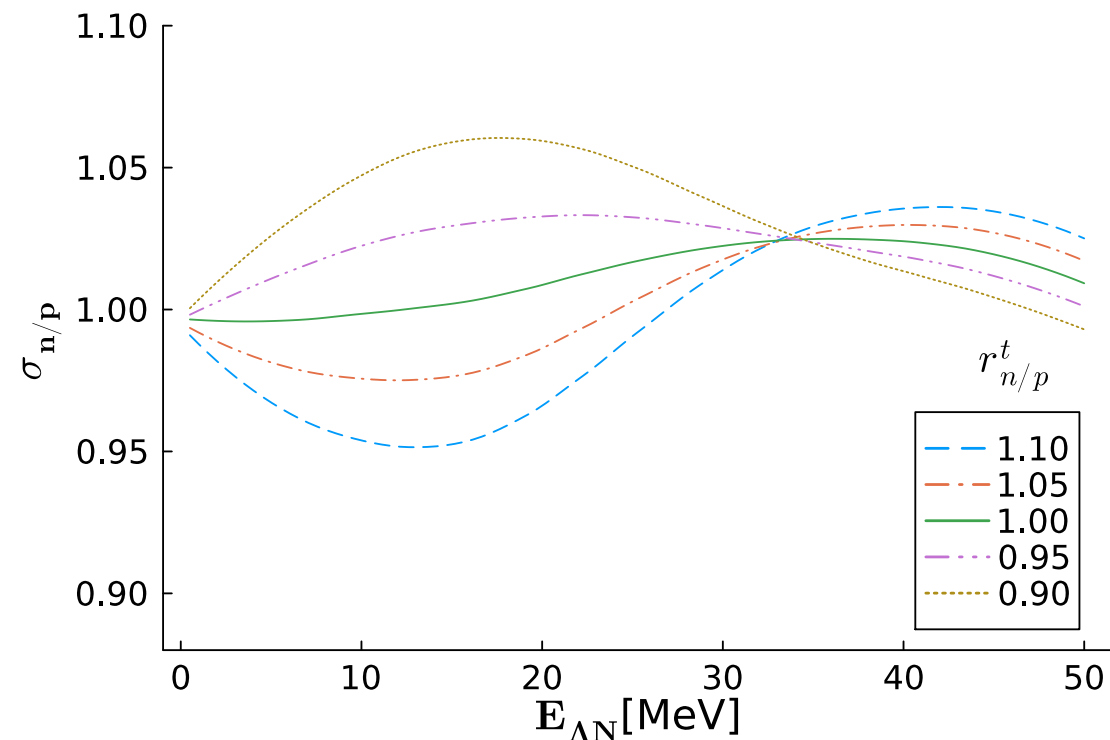
[A1] O. Braun, et al, Nuclear Physics B 124, 45 (1977).

[A2] T. A. Rijken, V. G. J. Stoks, and Y. Yamamoto, Phys. Rev. C 59, 21 (1999).

Cross section ratio (effective range)



Restriction
Pion angle, $\cos \theta \geq 0.9$

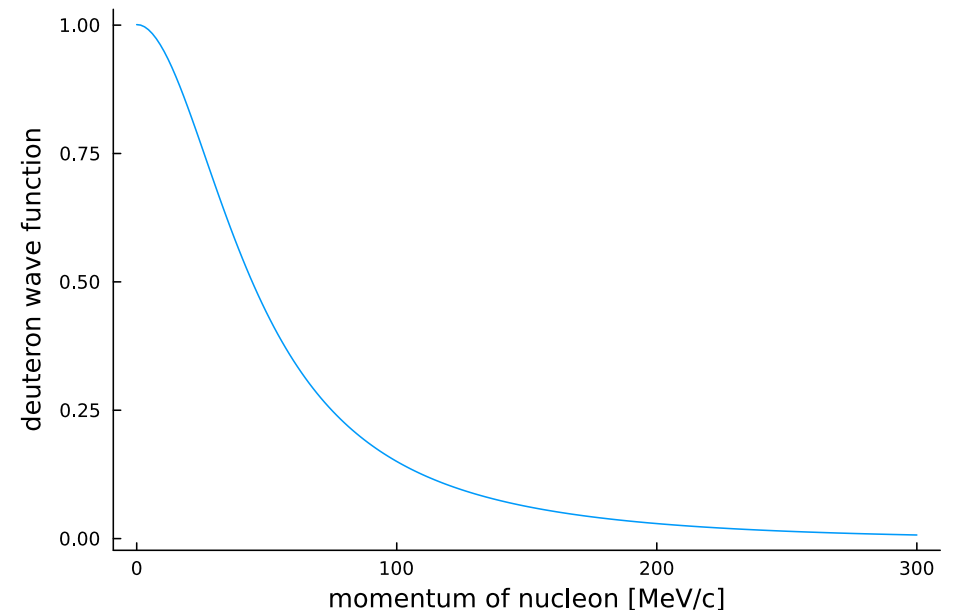


Restriction

- ① Pion angle, $\cos \theta \geq 0.9$
- ② Nucleon momentum, $p_N \geq 150 \text{ MeV}$

Deuteron wave-function

- We employ deuteron wave-function, CD-Bonn potential^[A3] $\varphi(p)$ (p denotes momentum of nucleon in deuteron).
- The scale of amplitudes are mainly determined by $\varphi(p)$.
- From momentum conservation, p varies for each diagram.



Calculation of Σ exchange diagram

- We use effective range expansion for Σ exchange in the same way as Λ exchange.
- $a_{\Sigma N \rightarrow \Lambda N}$, $r_{\Sigma N \rightarrow \Lambda N}$ are calculated by unitarization (by P) of ΣN and ΛN doublet state.

$$T = (V^{-1} + P)^{-1}$$

$$T = \begin{pmatrix} T_{\Lambda N \rightarrow \Lambda N}(a, r) & T_{\Lambda N \rightarrow \Sigma N}(a, r) \\ T_{\Sigma N \rightarrow \Lambda N}(a, r) & T_{\Sigma N \rightarrow \Sigma N}(a, r) \end{pmatrix}$$