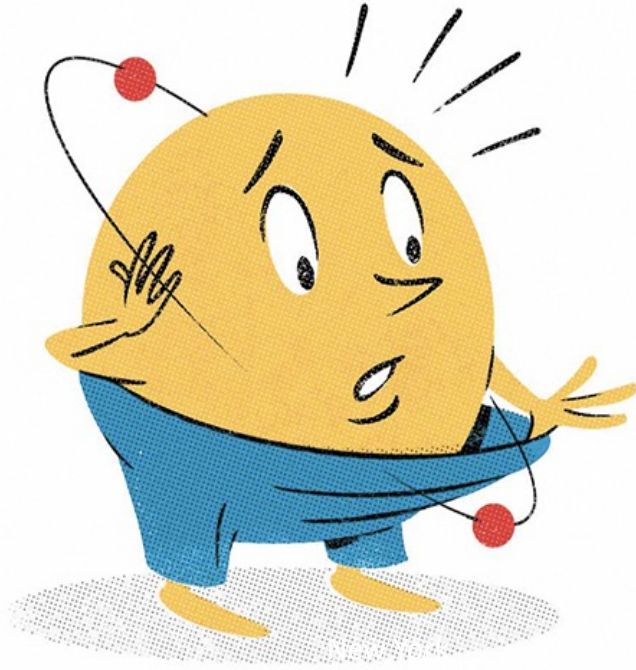




山东大学  
SHANDONG UNIVERSITY

Jefferson Lab  
Exploring the Nature of Matter



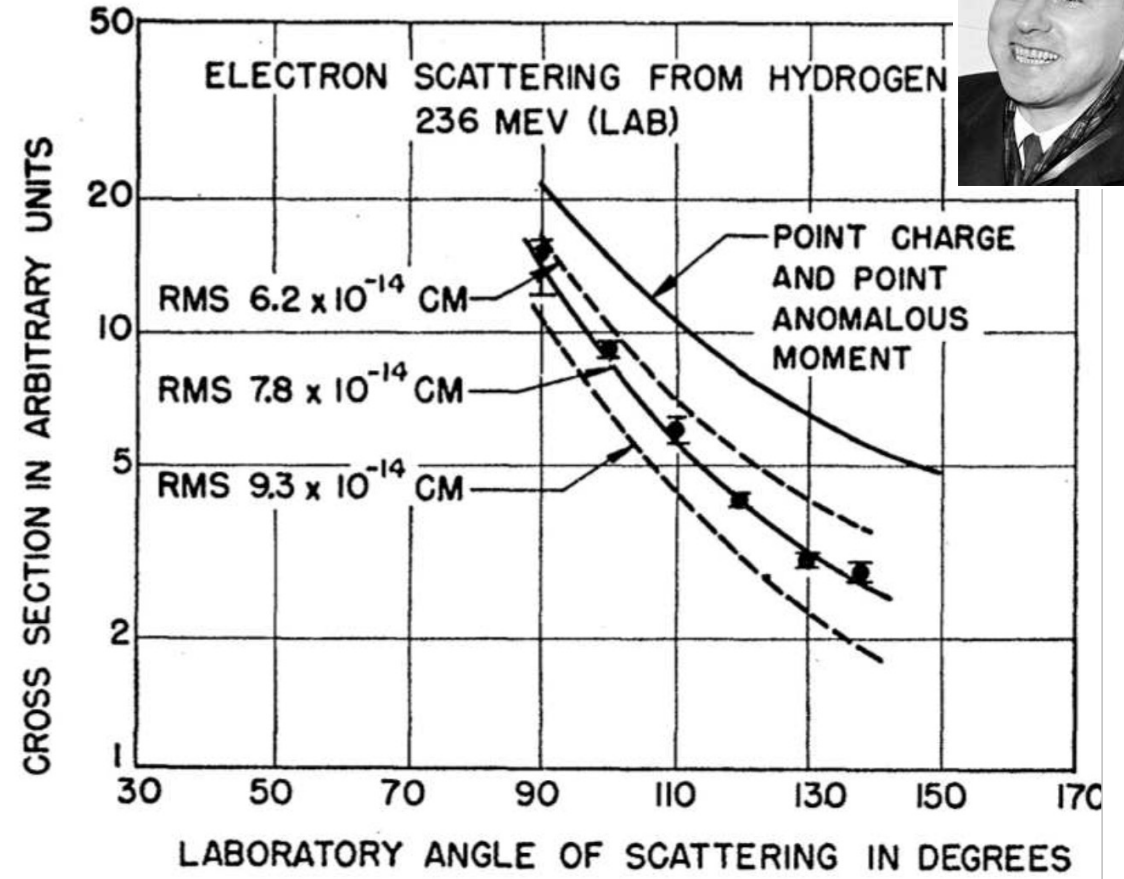
# Proton Charge Radius Experiment at Jefferson Lab

- Weizhi Xiong (熊伟志)
- Shandong University
- LEES 2024, Tohoku University Sendai, Japan
- Oct. 28<sup>th</sup> – Nov. 1<sup>st</sup> 2024

PR<sup>o</sup>ton  
Radius

# Outline

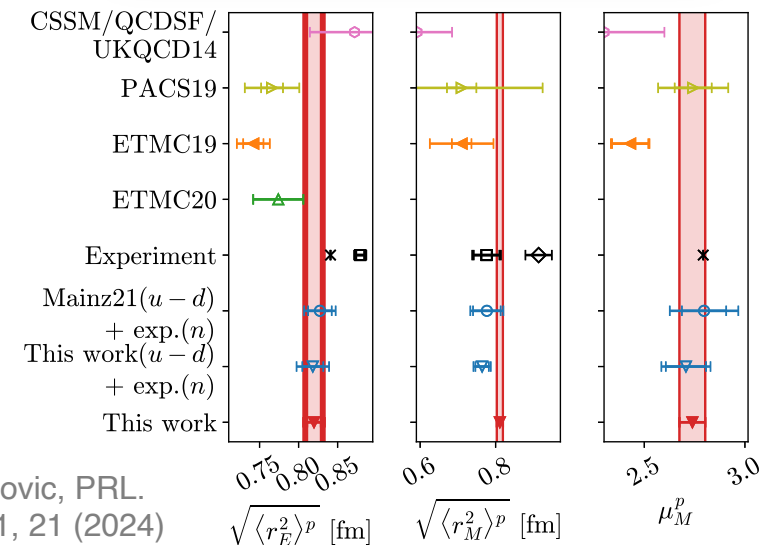
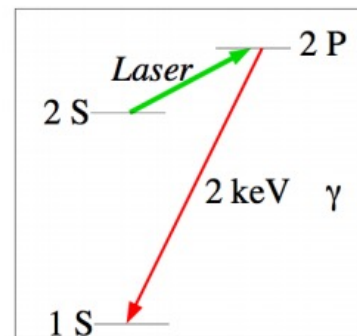
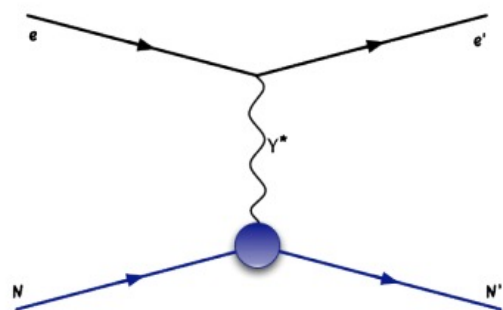
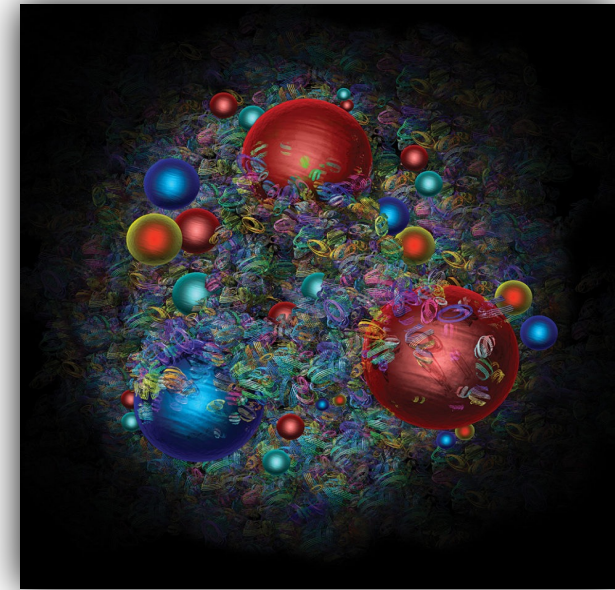
- Introduction: proton charge radius and electromagnetic form factors
- PRad experiment at JLab
- Preparation of PRad-II
- Summary



1956 Measurements @ Stanford

# General Info on Proton Charge Radius

- Proton charge radius ( $r_p$ ):
  1. Spacial distribution of proton's charge
  2. Important for understanding how QCD works
  3. Input to the bound state QED calculation for atomic hydrogen energy levels
  4. Critical in determining Rydberg constant ( $R_\infty$ )
- Two well-established experimental methods:
  1.  $e$ - $p$  elastic scattering (nuclear physics)
  2. Hydrogen spectroscopy (atomic physics)



D. Djukanovic, PRL.  
132, no.21, 21 (2024)

# Unpolarized Lepton-Proton Elastic Scattering

- Elastic ep scattering, in the limit of Born approximation (neglecting lepton mass):

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \left( \frac{E'}{E} \right) \frac{1}{1+\tau} \left( G_E^p{}^2(Q^2) + \frac{\tau}{\epsilon} G_M^p{}^2(Q^2) \right)$$

$$Q^2 = 4EE' \sin^2 \frac{\theta}{2} \quad \tau = \frac{Q^2}{4M_p^2} \quad \epsilon = \left[ 1 + 2(1+\tau) \tan^2 \frac{\theta}{2} \right]^{-1}$$

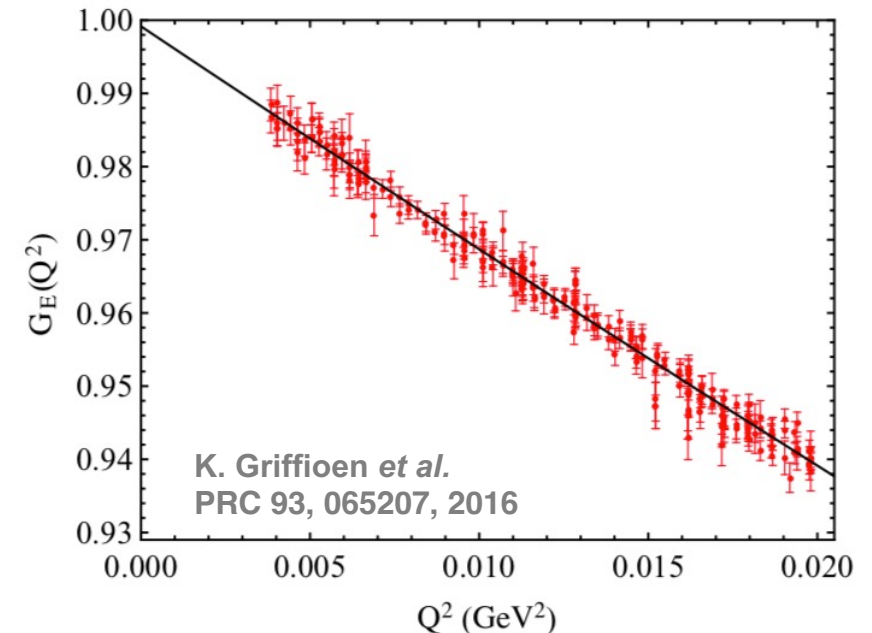
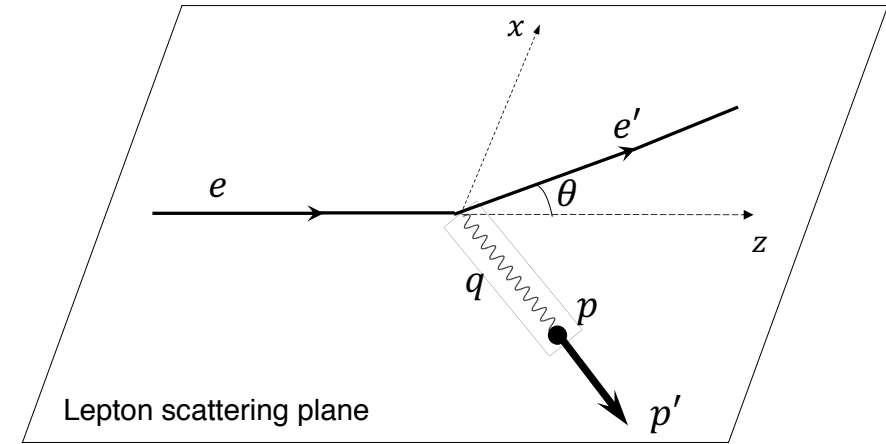
Taylor expansion of  $G_E$  at low  $Q^2$

$$G_E^p(Q^2) = 1 - \frac{Q^2}{6} \langle r^2 \rangle + \frac{Q^4}{120} \langle r^4 \rangle + \dots$$

Derivative at low  $Q^2$  limit

$$\langle r^2 \rangle = -6 \left. \frac{dG_E^p(Q^2)}{dQ^2} \right|_{Q^2=0}$$

- Exploit  $\epsilon$  dependency to separate  $G_E^p$  and  $G_M^p$



# Polarized ep Elastic Scattering

- Directly measure  $G_E^p/G_M^p$  at a given  $Q^2$
- Combined with unpolarized cross section to separate  $G_E^p$  and  $G_M^p$
- Ratio measurement, lots of cancellation for systematics
- Overcome several difficulties for unpolarized technique:  $G_E^p$  at high  $Q^2$ , radiative correction...

