

# AB INITIO NUCLEAR DENSITIES FROM LOW-RESOLUTION INTERACTIONS

Pierre Arthuis



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# A tale of two LEES

**From the LEES workshop to sake lees**

Sendai workshop on "Low-Energy Electron Scattering for Nucleon and Exotic Nuclei"

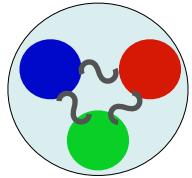


[DryPot - Own work, CC BY-SA 3.0, Wikimedia]

**Or how sometimes it is good to leave time for things to precipitate**

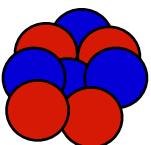


# *Ab initio* many-body scheme



## **Particle physics**

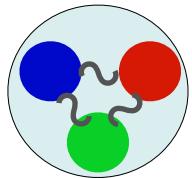
No direct application of  
quantum chromodynamics  
(Lattice QCD only for few nucleons)



## **Nuclear theory**

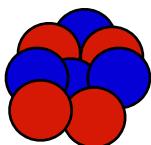


# *Ab initio* many-body scheme



## Particle physics

No direct application of quantum chromodynamics  
(Lattice QCD only for few nucleons)



## Nuclear theory

### Interactions anchored in Effective Field Theory

#### A-body Schrödinger equation

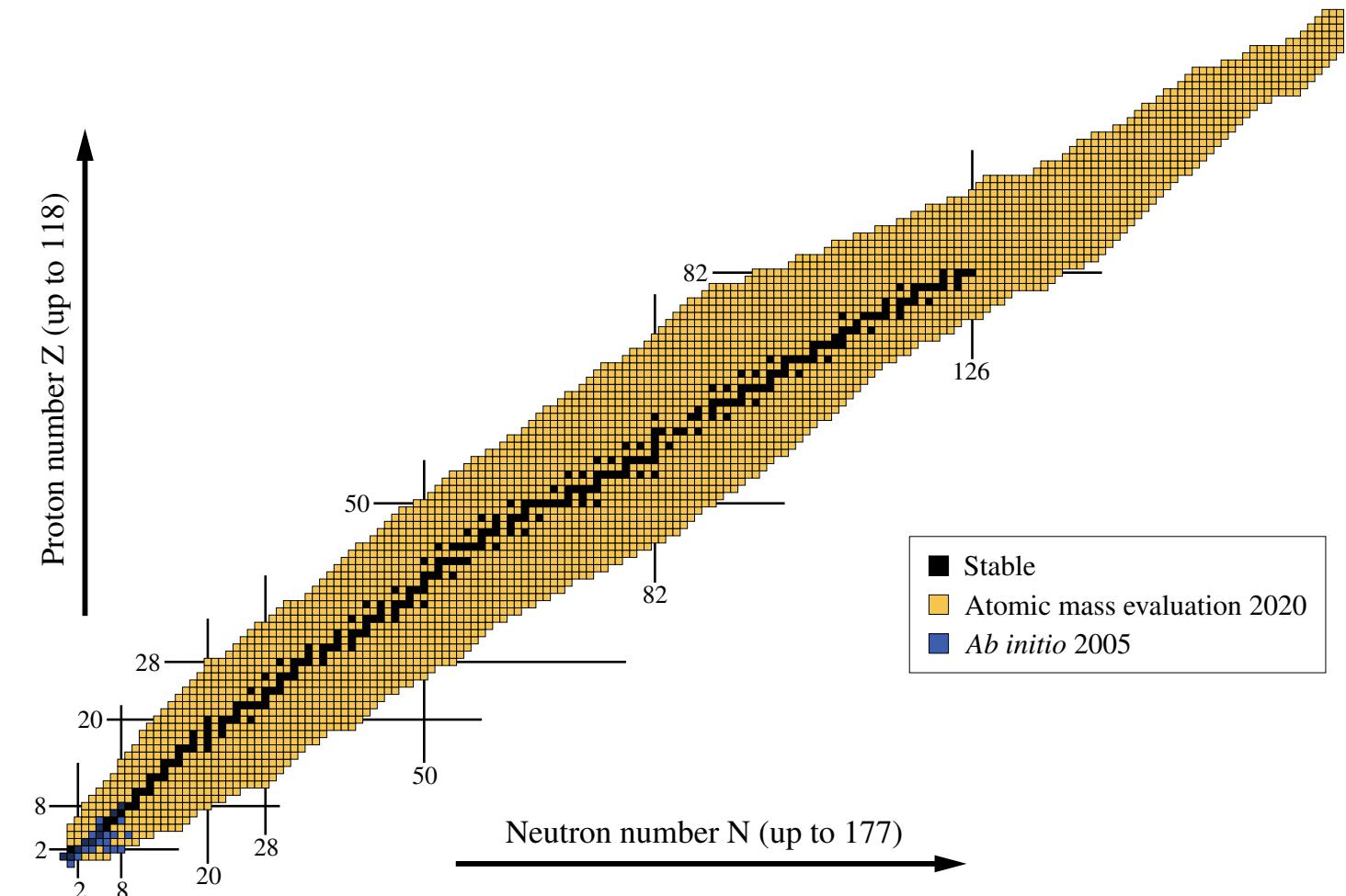
$$H |\Psi^A\rangle = E^A |\Psi^A\rangle$$

#### Obtain a description that is:

- Consistent
- Systematic
- Accurate enough
- From inter-nucleon interactions
- Rooted in quantum chromodynamics