## Double polarization, asymmetry measurements

$$A_{eN} \equiv \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

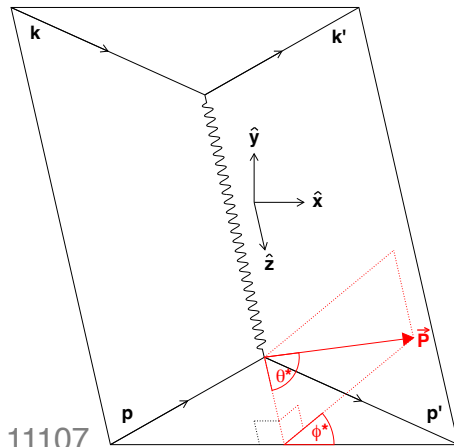
$$= P_{\text{beam}} P_{\text{targ}} [A_t \sin \theta^* \cos \phi^* + A_l \cos \theta^*]$$

$$A_t = -\sqrt{\frac{2\epsilon(1-\epsilon)}{\tau}} \frac{r}{1 + \frac{\epsilon}{\tau} r^2}$$

$$A_l = -\frac{\sqrt{1-\epsilon^2}}{1 + \frac{\epsilon}{\tau} r^2}$$

$$r \equiv G_E/G_M$$

arXiv:2212.11107

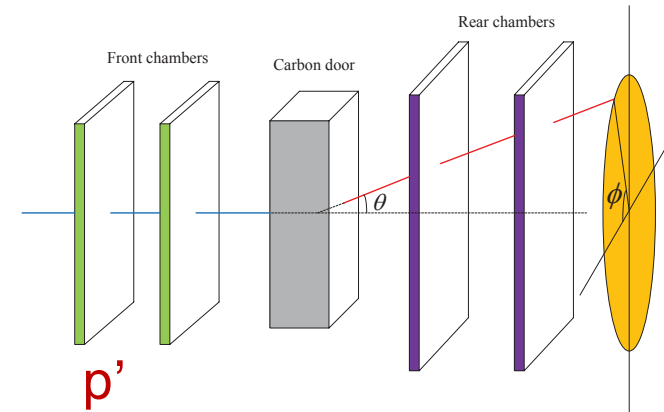


## Polarization transferred to final state proton

$$P_t = P_{\text{beam}} A_t$$

$$P_l = -P_{\text{beam}} A_l$$

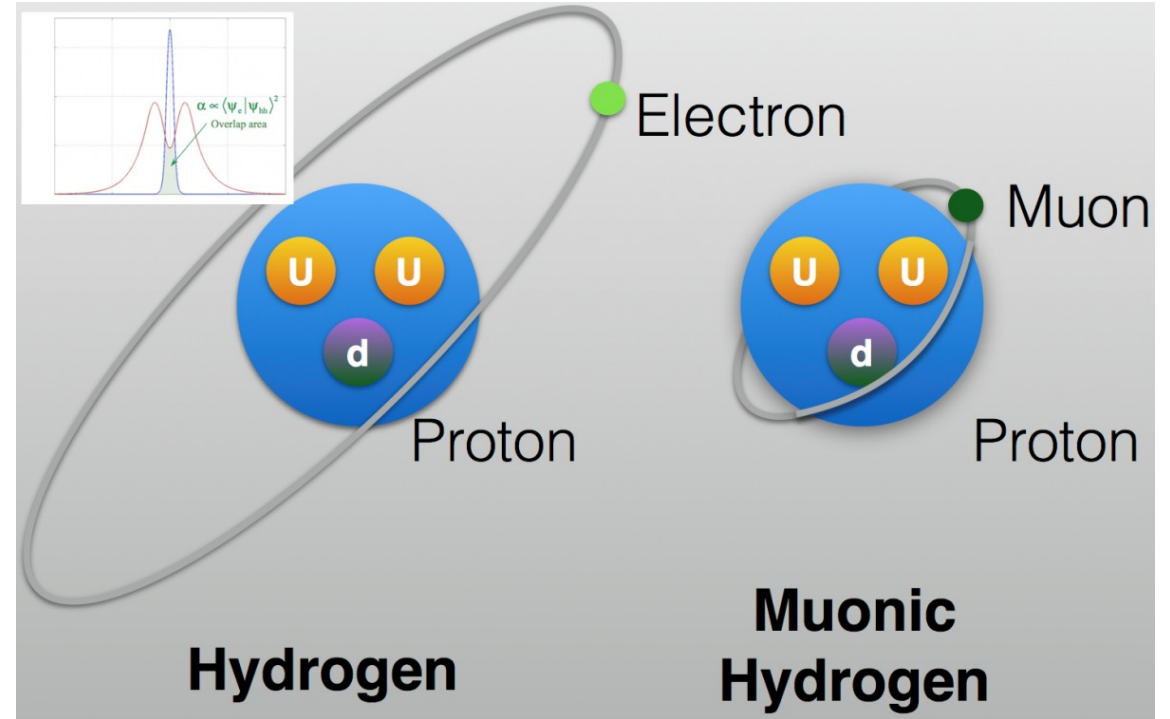
$$\frac{G_E}{G_M} = -\frac{P_t}{P_l} \sqrt{\frac{\tau(1+\epsilon)}{2\epsilon}} = -\frac{P_t}{P_l} \frac{E_e + E'_e}{2M} \tan\left(\frac{\theta_e}{2}\right)$$



# Ordinary Hydrogen v.s. Muonic Hydrogen

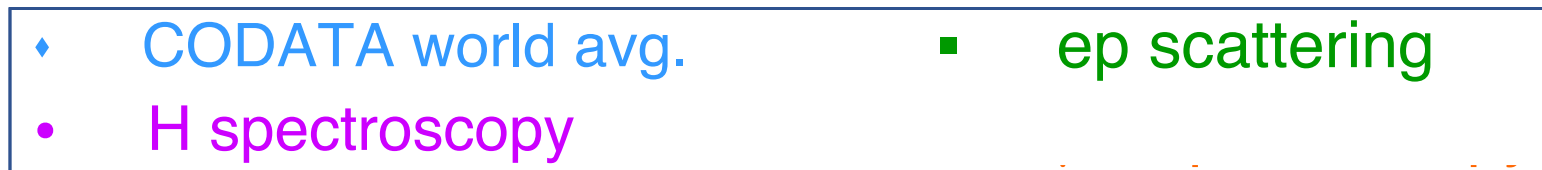
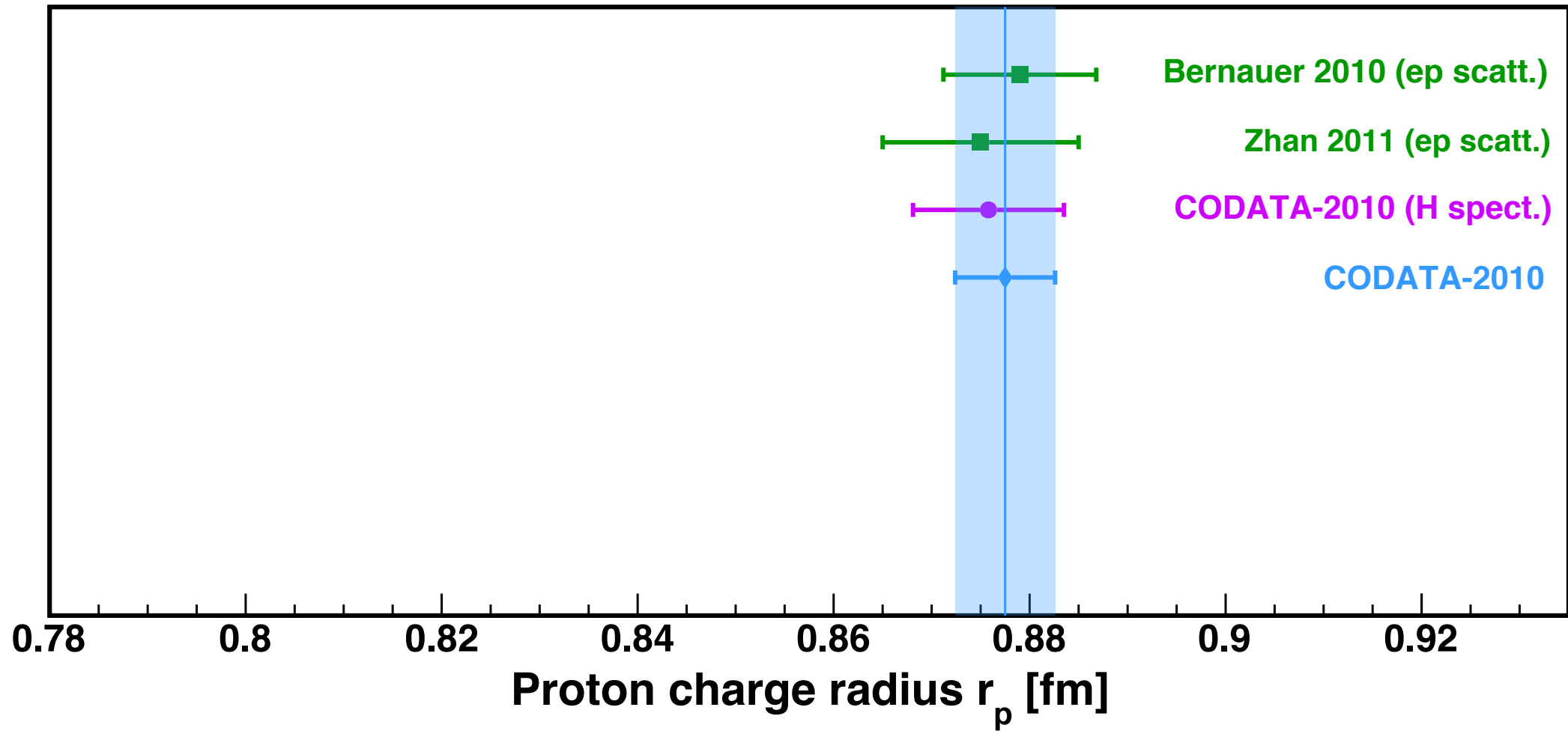
- One can do this with ordinary hydrogen or muonic hydrogen
- Muon is ~200 times heavier than electron
- Orbit much closer to proton, more sensitive to proton size

$$\langle r^{\text{orbit}} \rangle \simeq \frac{\hbar}{Z\alpha m_r c} n^2$$

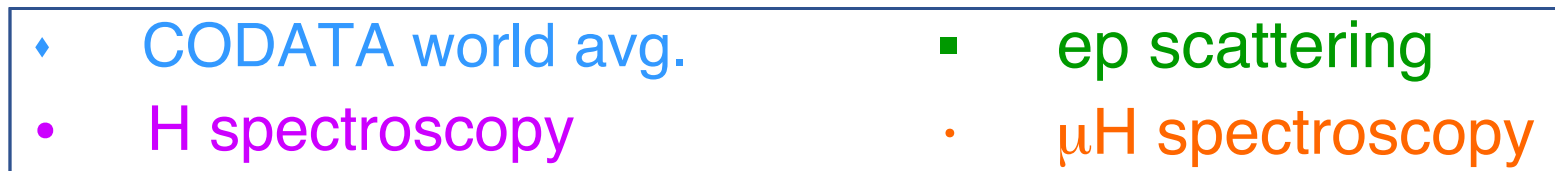
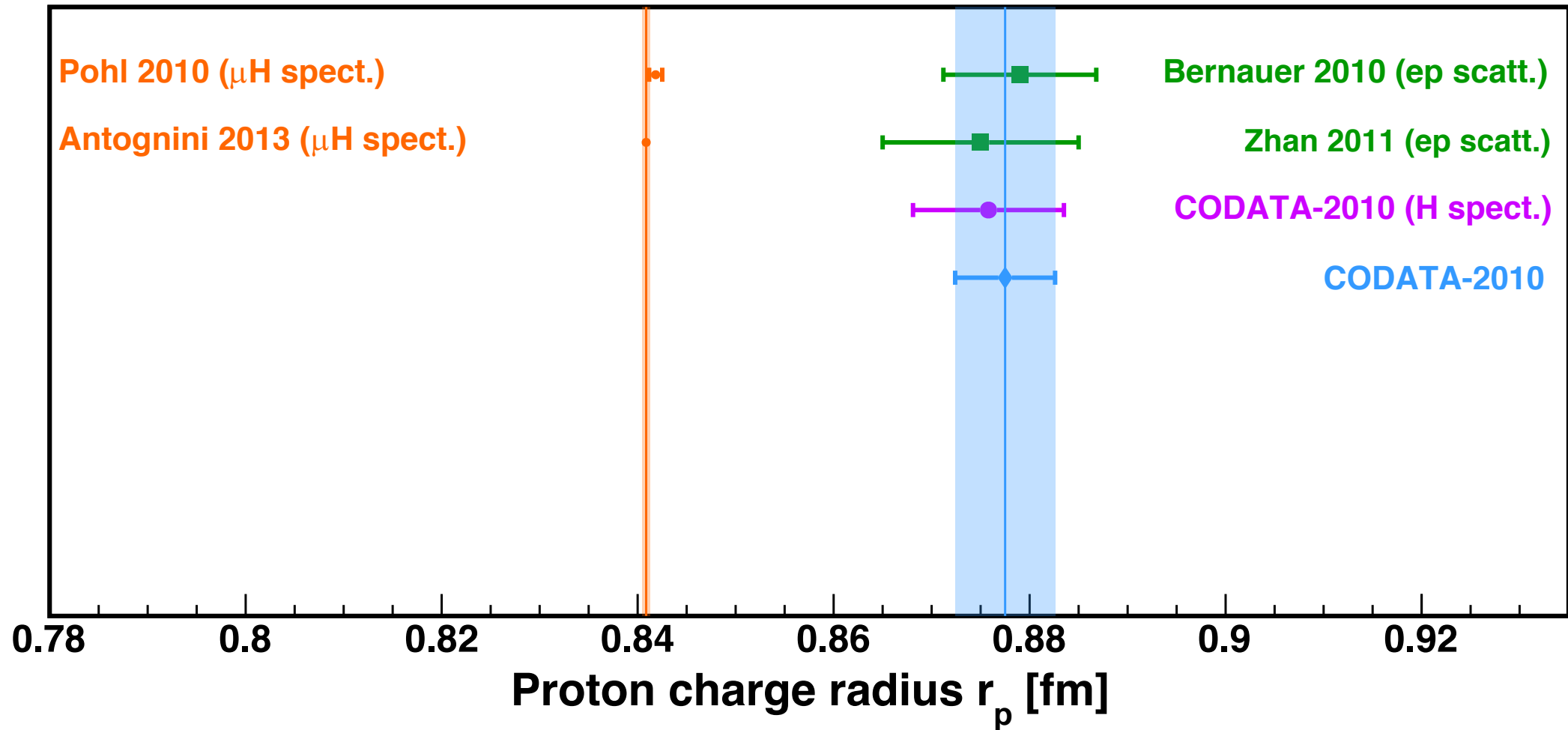