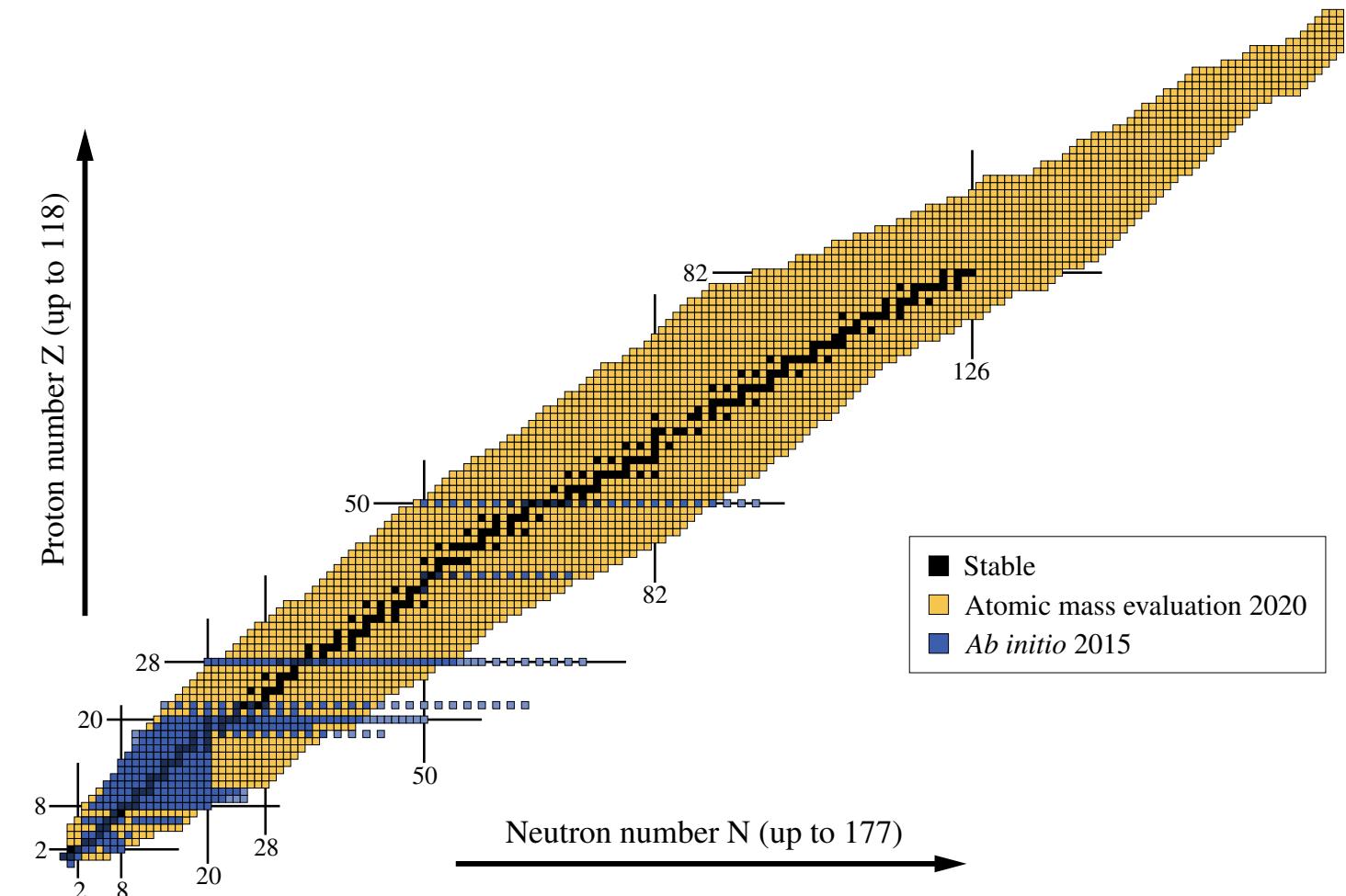
# *Ab initio* many-body methods range



Adapted from B. Bally



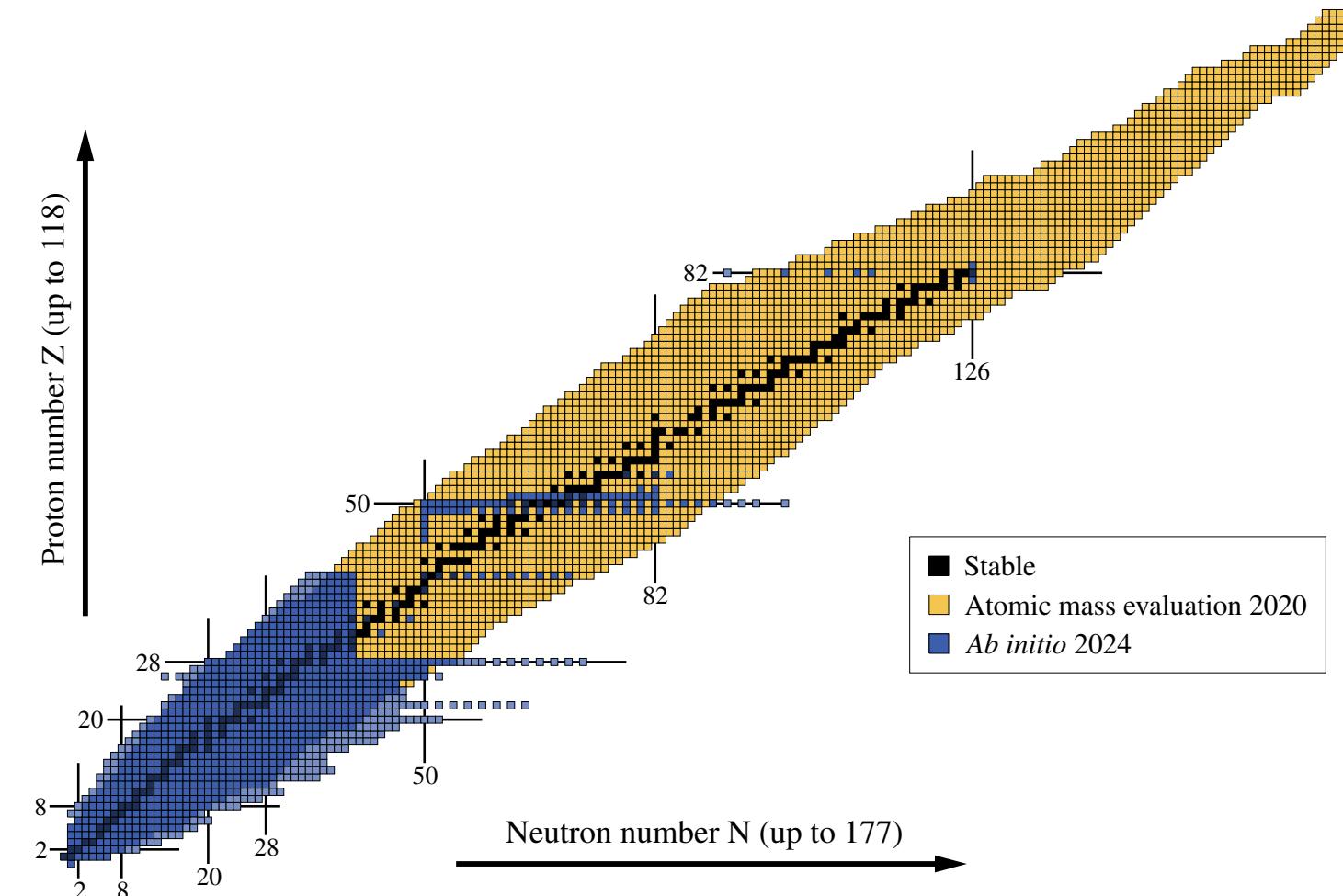
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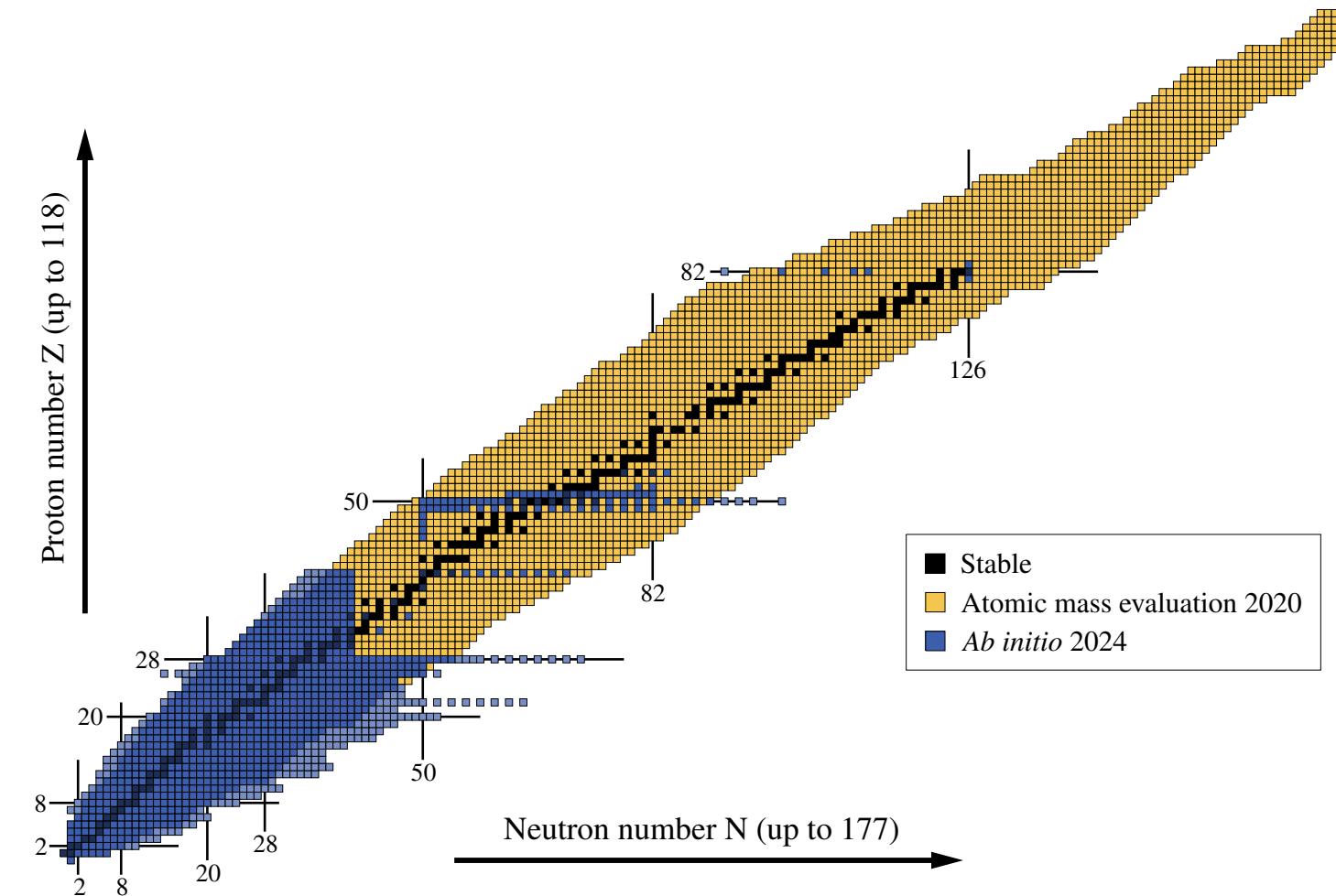
# *Ab initio* many-body methods range



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# *Ab initio* many-body methods range