**Proton finite size effect in 2S-2P: 2% in  $\mu\text{H}$ , 0.015% in H**

# Proton Charge Radius

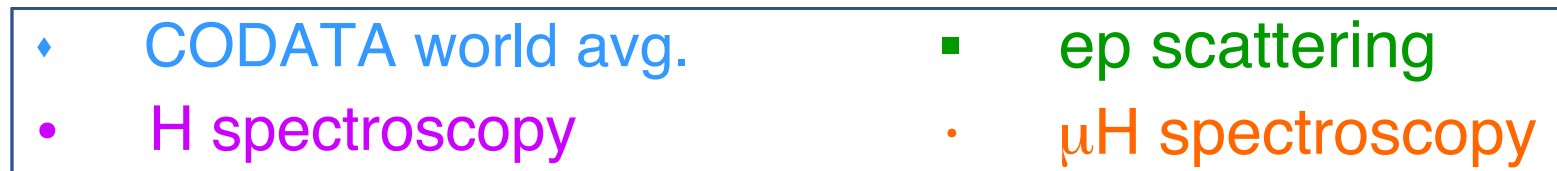
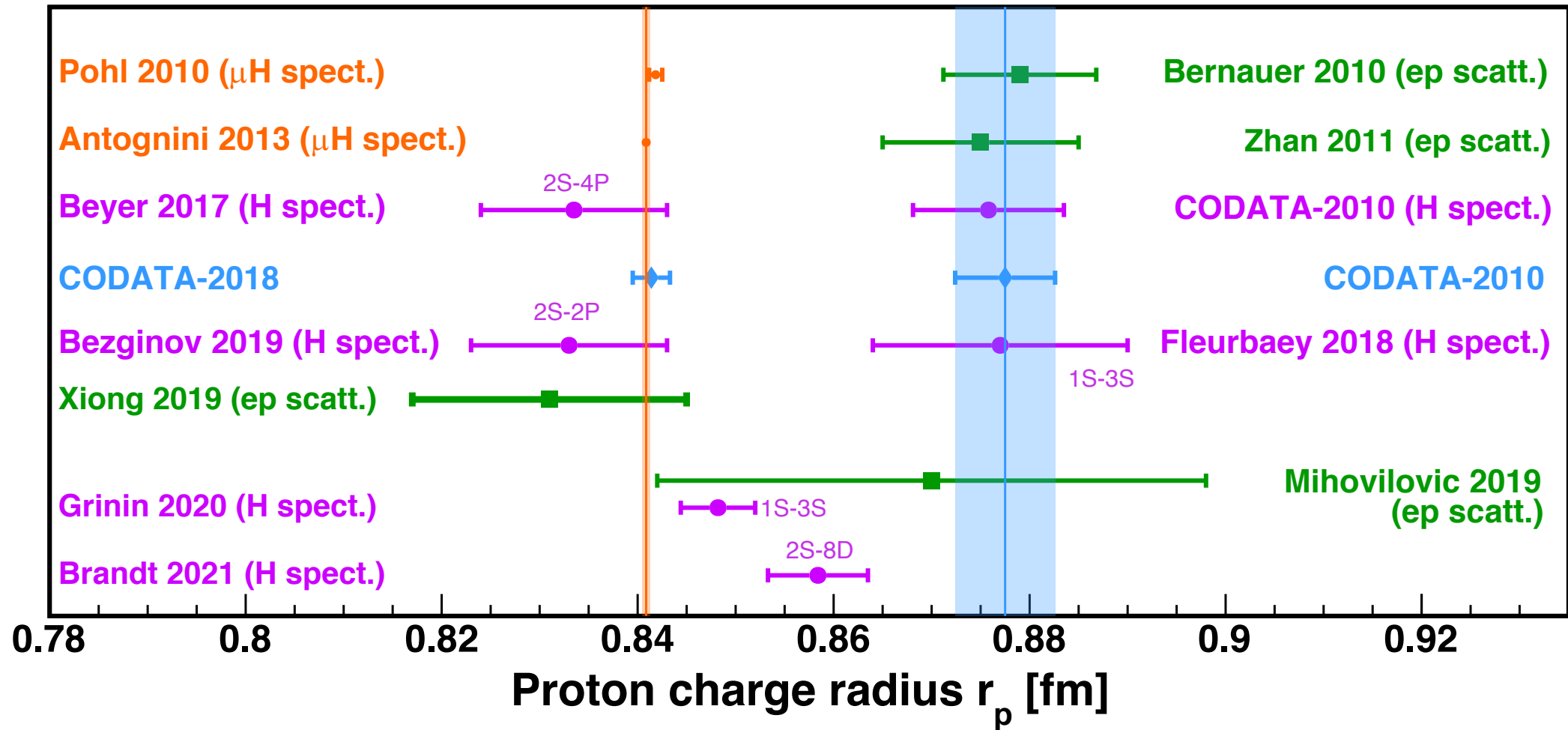


# Proton Charge Radius Puzzle



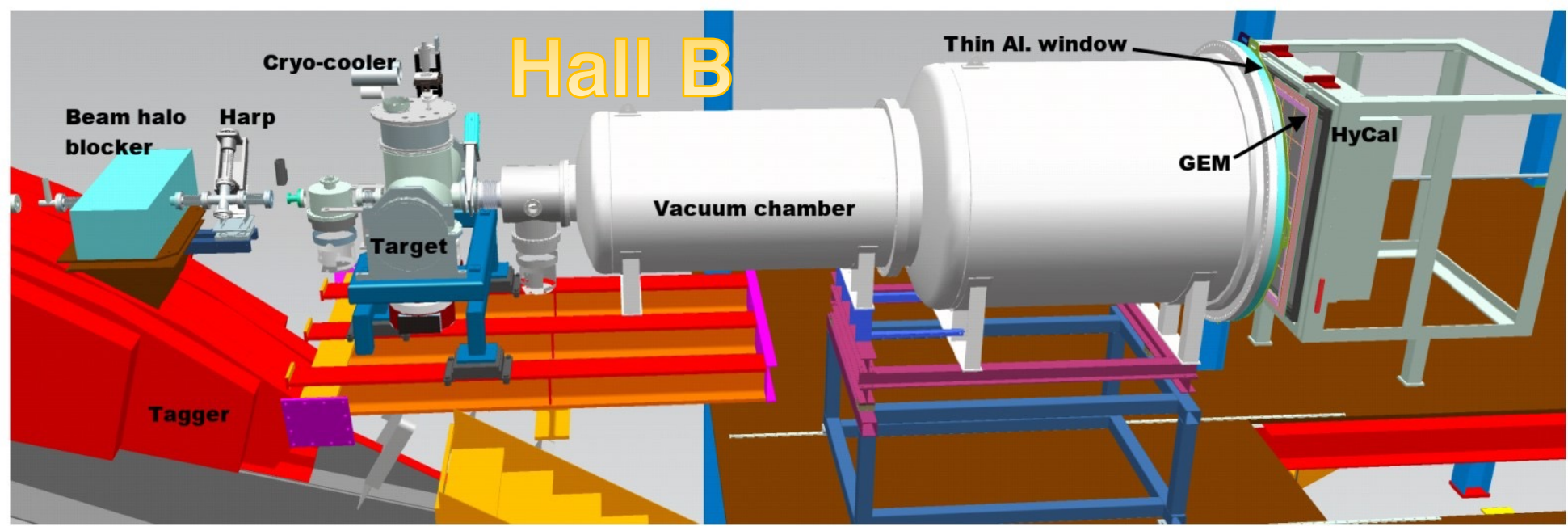
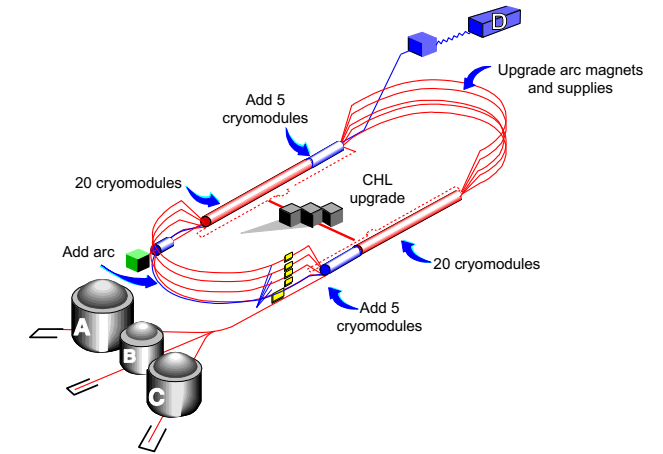


# Proton Charge Radius Puzzle



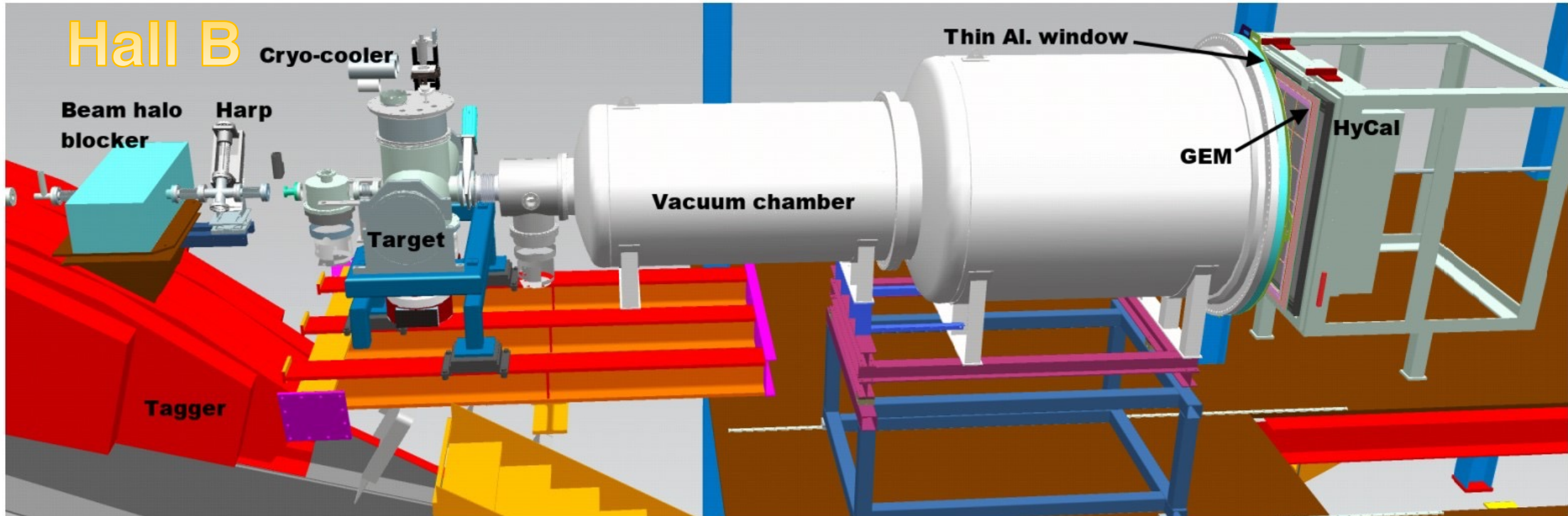
# PRad Experiment at Jefferson Lab

- Thomas Jefferson National Accelerator Facility (JLab), Newport News, VA
- Data taking May/June 2016, **1.1 GeV** and **2.2 GeV** e beams