## Expansion methods

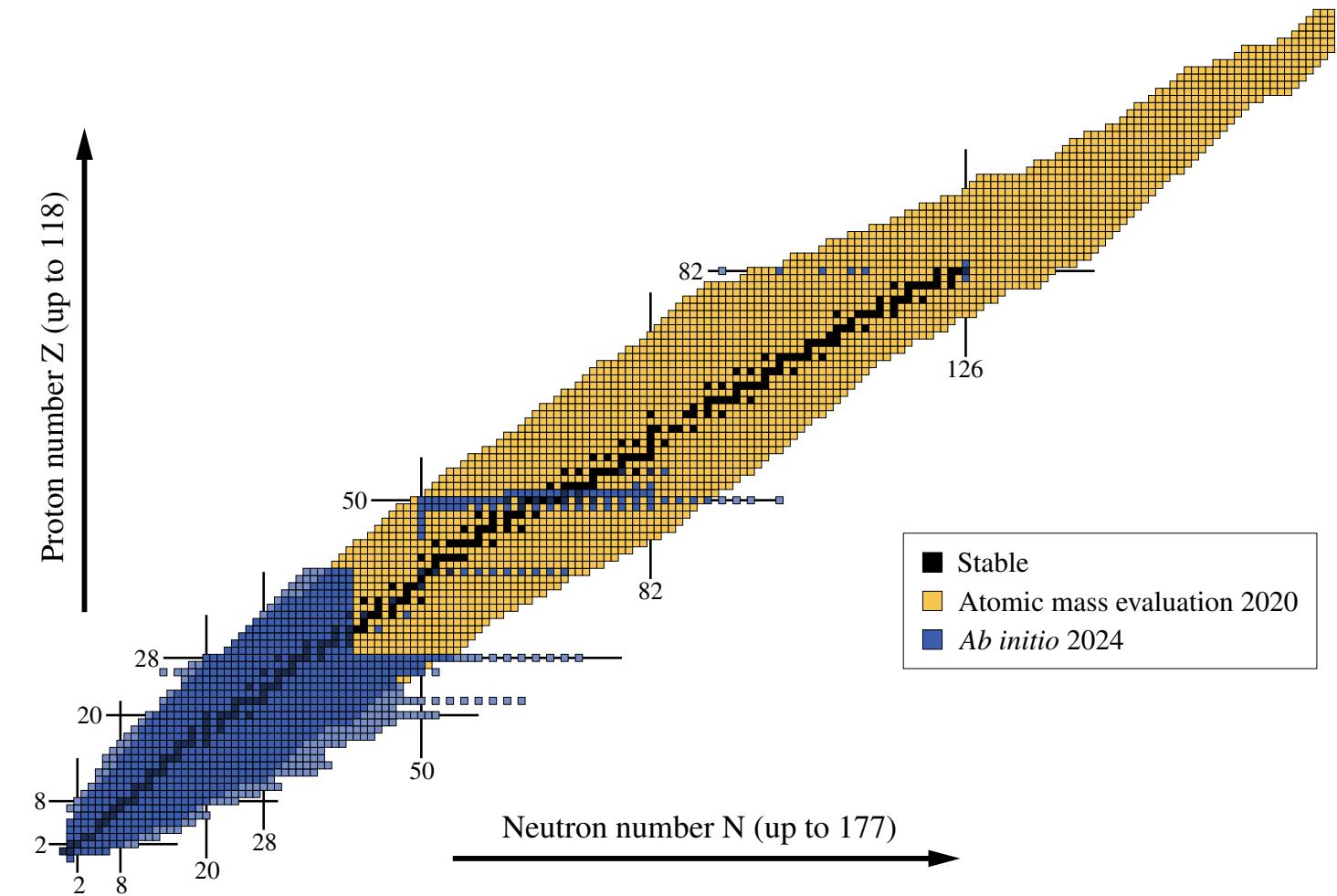
$$\begin{aligned} H|\Psi\rangle &= U(\infty)|\Phi\rangle \\ &= (U_1 + U_2 + U_3 + \dots)|\Phi\rangle \end{aligned}$$

- Expand the correlations order by order
- Truncate at desired order
- Estimate uncertainties

**Controlled expansion & uncertainty**  
**Moderate cost**



# A look at experimental facilities



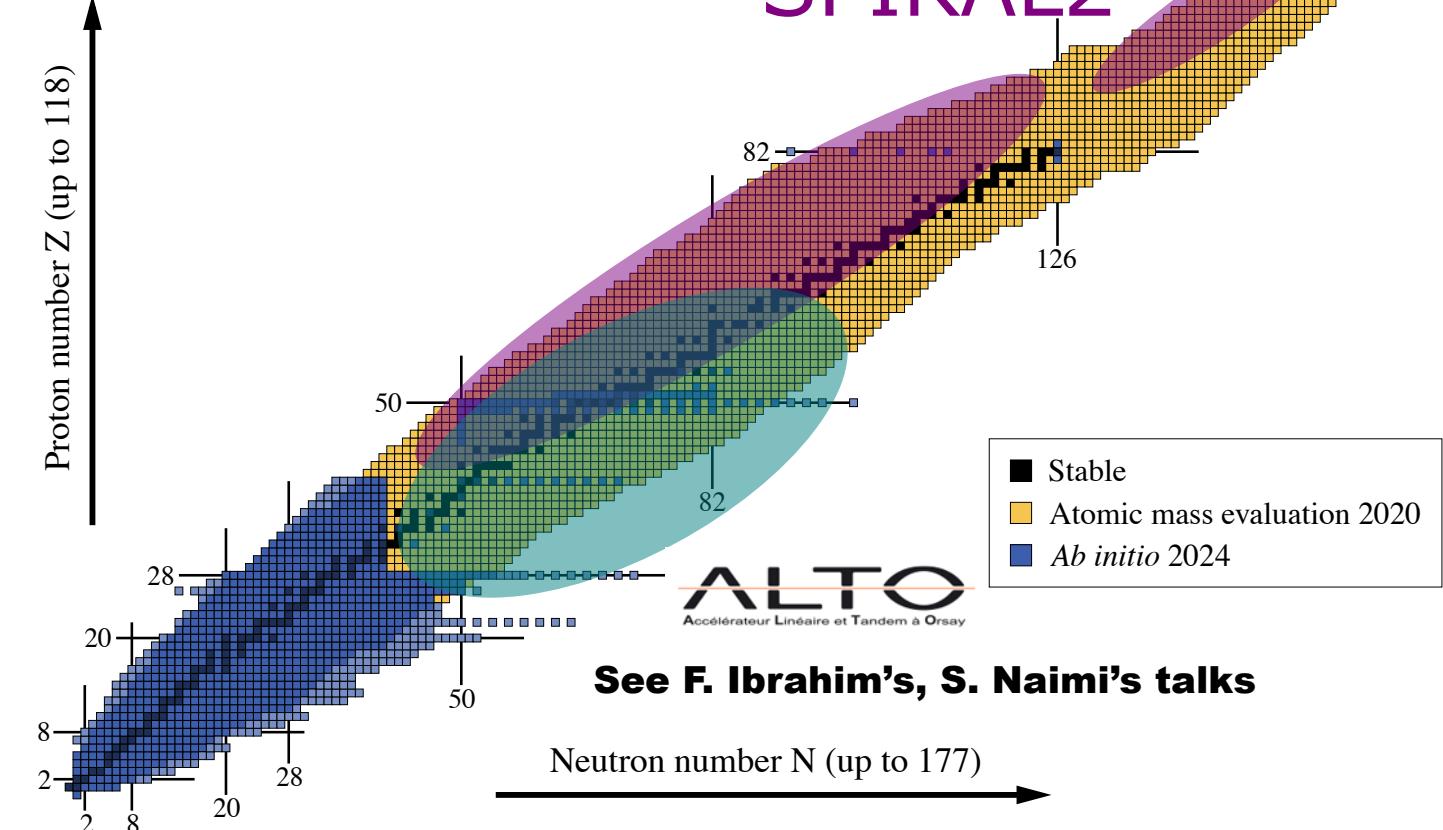
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# A look at experimental facilities