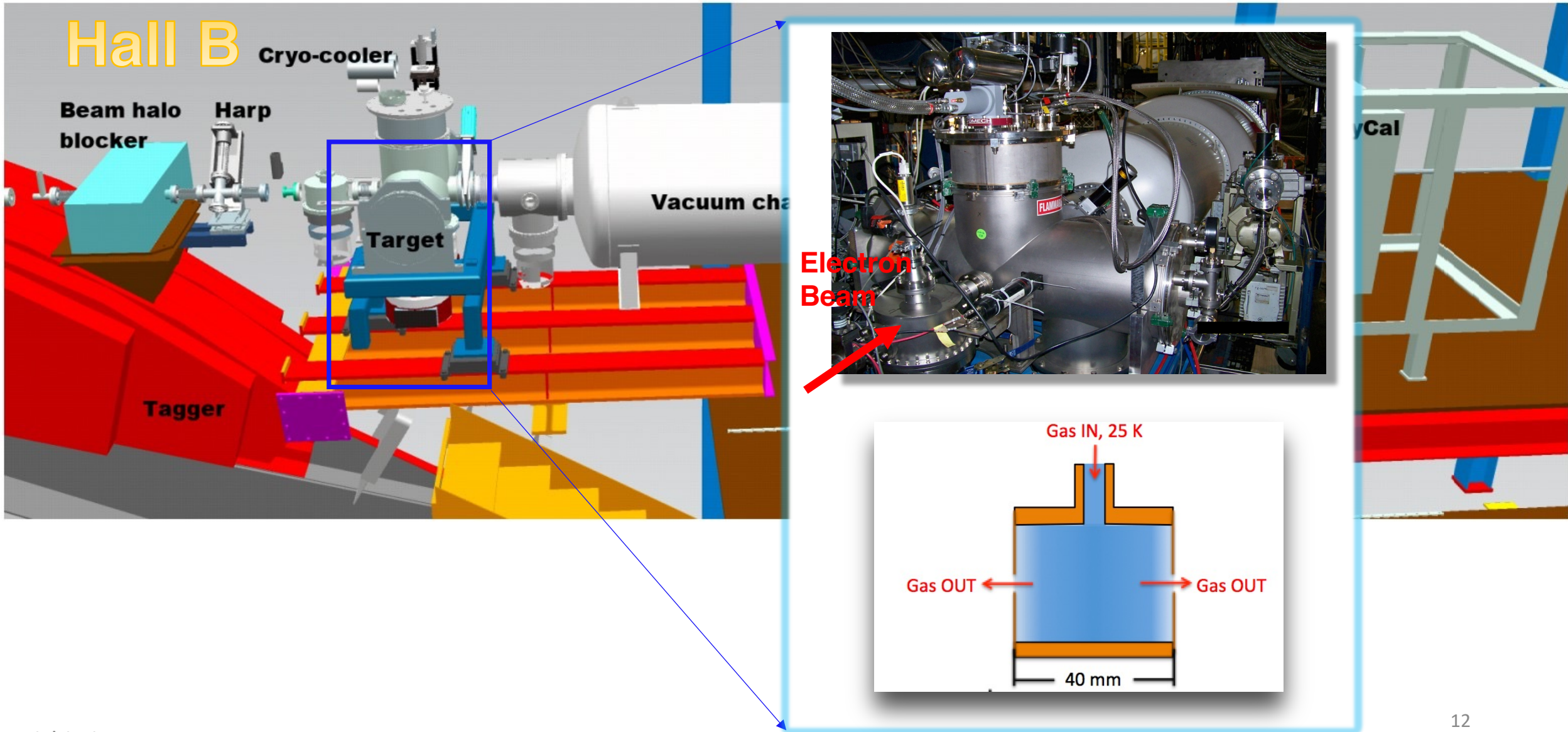
# PRad Experimental Apparatus

Large acceptance, small angle and non-spectrometer apparatus



# PRad Experimental Apparatus

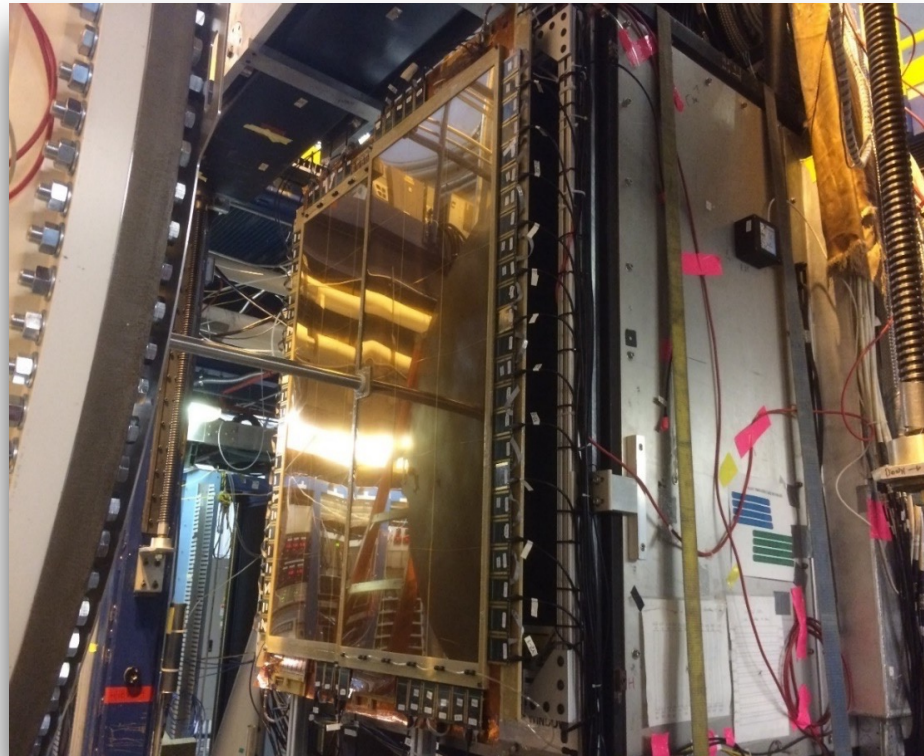
Large acceptance, small angle and non-spectrometer apparatus



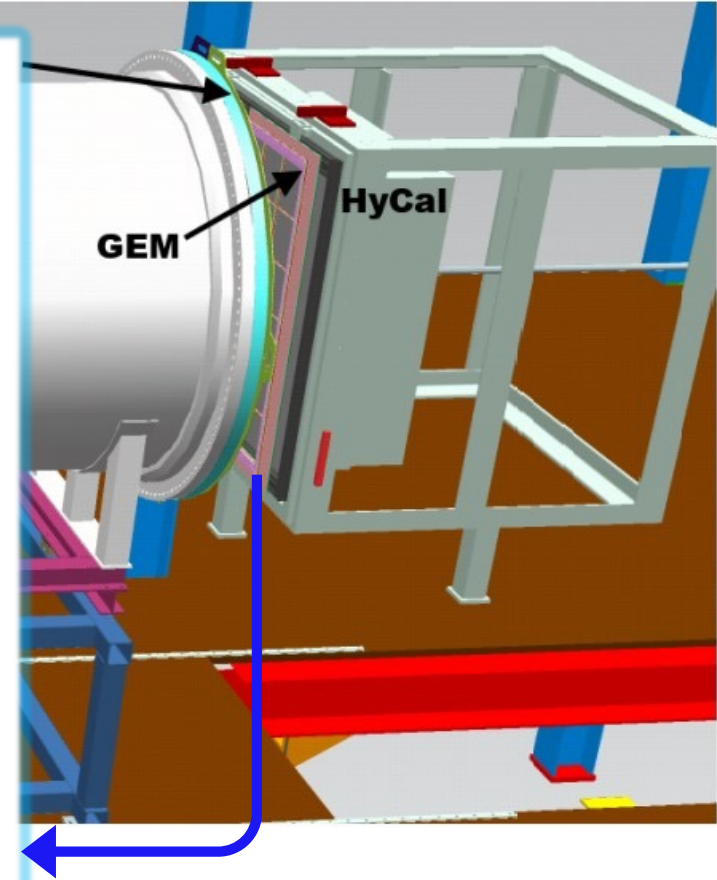
# PRad Experimental Apparatus

Large acceptance, small angle and non-spectrometer apparatus

Hall B



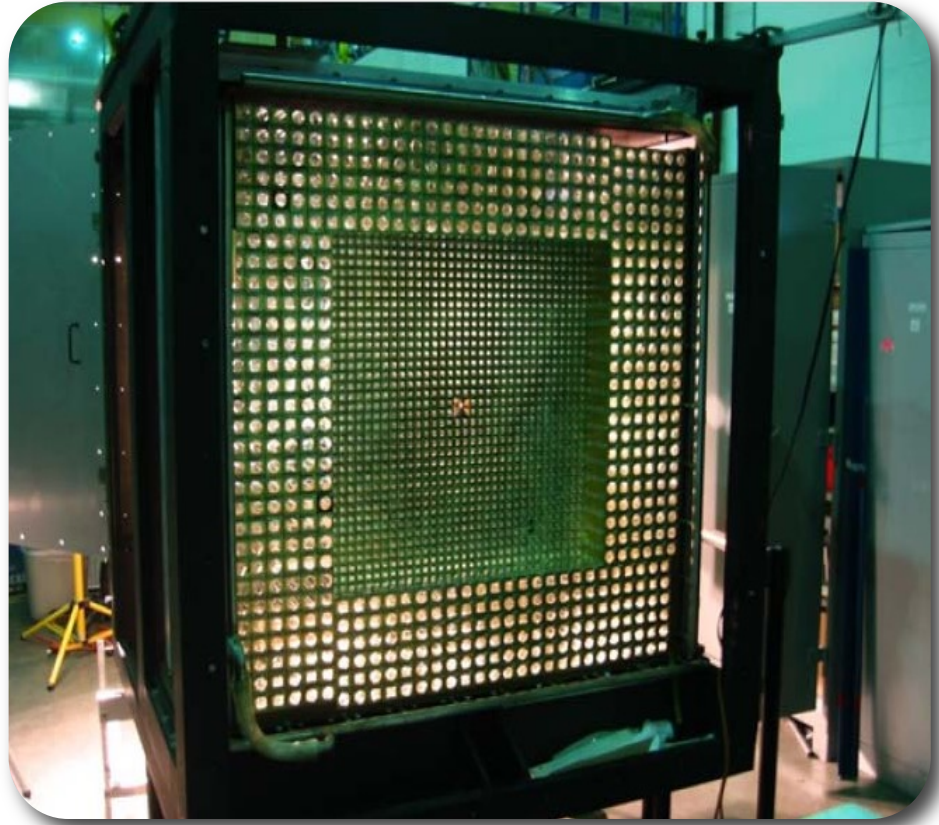
- Two large area GEM detectors
- Small overlap region in the middle
- Excellent position resolution ( $72 \mu\text{m}$ )



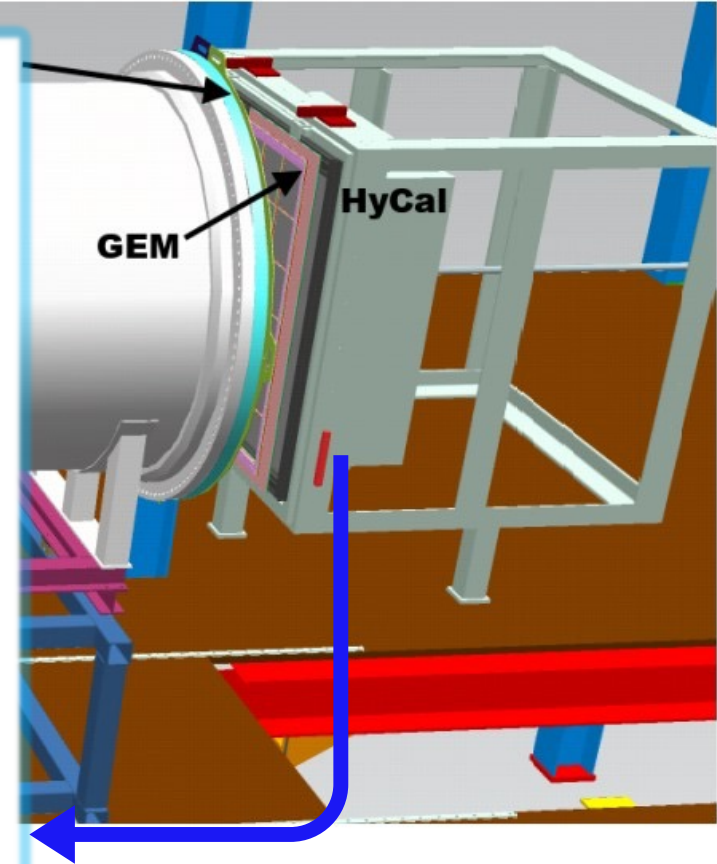
# PRad Experimental Apparatus

Large acceptance, small angle and non-spectrometer apparatus

Hall B



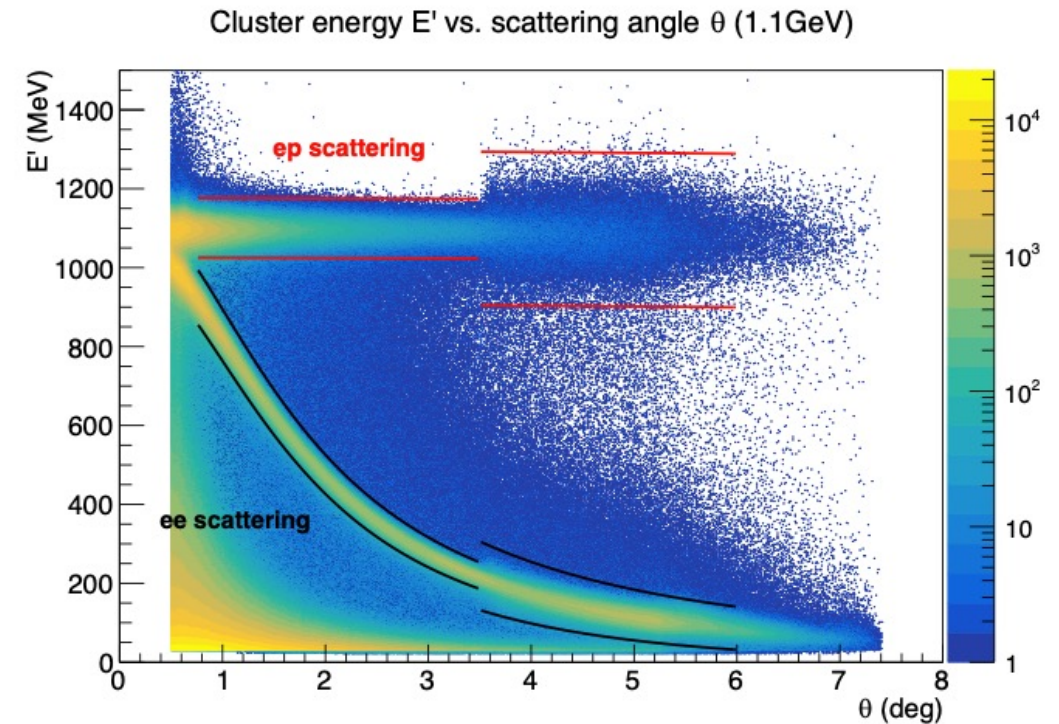
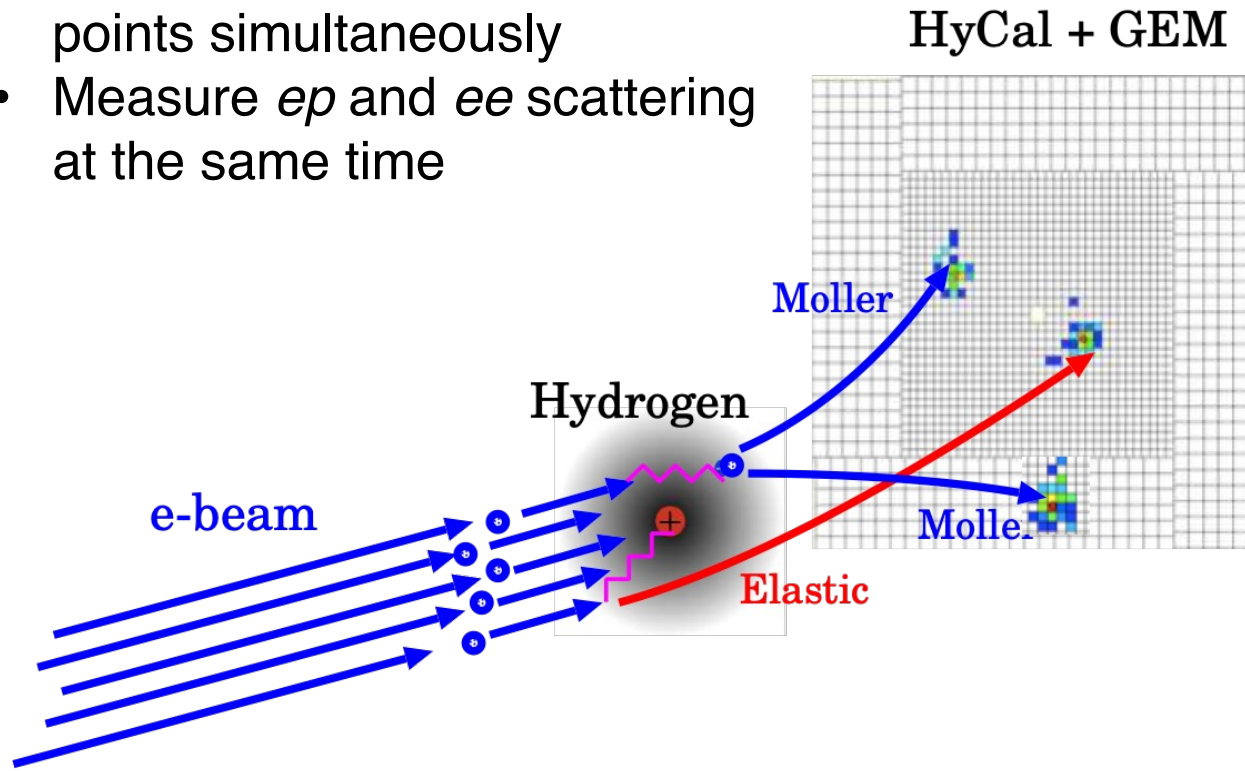
- Hybrid EM calorimeter (HyCal)
  - Inner 1156  $\text{PbWO}_4$  modules
  - Outer 576 lead glass modules
- Scattering angle coverage:  $\sim 0.7^\circ$  to  $7.0^\circ$
- Full azimuthal angle coverage
- High resolution and efficiency



# PRad Experiment at Jefferson Lab

## Non-spectrometer apparatus

- Large acceptance:
  - Measure multiple  $Q^2$  data points simultaneously
  - Measure  $ep$  and  $ee$  scattering at the same time

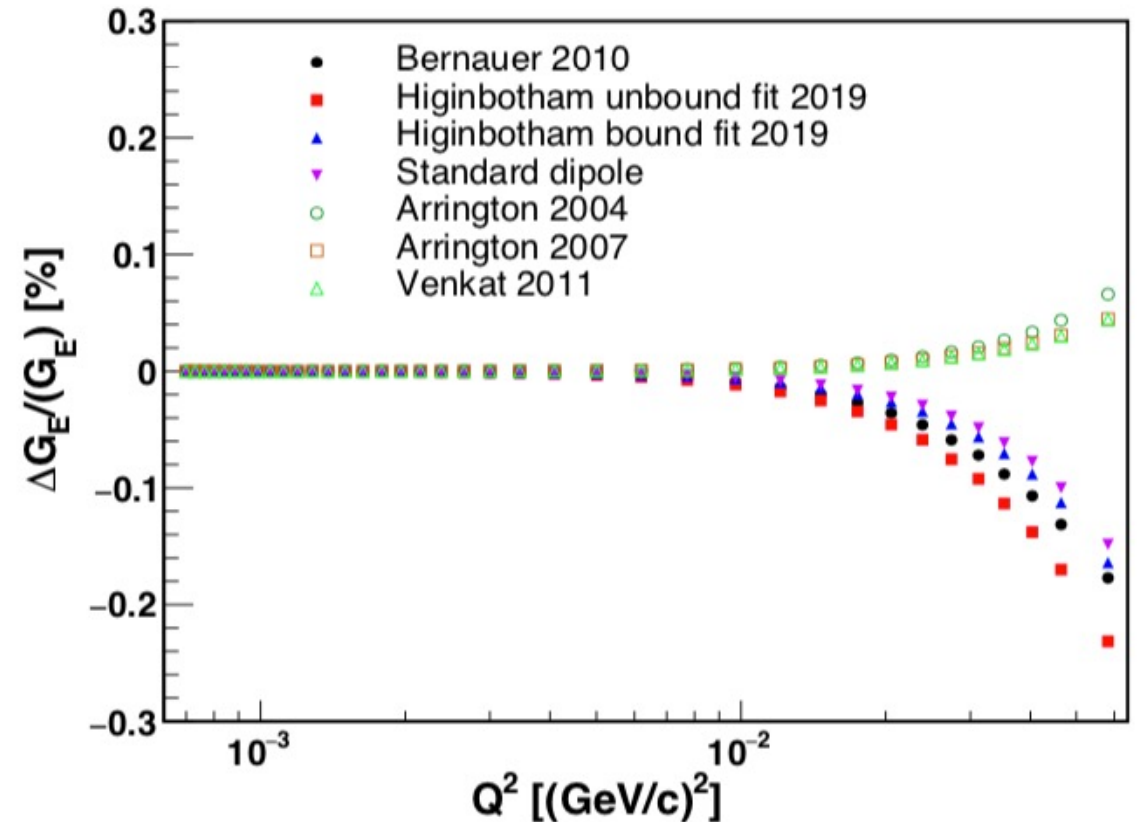
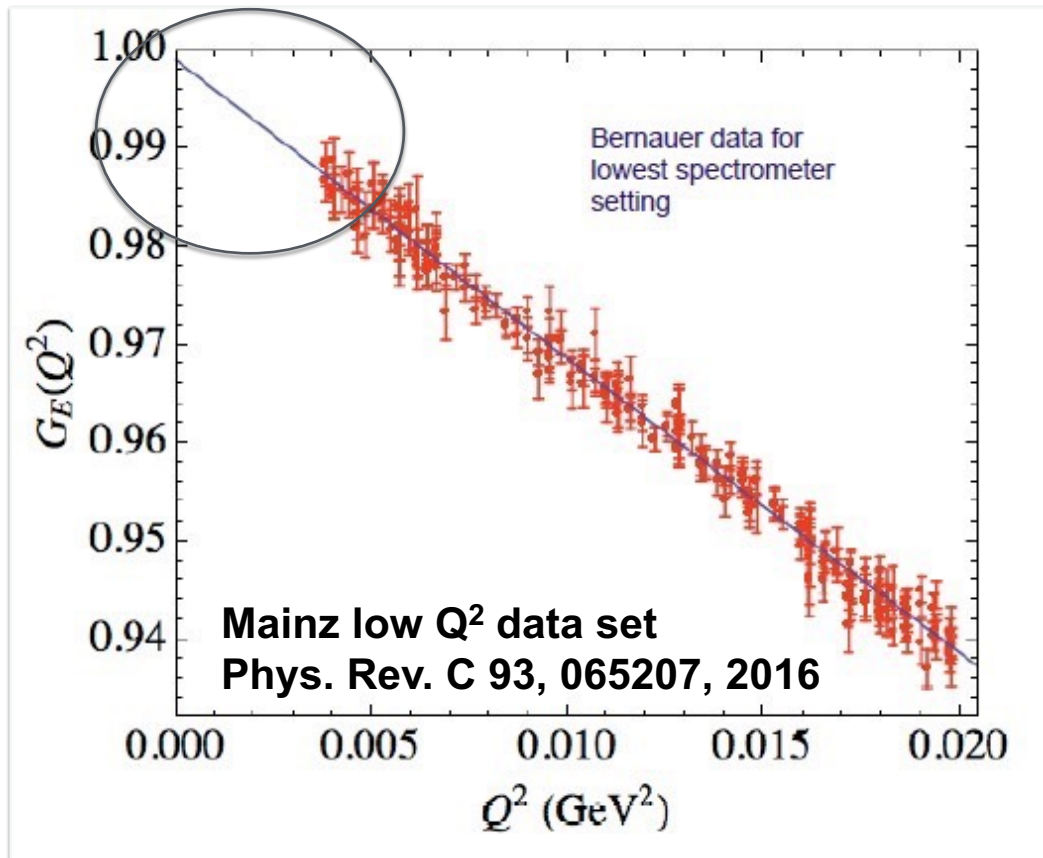


# PRad Experiment at Jefferson Lab

## Non-spectrometer apparatus

- Small scattering angle ( $0.5^\circ$ - $7.5^\circ$ ):
  - Unprecedented low  $Q^2$  ( $\sim 2 \times 10^{-4}$  GeV $^2$ )
  - Minimize  $G_M^p$  contribution

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \left( \frac{E'}{E} \right) \frac{1}{1+\tau} \left( G_E^{p2}(Q^2) + \frac{\tau}{\varepsilon} G_M^{p2}(Q^2) \right)$$



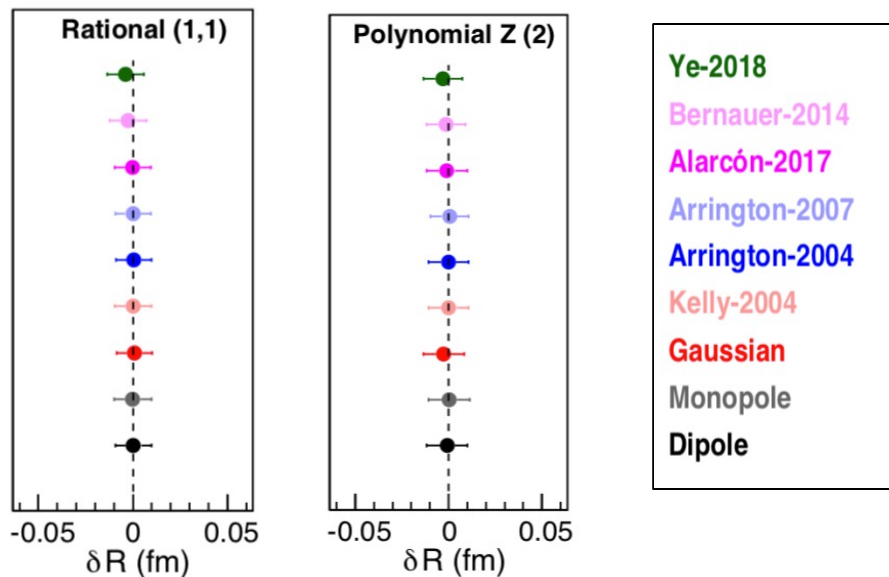


# PRad Experiment at Jefferson Lab

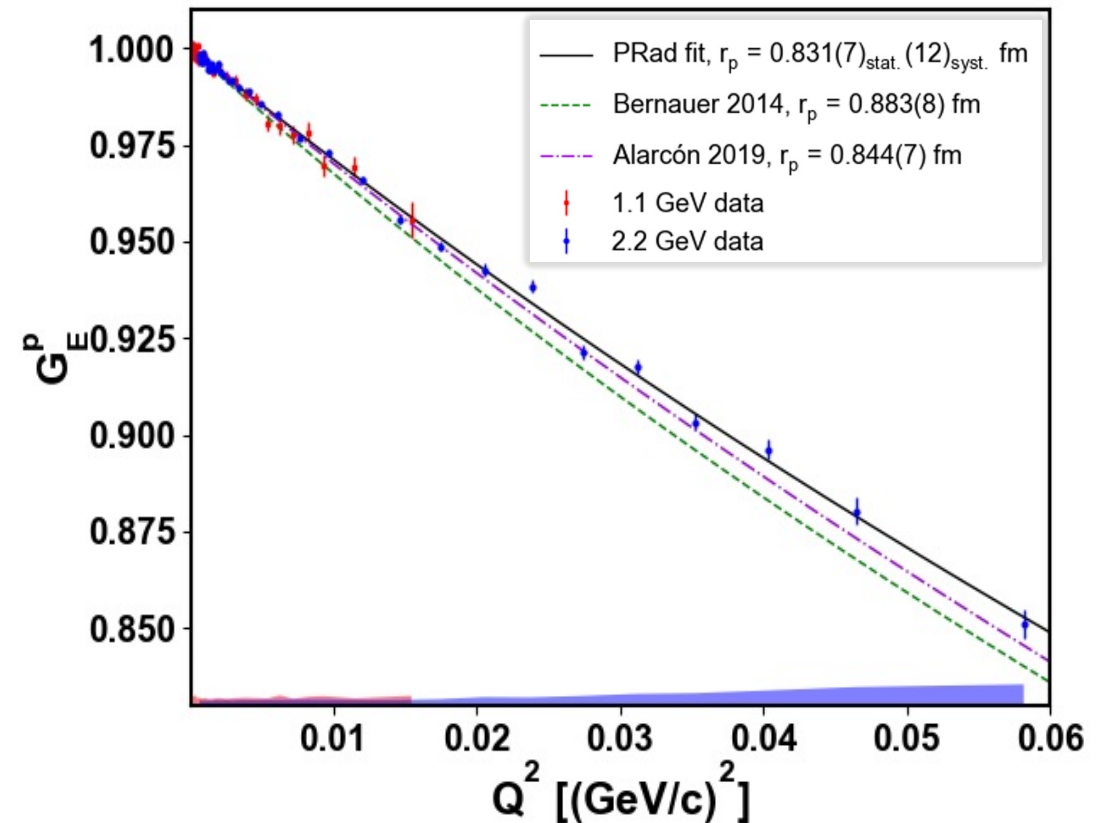
## Non-spectrometer apparatus

- Numerous functional forms tested with wide range of  $G_E$  parameterizations, using PRad kinematic range and uncertainties: X. Yan *et al.* Phys. Rev. C98, 025204 (2018)
- Rational (1,1), 2<sup>nd</sup> order z transformation and 2<sup>nd</sup> order continuous fraction identified as robust fitters with reasonable uncertainties

$$r_p = 0.831 \pm 0.007 \text{ (stat.)} \pm 0.012 \text{ (syst.) fm}$$



$$\text{Rational (1,1): } \frac{1 + p_1 Q^2}{1 + p_2 Q^2}$$



Nature 575 (2019) 7781

# Highlights of Future Lepton Scattering Experiments

## Muon scattering

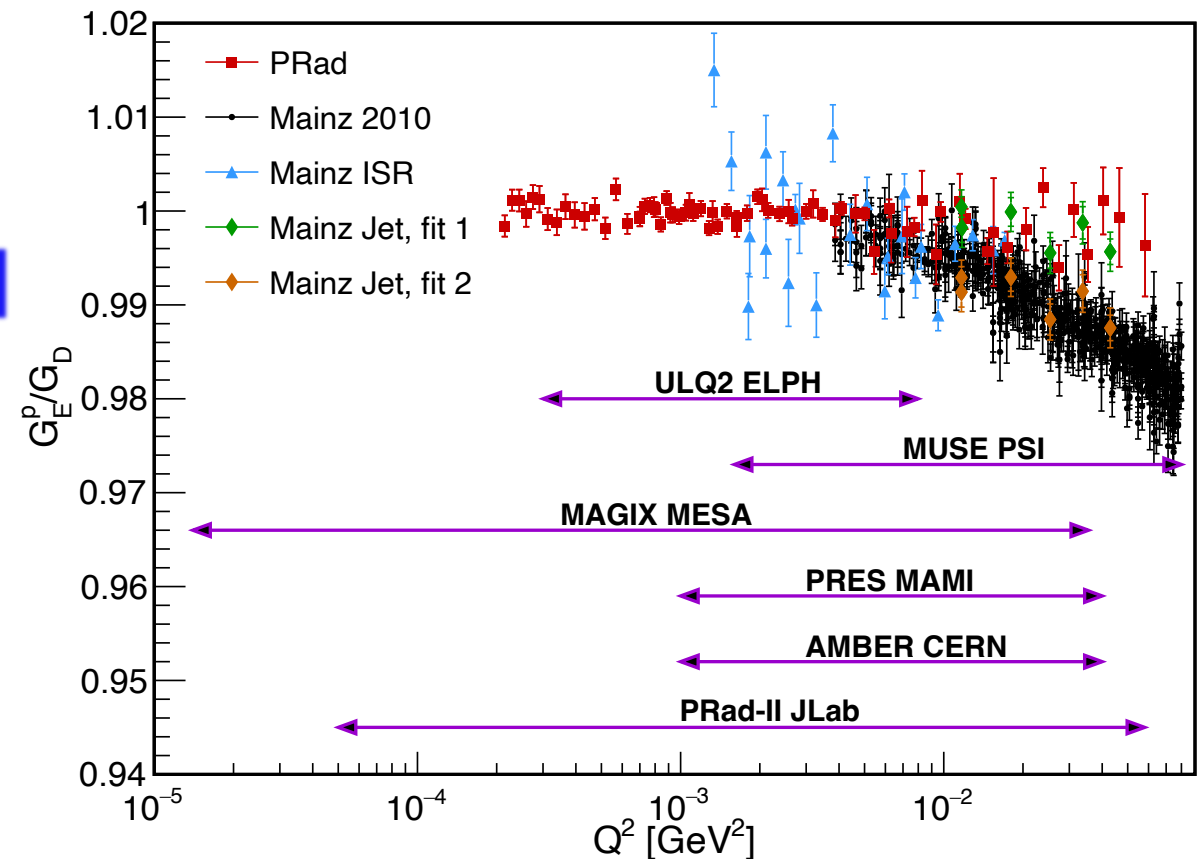
- MUSE exp. at PSI
  - First  $r_p$  measurement using muon
  - 4 types of incident leptons:  $e^\pm$  and  $\mu^\pm$
- AMBER exp. at CERN
  - 100 GeV muon beam, detecting scattered muon and recoiled proton
  - Ultra-small scattering angle, minimize  $G_M$
  - Smaller RC for muon