See V. Lapoux' talk

**GANIL**  
**SPIRAL2**



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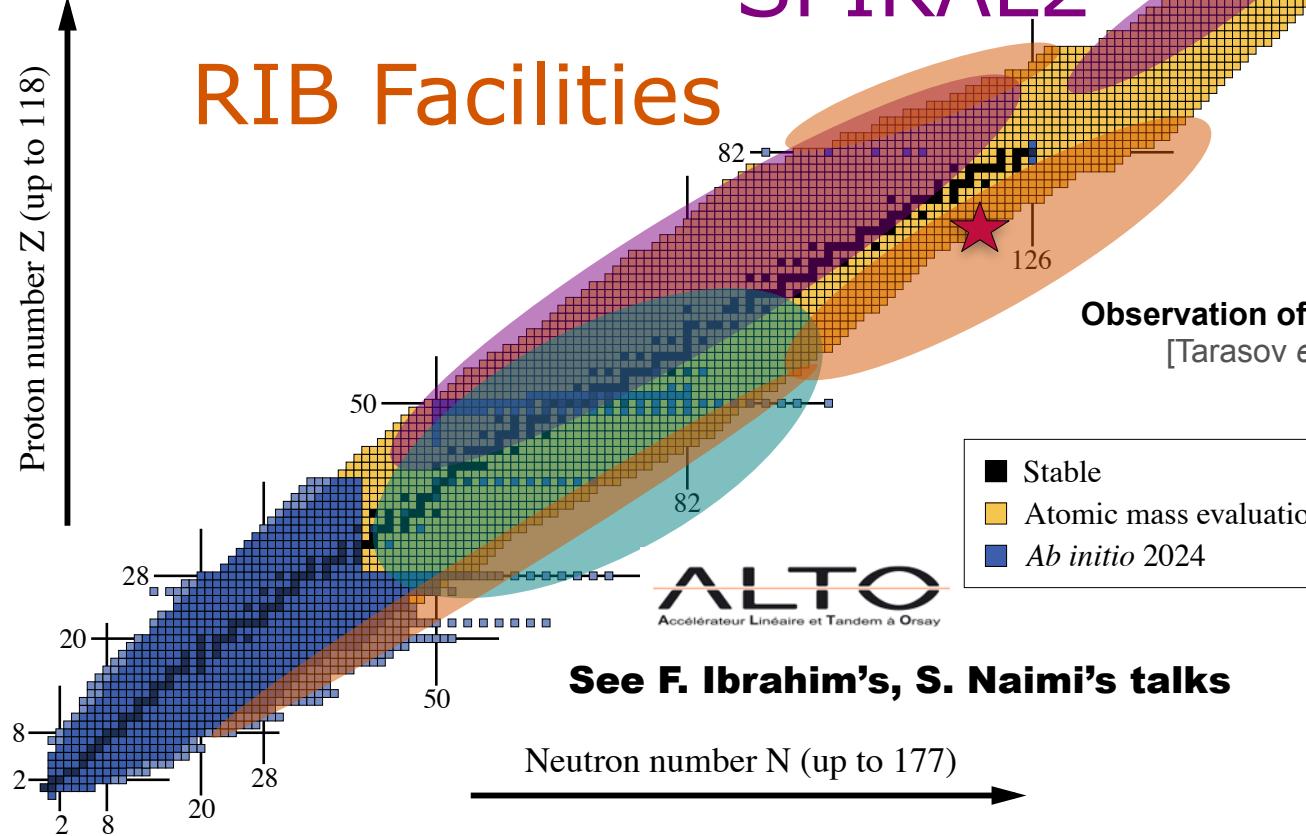


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RIB Facilities



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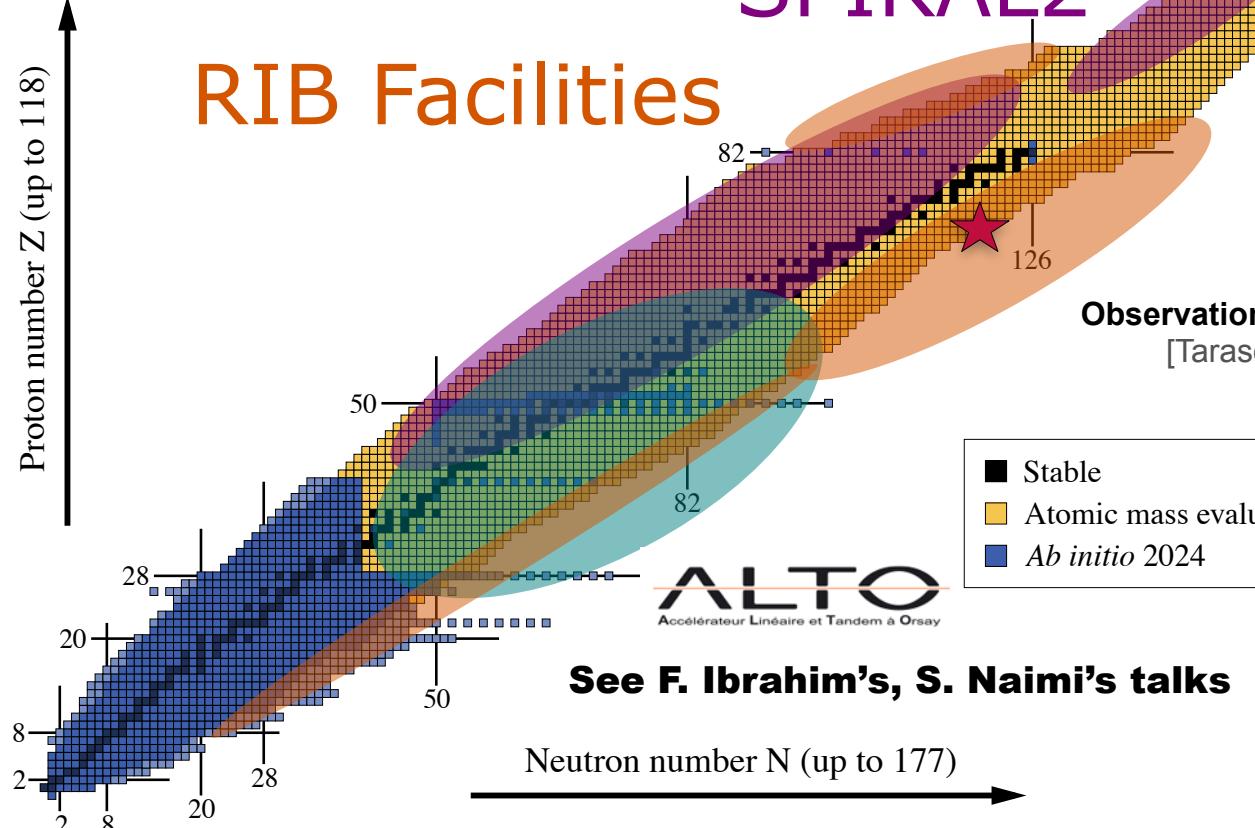


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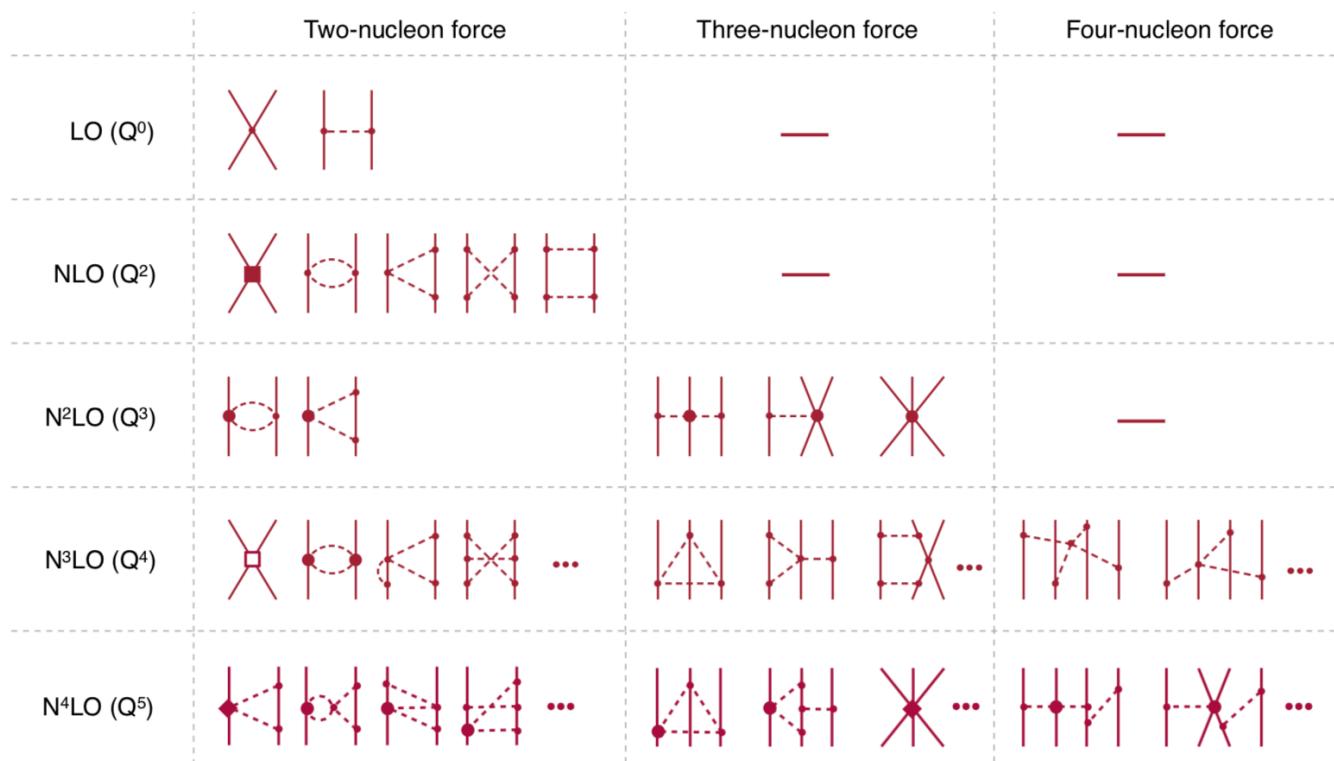