## Electron scattering

- Prad-II exp. at JLab
  - ultra-precise  $r_p$  measurement ( $\sim 4$  times smaller uncertainty than PRad)
- PRES exp. at Mainz
  - detecting both scattered electron and recoiled proton
- MAGIX exp. at Mainz
  - Using jet target
- ULQ2 exp. at Tohoku University, Japan
  - Normalize to the well-known  $e^{-12}\text{C}$  cross section

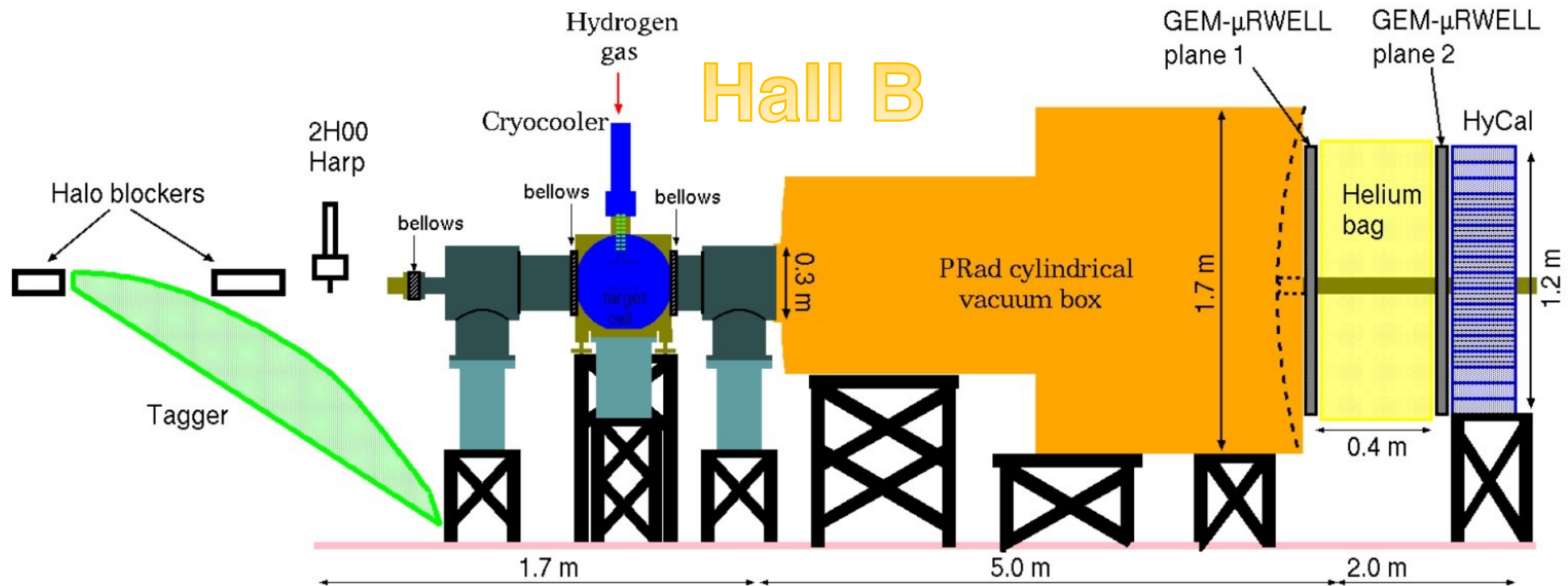
No  $\mu$ -p scattering result yet

Projected  $Q^2$  coverage



# PRad-II Experiment

- JLab PAC 48 approved **PRad-II** (PR12-20-004) with the highest scientific rating “A”
- Goal: reach ultra-high precision ( $\sim 4$  times smaller total uncertainty), resolve tension between modern  $e-p$  scattering results
  - Additional new GEM plane
  - Full DAQ and readout system upgrade
  - New scintillating detector, help reaching  $Q^2 \sim 10^{-5} \text{ GeV}^2$



# PRad-II Experiment

- Adding tracking capacity (**second GEM plane**)
  - Improve GEM efficiency measurement

**Bin-by-bin method:** taking the ep/ee ratio within the same angular bin

**Good:** Detector acc. and eff. cancel at leading order

**Bad:** Easily introduce Q<sup>2</sup>-dependent syst. from Moller

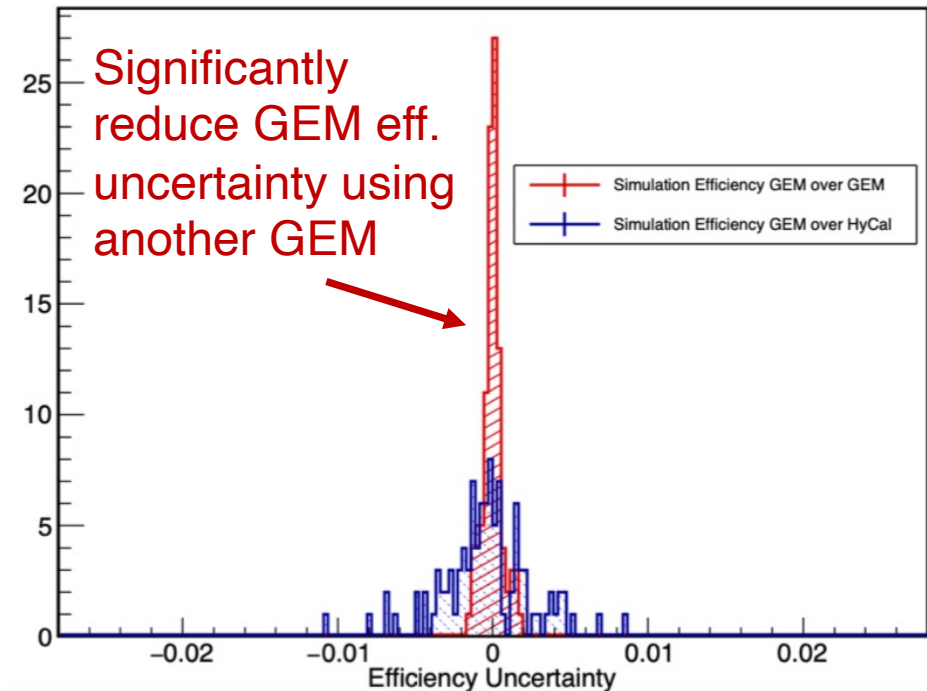
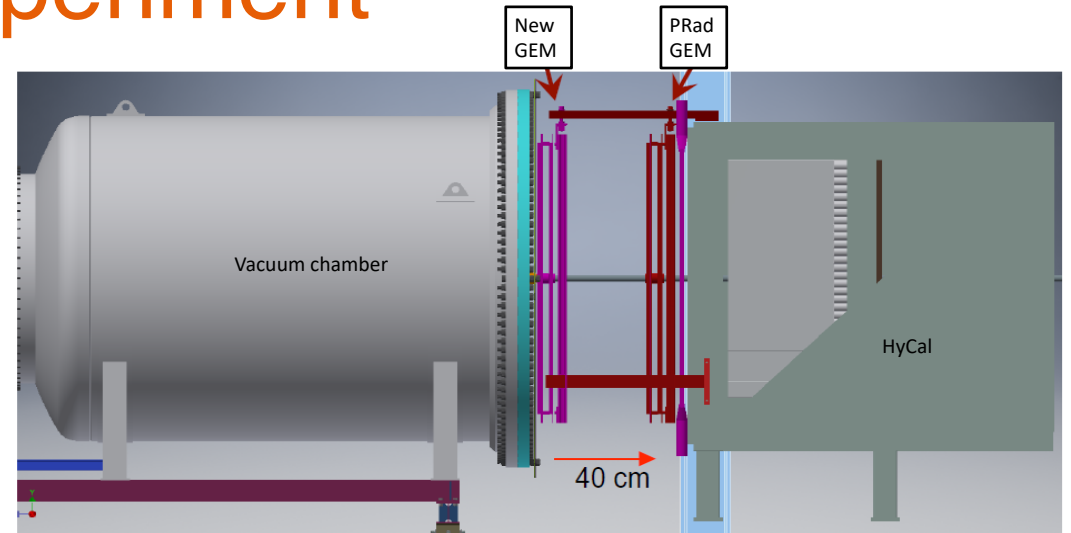
$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[ \frac{N_{\text{exp}}^{\text{yield}}(ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta) \cdot \epsilon_{\text{geom}}^{e^-e^-} \cdot \epsilon_{\text{det}}^{e^-e^-}}{N_{\text{exp}}^{\text{yield}}(e^-e^- \rightarrow e^-e^-) \cdot \epsilon_{\text{geom}}^{ep} \cdot \epsilon_{\text{det}}^{ep}} \right] \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$

**Integrated Moller method:** select ee in an angular range, and use it to normalize all ep

**Good:** Not limited by Moller acceptance, Moller uncertainty only affect normalization

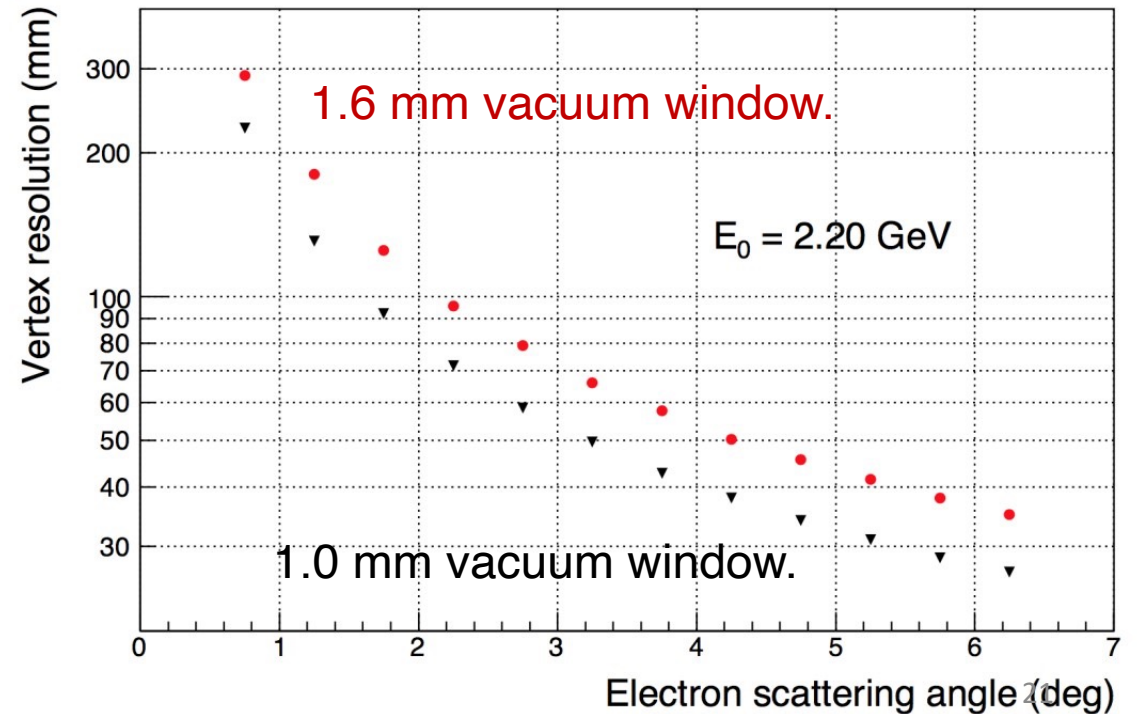
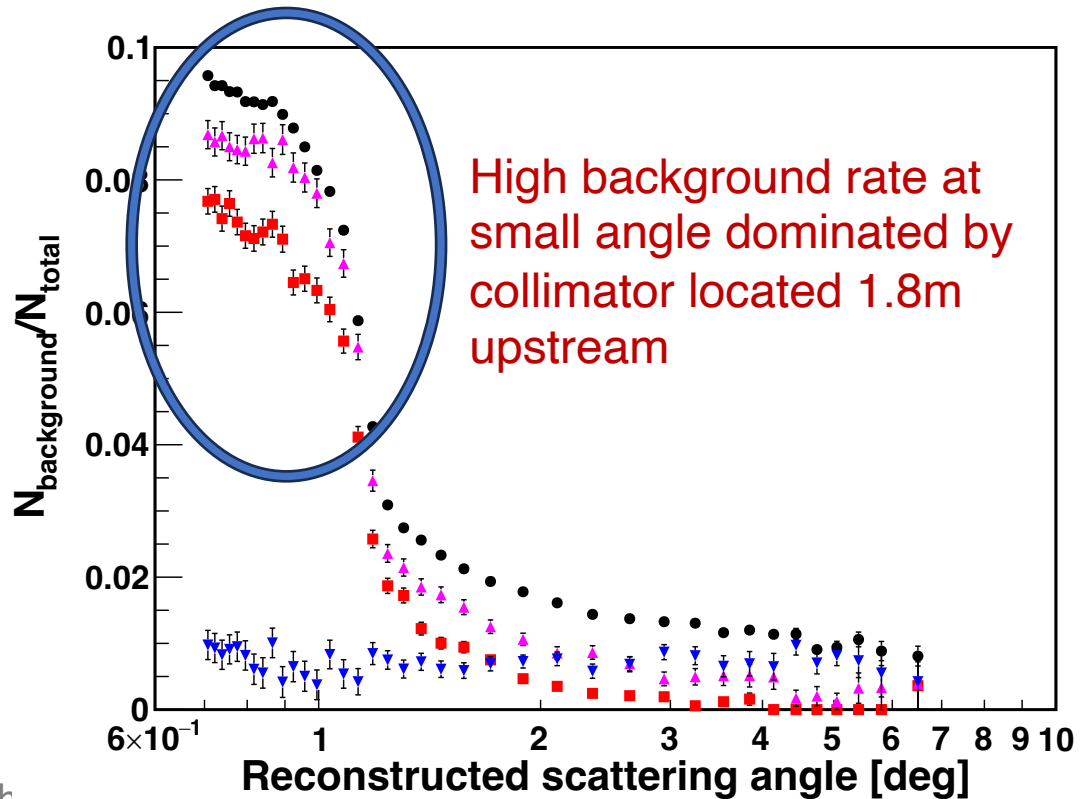
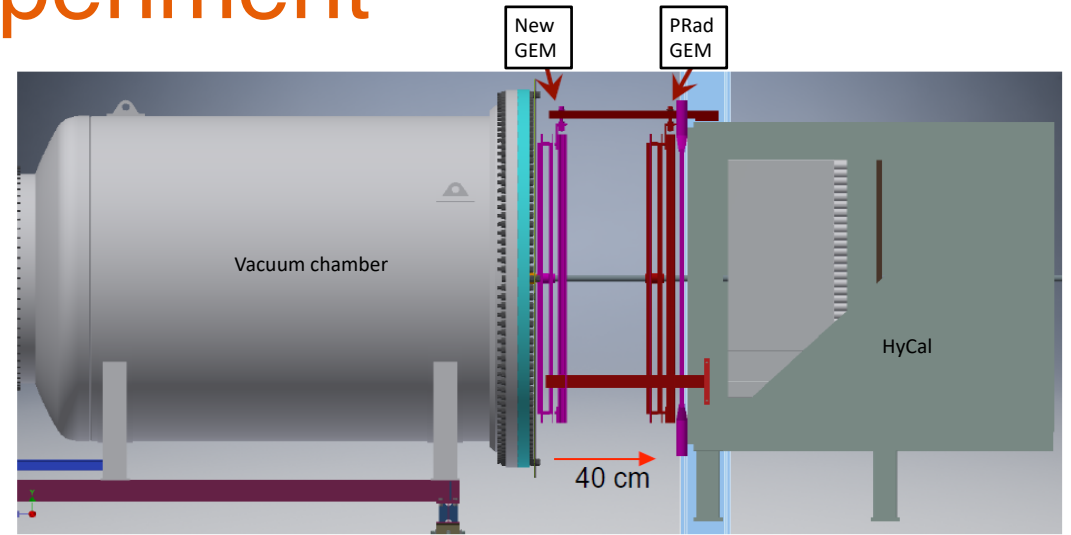
**Bad:** Need accurate GEM efficiency measurement