# A look at chiral interactions

## Rationale

- Nucleons and pions as degrees of freedom
- Link to QCD through Hamiltonian symmetries
- Natural hierarchy of terms
- Systematically improvable

$$M_{\text{low}} \sim m_\pi \quad M_{\text{high}} \sim \Lambda_\chi \quad \Lambda = \{\Lambda_{\text{NN}}, \Lambda_{3\text{N}}, \dots\}$$



[Epelbaum, PoS CD15 (2016)]

**See G. King's, Y. Maeda's talks**



# A look at chiral interactions

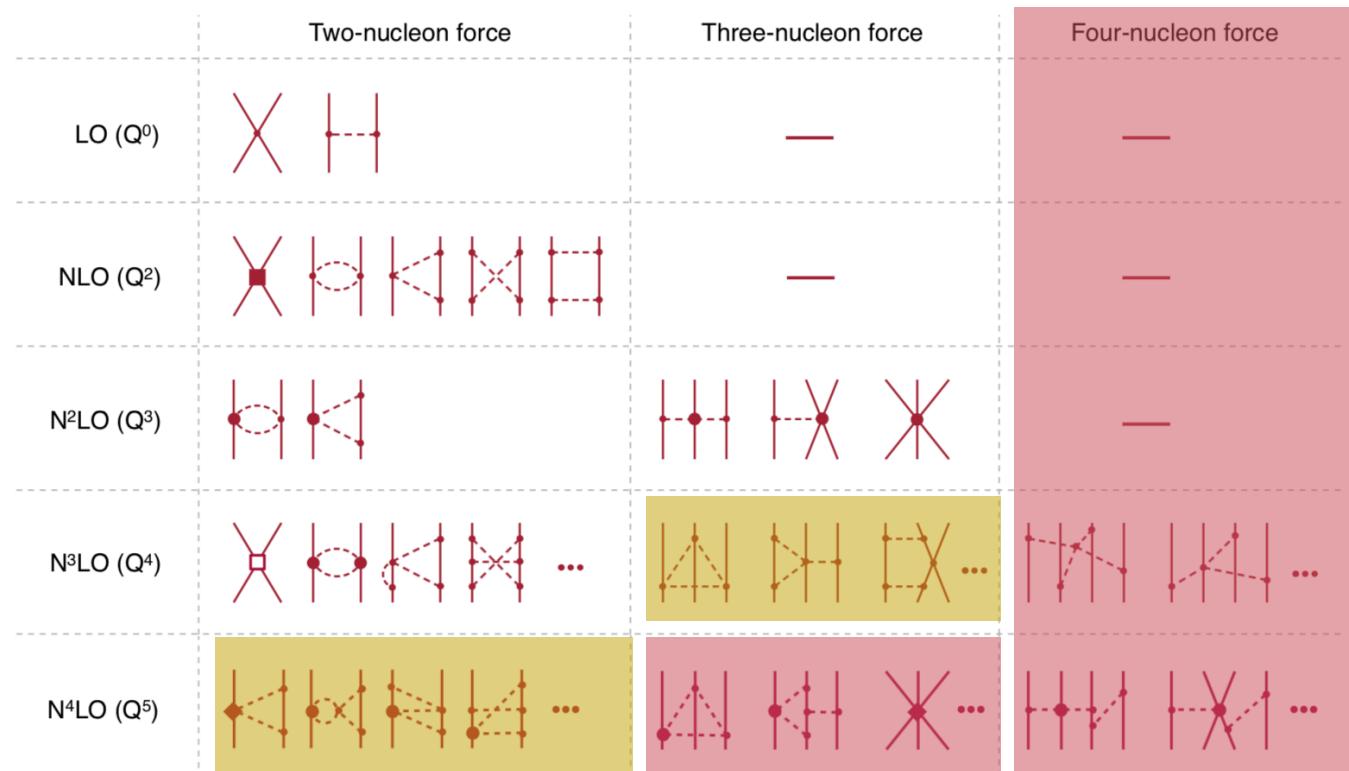
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## In practice

- NN terms up to  $\text{N}^4\text{LO}$  (though mostly  $\text{N}^3/\text{N}^2$ )
- 3N terms up to  $\text{N}^3\text{LO}$  (though mostly  $\text{N}^2\text{LO}$ )



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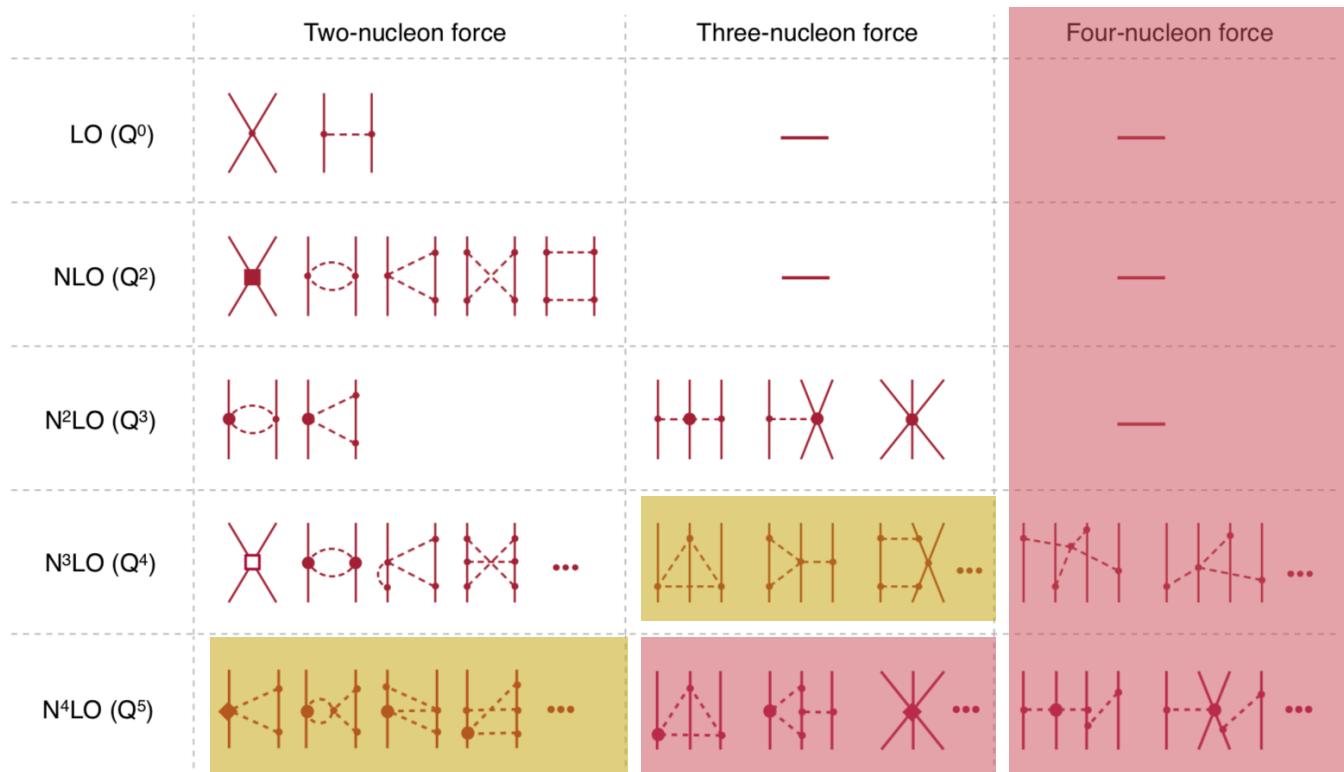
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**Footnote: Similar expansion with  $\Delta$  excitation**

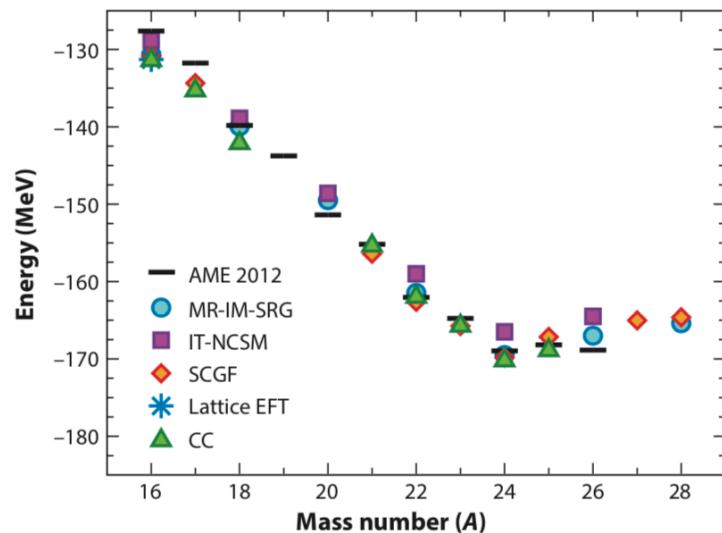
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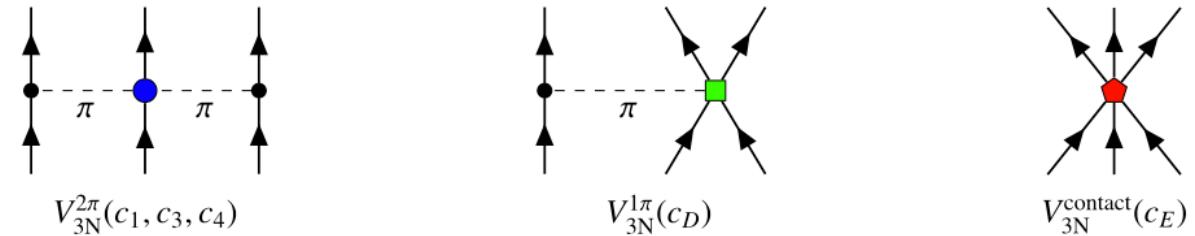
# The leading three-body force

## N2LO contributions

- Two-pion exchange: LECs set in the NN sector
- Two new LECs: one-pion exchange and contact term
- $c_D, c_E$  only new parameters in 3N sector



[Hebeler et al., Annu. Rev. Nucl. Part. Sci. 65 (2015)]



[Hebeler, Phys. Rept. 890 (2021)]

## Practical aspects

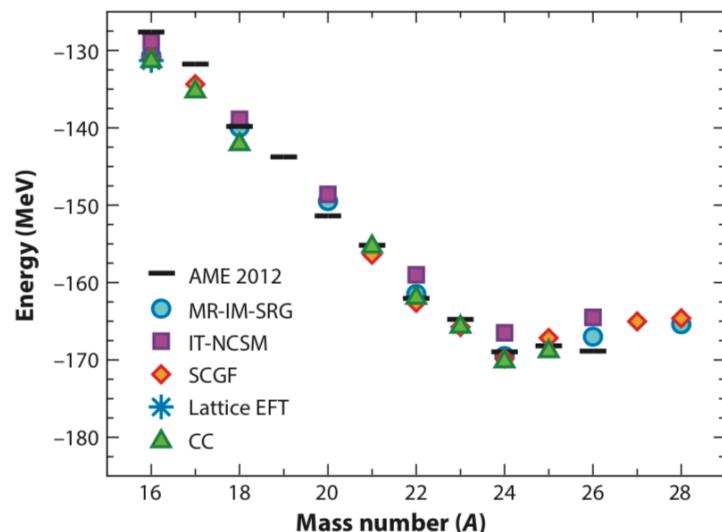
- Most often fitted in the 3N sector
- Bring repulsion necessary for a good qualitative description



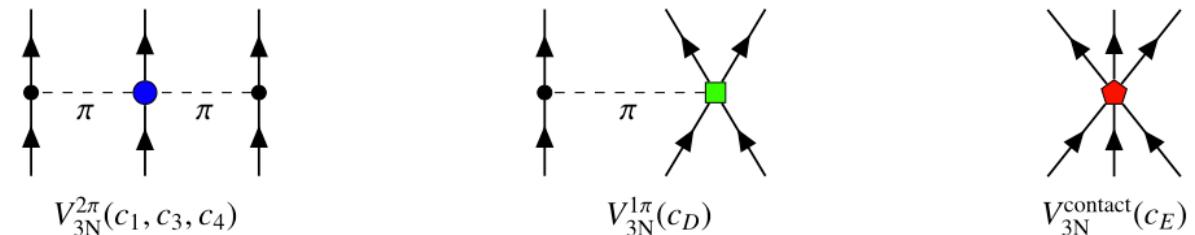
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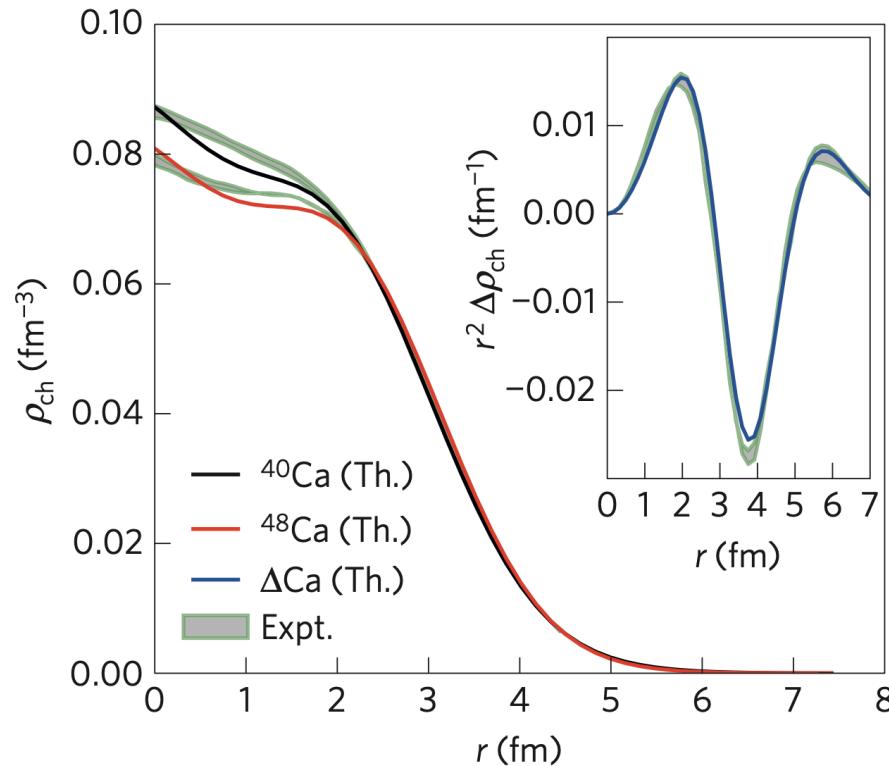
## Practical aspects

- Most often fitted in the 3N sector
- Bring repulsion necessary for a good qualitative description

**A good reproduction of all nuclear properties is hard**

## Charge densities of $^{40}\text{Ca}$ and $^{48}\text{Ca}$

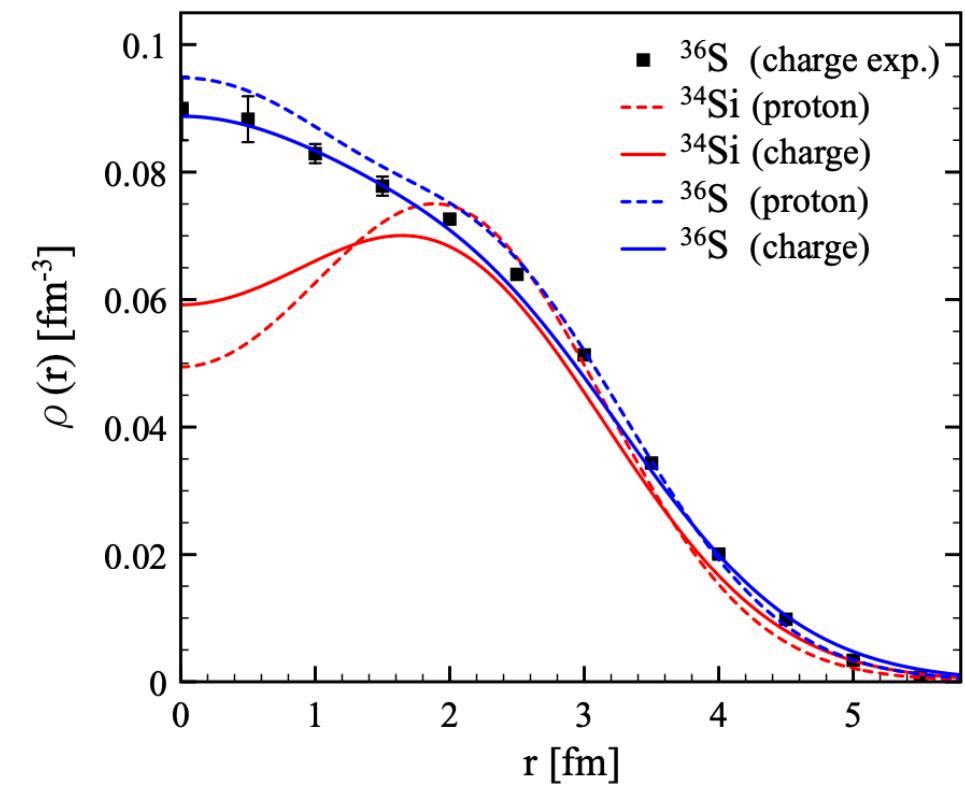
- First established NNLOsat as accurate interaction for  $\rho$
- Connection to weak charge radius,  $R_{\text{skin}}$  and  $\alpha_D$