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[ \frac{N_{\text{exp}}^{\text{yield}}(ep, \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^-, \text{ on PWO})} \right] \frac{\epsilon_{\text{geom}}^{e^-e^-}(\text{all PWO}) \cdot \epsilon_{\text{det}}^{e^-e^-}(\text{all PWO})}{\epsilon_{\text{geom}}^{ep}(\theta_i \pm \Delta\theta) \cdot \epsilon_{\text{det}}^{ep}(\theta_i \pm \Delta\theta)} \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$



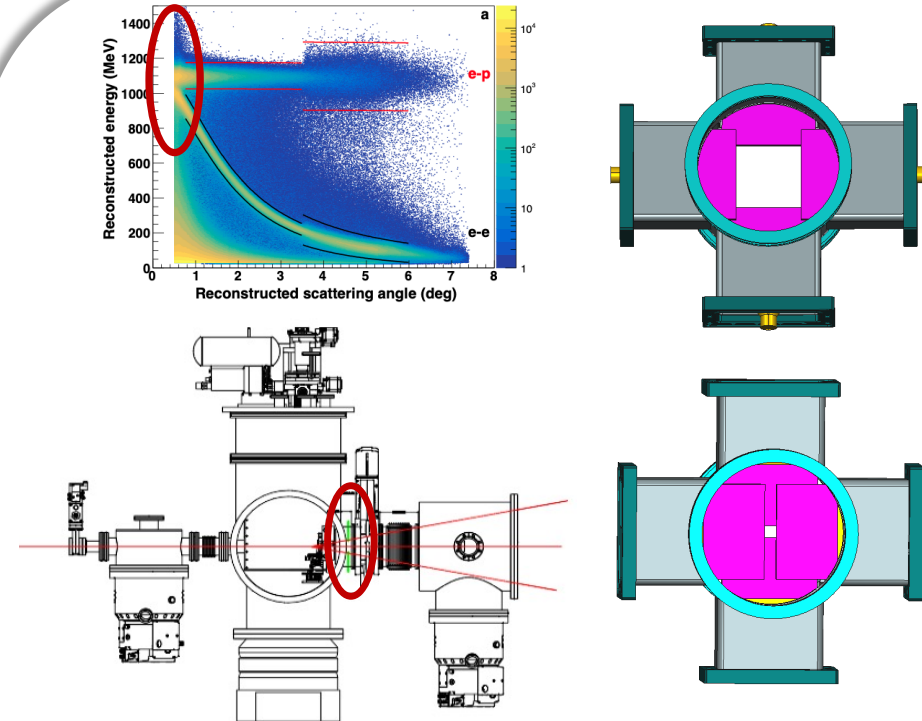
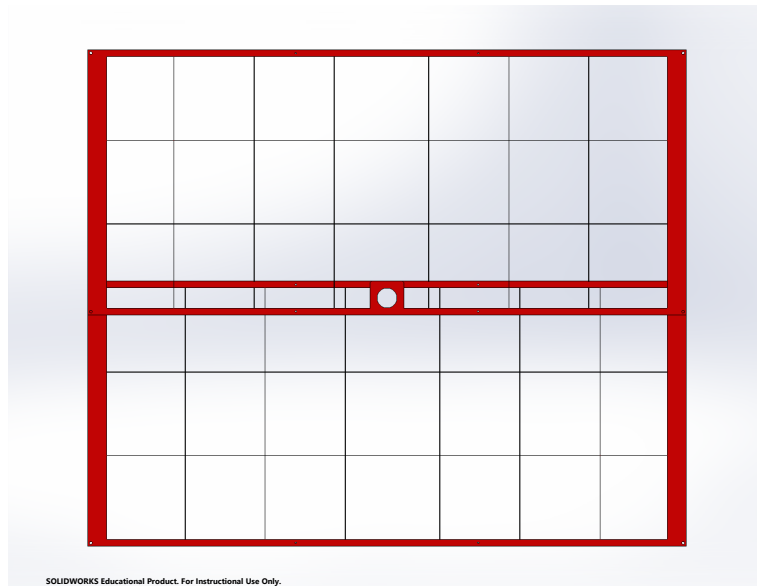
# PRad-II Experiment

- Adding tracking capacity (**second GEM plane**)
  - Improve GEM efficiency measurement
  - Vertex-z reconstruction for *ep* to reject upstream background



# PRad-II Experiment

- 4 new GEM chambers to assemble 2 tracking layers.
  - Detector fabrication expected to be finished for all GEM parts, by **March 2025**.
  - All readout electronics ordered, expected by **this November**.
  - Will be ready for installation and testing by **mid- spring, 2025**.



- 4 movable scintillator detectors placed next to the H<sub>2</sub> gas flow target chamber.
  - Conceptual design done, engineering design in progress
  - Manufacturing: **by Spring, 2025**
  - Estimated time for test in beamline: **Summer, 2025**.

# Preparation of PRad-II Experiment

- All FASTBUS crates with power supplies removed
- 5 new VXS crates is planned to install in next few weeks
- HyCal recently re-positioned and refurbishing on-going
- Planned to finish all tests by end of this year



# Preparation of PRad-II Experiment

- PRad target system and control rack moved to the experimental staging building
- Performing test and getting ready for the experiment

Main target vessel

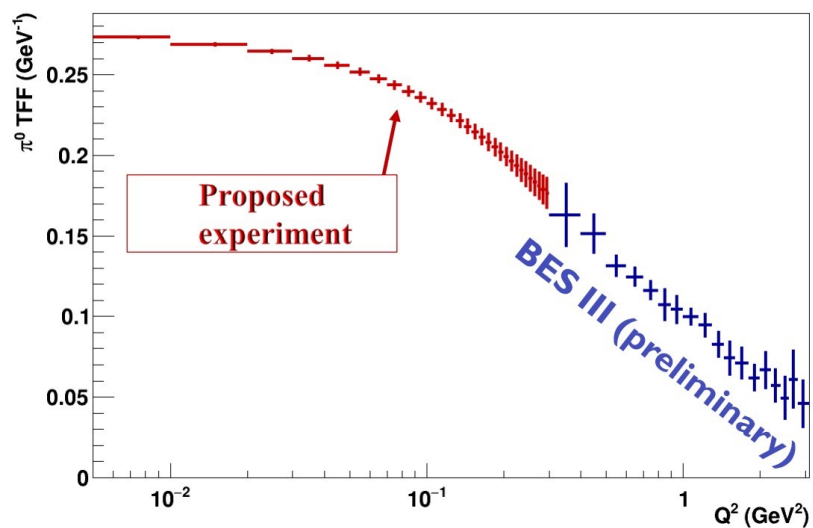


Control rack

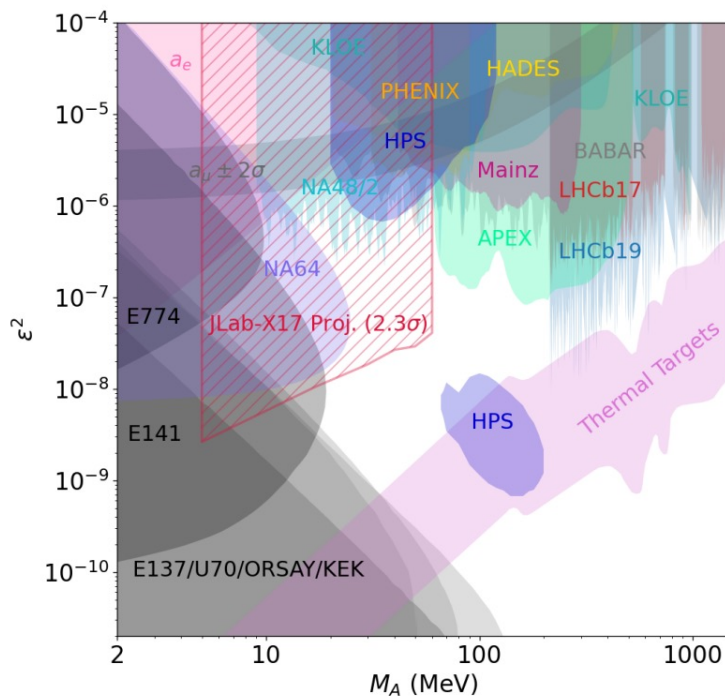


# Other Experiments with PrimEx/PRad Setup

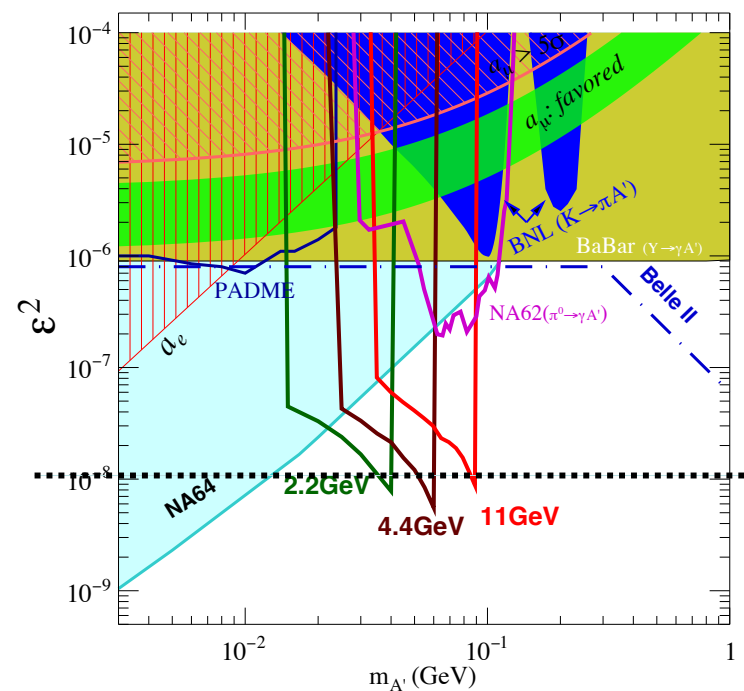
Precision Measurement of the Neutral Pion Transition Form Factor  
Rate A-, 67 days



A Direct Detection Search for Hidden Sector New Particles in the 3-60 MeV Mass Range  
Rate A, 60 days



A Dark Photon Search with a JLab Positron Beam  
Rate A-, 55 days



# Summary

- Puzzle considered **partially resolved**, but many problems remain
  - Tensions between some new H spec. results
  - Form factor difference between PRad and Mainz data
  - New physics may still be there
- Many future experiments on proton charge radius and form factors, and push precision frontier
  - New uH measurement for 1S HFS, 2S-2P transition...
  - First  $r_p$  measurement using muon scattering: MUSE and AMBER
  - PRad-II experiment with  $\delta_r \sim 0.0036$  fm, aim to be **most precise** scattering result, new search for lepton-universality violation
    - Ready for ERR review in Spring 2025
    - Experiment ready to run from Fall 2025

# PRad/PRad-II Collaboration



**Duke University, NC A&T State University,  
Mississippi State University, Idaho State University,  
University of Virginia, Jefferson Lab,  
Argonne National Lab,  
University of North Carolina at Wilmington,  
Kharkov Institute of Physics and Technology,  
MIT, Old Dominion University, ITEP,  
University of Massachusetts, Amherst  
Hampton University, College of William & Mary,  
Norfolk State University, Yerevan Physics Institute  
Shandong University**

## PRad-II

### Graduate students:

**Yining Liu (Duke)  
Erik Wrightson (MSU)  
Buddhiman Tamang(MSU)  
Yuan Li (SDU)**

### Post-docs:

**Tyler Hague (NC A&T/LBNL)  
Aruni Nadeeshani(MSU)**

## PRad

### Graduate students (Thesis students):

**Chao Peng (Duke)  
Li Ye (MSU)  
Weizhi Xiong (Duke)  
Xinzhan Bai (UVa)**

### Post-docs:

**Chao Gu (Duke)  
Xuefei Yan (Duke)  
Mehdi Meziane (Duke)  
Krishna Adhikari (MSU)  
Maxime Lavillain (NC A&T )  
Latif-ul Kabir (MSU)**