[Hagen *et al.*, *Nat. Phys.* **12** (2015)]

## Study of candidate bubble nucleus $^{34}\text{Si}$

- Investigation of the central depletion in  $^{34}\text{Si}$
- Link to details of the interaction and s.p. structure

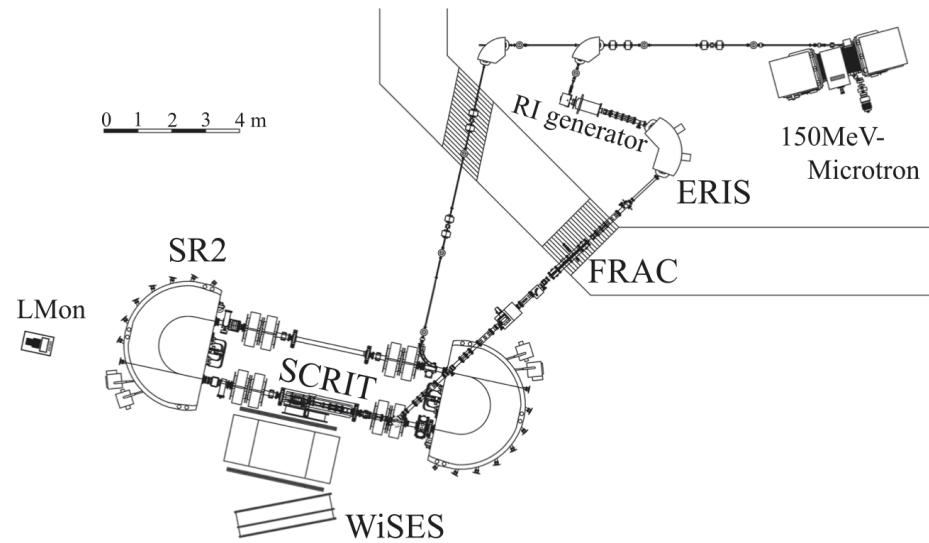


[Duguet *et al.*, *PRC* **95** (2017)]



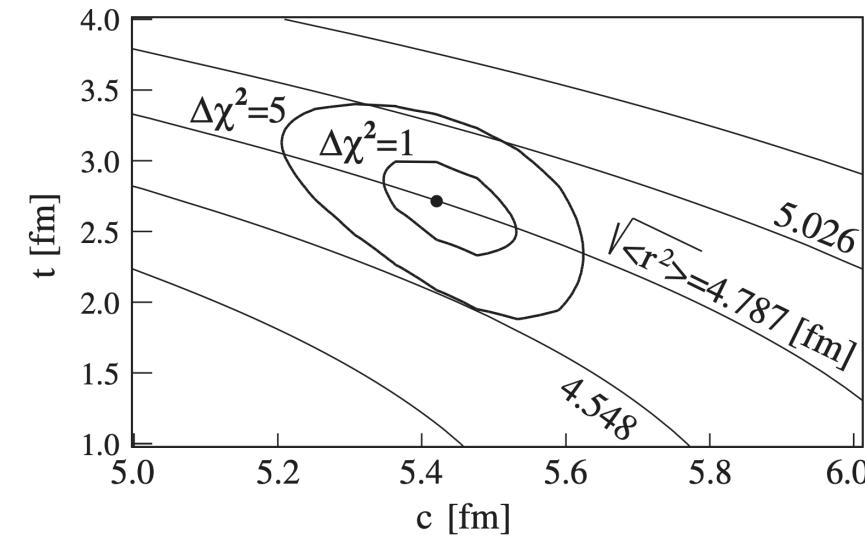
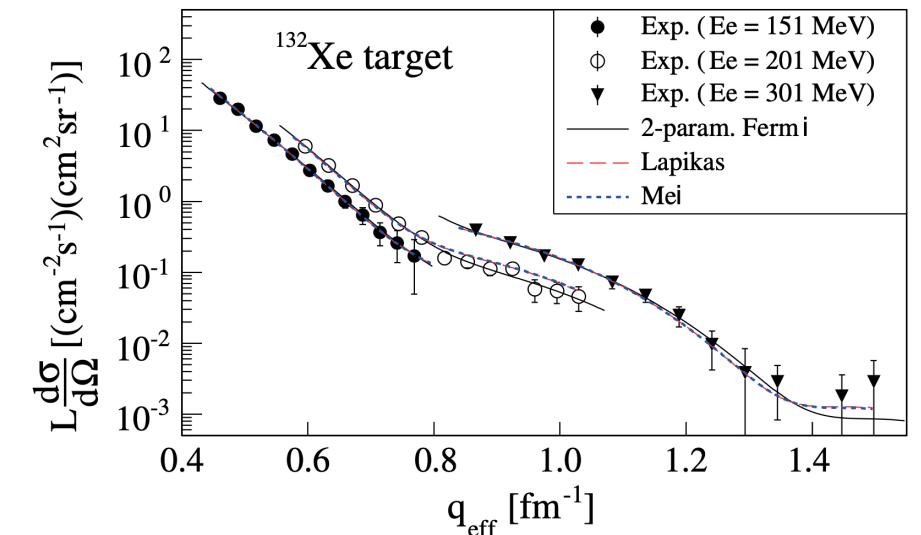
# 2017: First SCRIT results

[Tsukada, Enokizono, Ohnishi, et al., PRL 118 (2017)]



## Scattering off $^{132}\text{Xe}$

- Strong motivation to try and push our reach towards higher masses
- Radius and two-point Fermi extracted from the experiment