# Backup

# Extracting Form Factors

- One of the methods for form factor extraction is the well known Rosenbluth separation:

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \left(\frac{E'}{E}\right) \frac{1}{1+\tau} \left(G_E^{p2}(Q^2) + \frac{\tau}{\epsilon} G_M^{p2}(Q^2)\right)$$

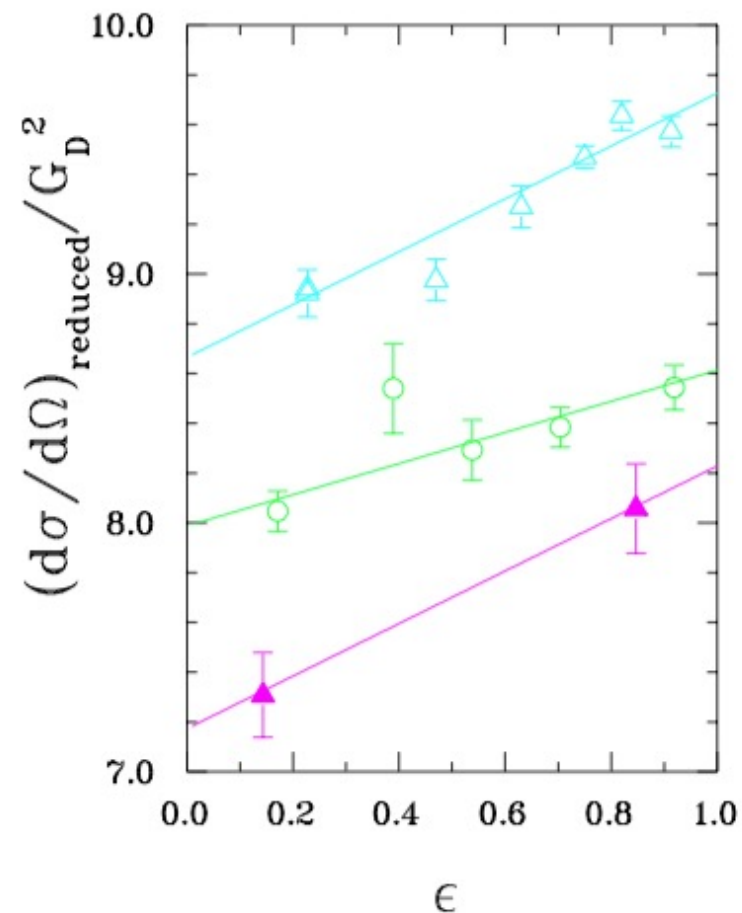


$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{reduced}} = G_M^{p2}(Q^2) + \frac{\epsilon}{\tau} G_E^{p2}(Q^2)$$

$$\tau = \frac{Q^2}{4M_p^2} \quad \epsilon = \left[1 + 2(1 + \tau) \tan^2 \frac{\theta}{2}\right]^{-1}$$

- Measure  $\sigma_{\text{reduced}}$  at same  $Q^2$  but different values of  $\epsilon$
- $G_E^p$  and  $G_M^p$  determined as slope and intersection from fits

$$G_D = \frac{1}{\left(1 + \frac{Q^2}{0.71 \text{GeV}^2}\right)^2}$$



C. F. Perdrisat, V. Punjabi and M. Vanderhaeghen,  
Prog. Part. Nucl. Phys. 59, 694 (2007)

# Unpolarized $ep$ Elastic Scattering

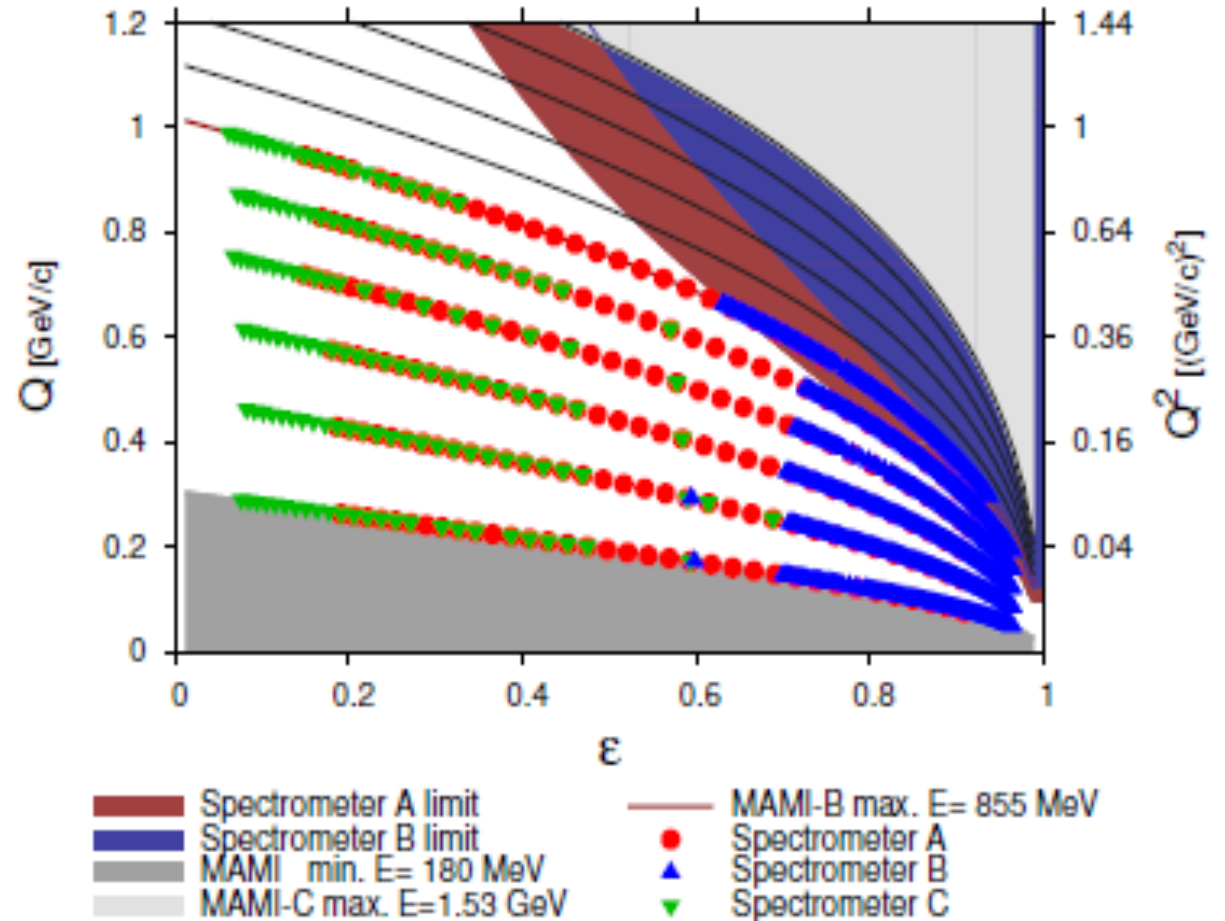
Three spectrometer facility of the A1 collaboration:



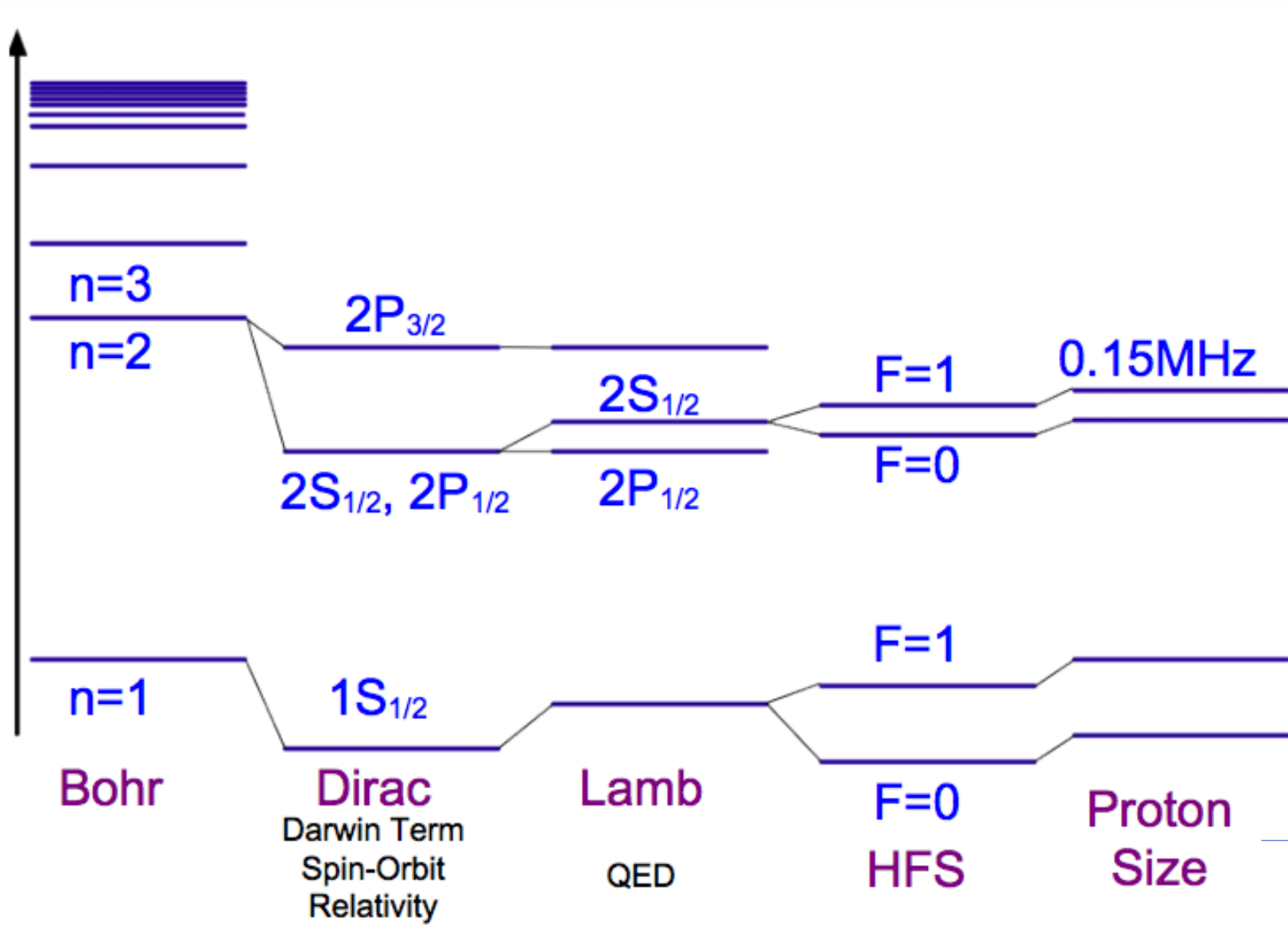
- Large amount of overlapping data sets
- Statistical error  $\leq 0.2\%$
- Luminosity monitoring with spectrometer
- $Q^2 = 0.004 - 1.0 \text{ (GeV/c)}^2$
- result:  $r_p = 0.8791(79) \text{ fm}$

J.C. Bernauer *et al.* PRL. 105 (2010) 242001

Measurements @ Mainz



# Hydrogen Spectroscopy



- Physics origin of the proton finite size effect:

- S-state wavefunction has overlap with the proton

G. Miller PRC 99 035202 (2019)

$$\Delta E = -4\pi\alpha G_E^p(0) |\psi_{n0}(0)|^2 \delta_{l0}$$

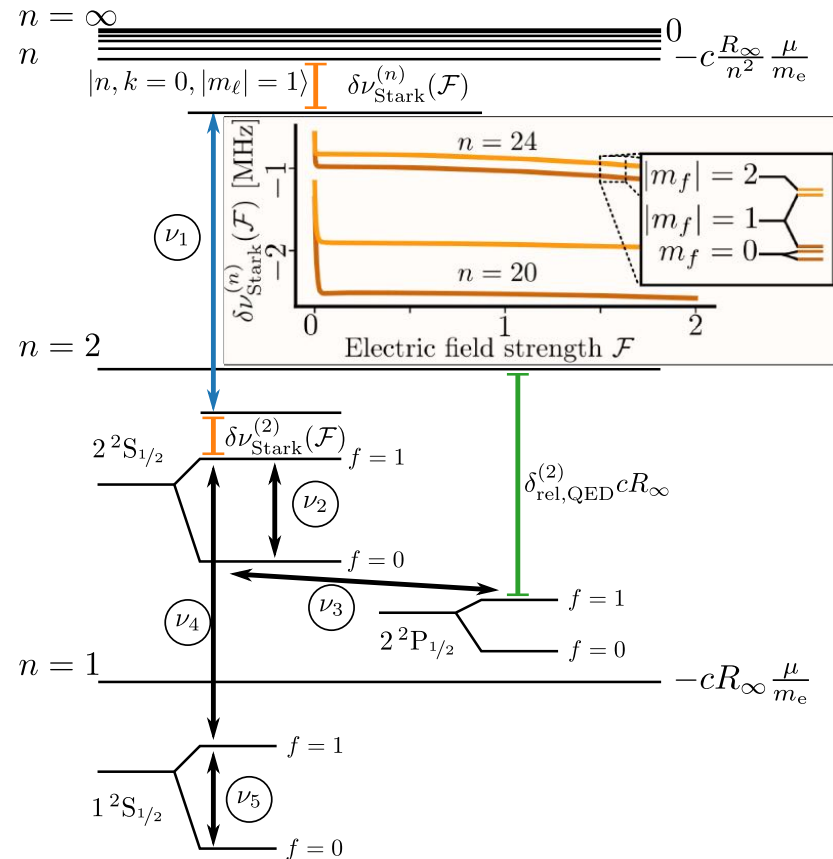
$$= 4\pi\alpha \frac{r_p^2}{6} |\psi_{n0}(0)|^2 \delta_{l0}.$$

$$\langle r^2 \rangle = -6 \frac{dG_E^p(Q^2)}{dQ^2} \Big|_{Q^2=0}$$

# Recent High-n Rydberg State Measurement

$$cR_\infty \left[ \left( \frac{1}{4} - \frac{1}{n^2} \right) \frac{\mu}{m_e} + |\delta_{\text{rel,QED}}^{(2)}| \right]$$

$$= \nu_1 + \nu_2 + \nu_3 + |\delta\nu_{\text{Stark}}^{(n)}(\mathcal{F})| + \delta\nu_{\text{Stark}}^{(2)}(\mathcal{F}),$$



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