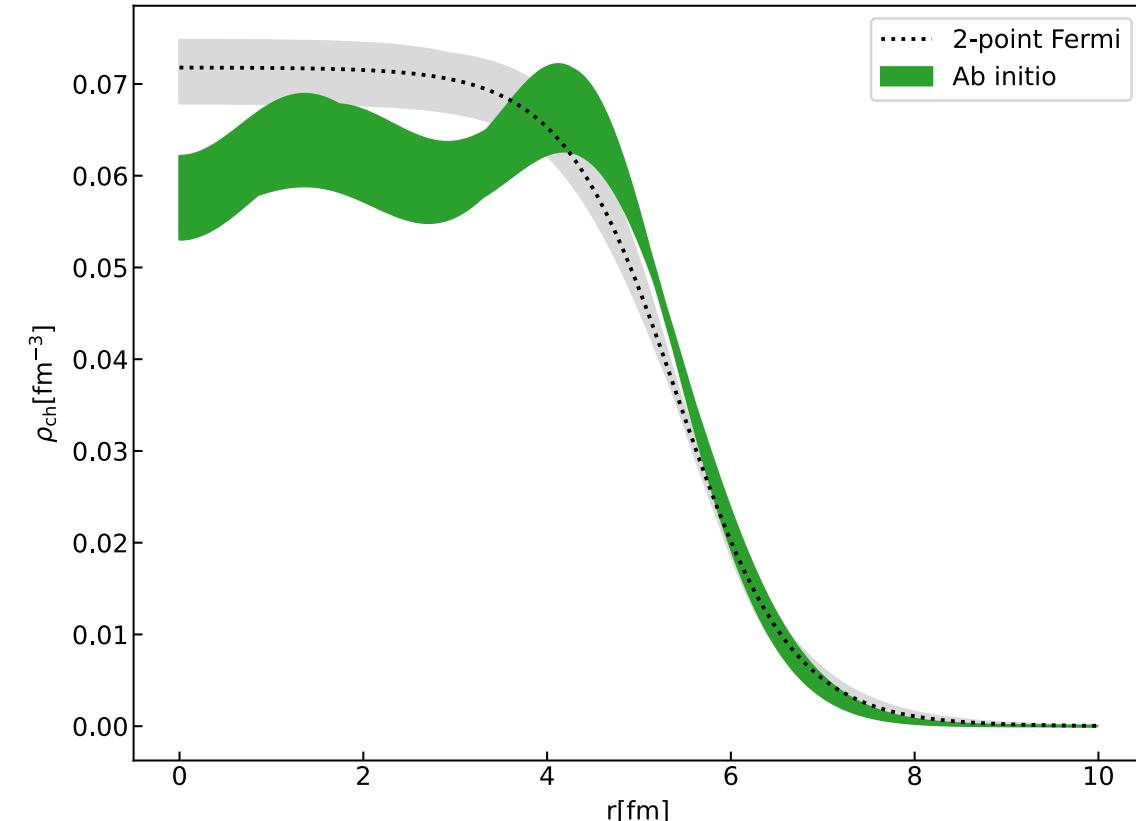


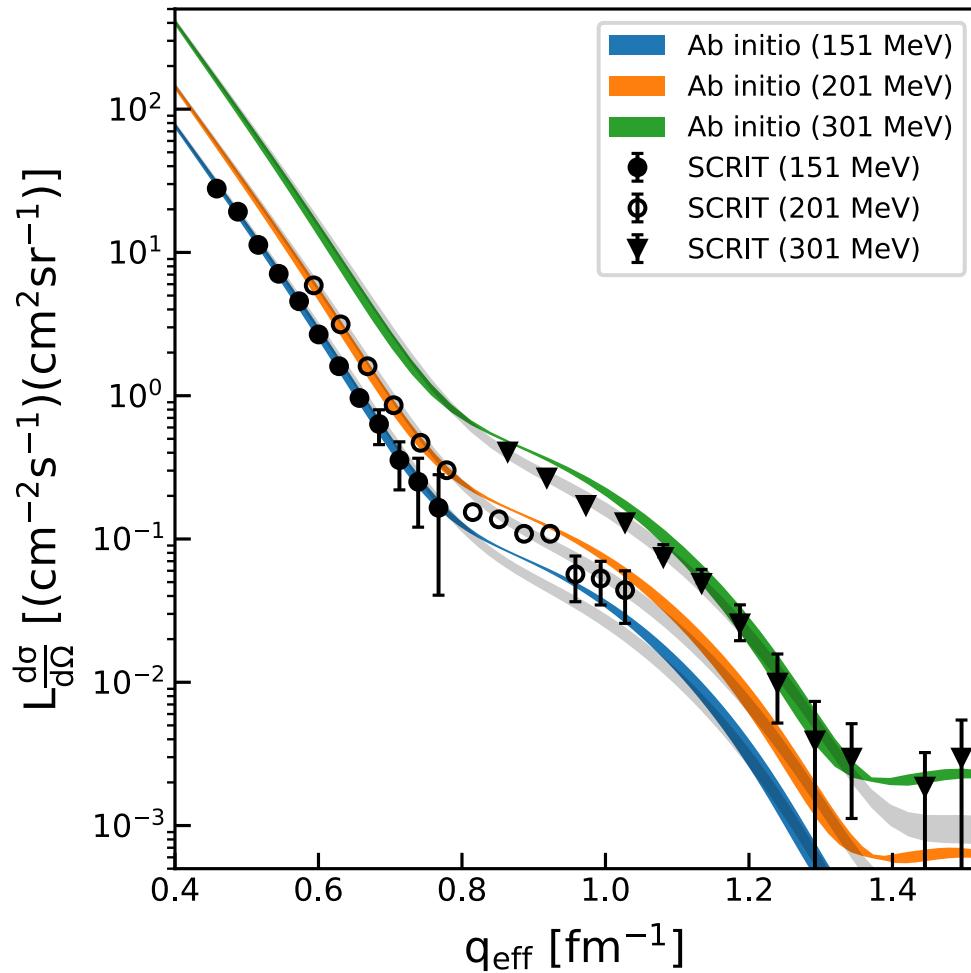
## $^{132}\text{Xe}$ charge density distribution with NNLOsat

- Radius compatible with experiment:  $4.824 \pm 0.124$  fm  
[Tsukada *et al.*, PRL 118 (2017)]:  $4.79_{-0.10}^{+0.12}$  fm
- NN+3N(lnl) severely underpredicts:  $4.070 \pm 0.045$  fm
- 2-point Fermi distribution insufficient to describe expected behaviour

### Uncertainty band

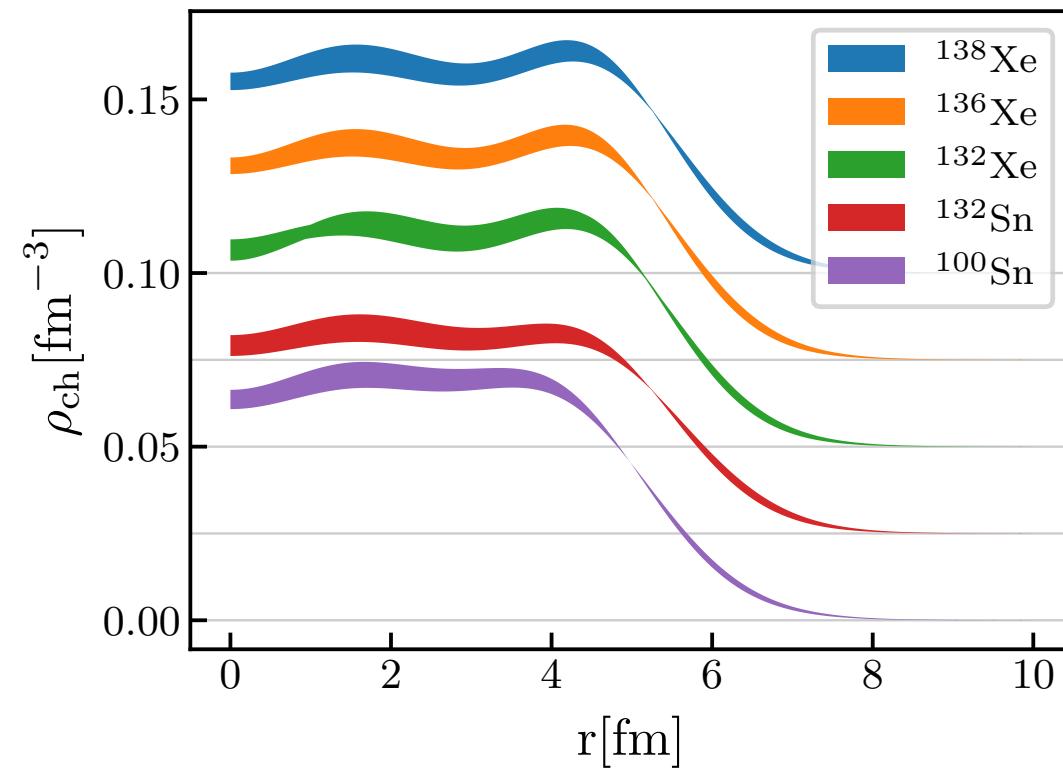
- Mainly model-space convergence uncertainty (truncated 3NF)
- Many-body method basically converged
- Not included: Chiral EFT uncertainty





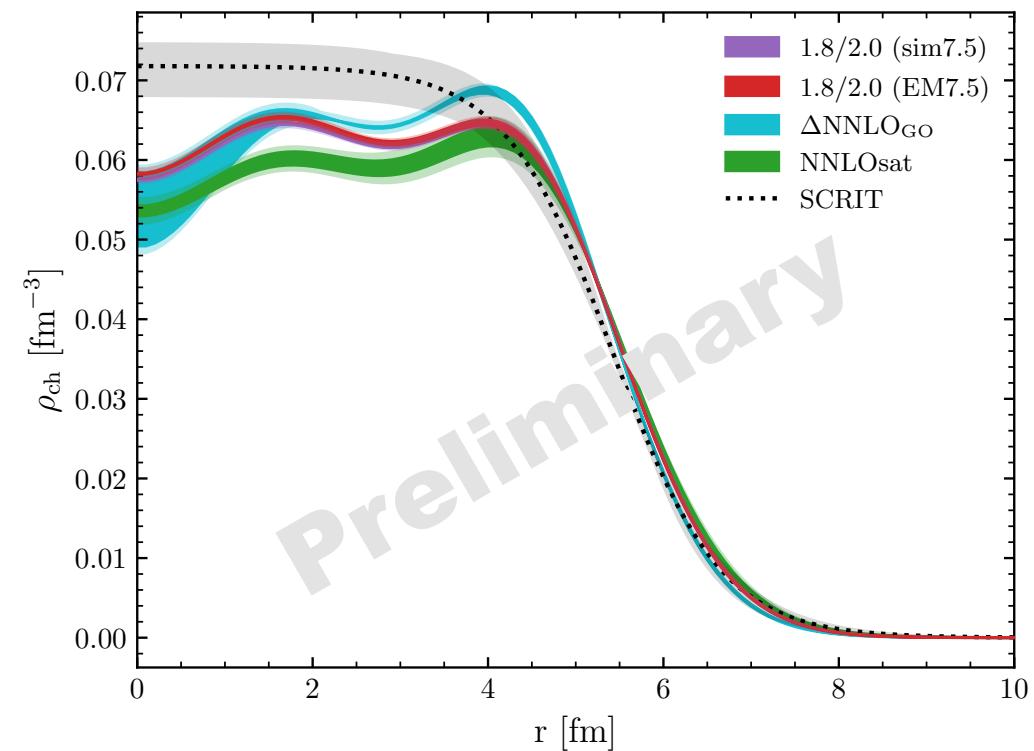
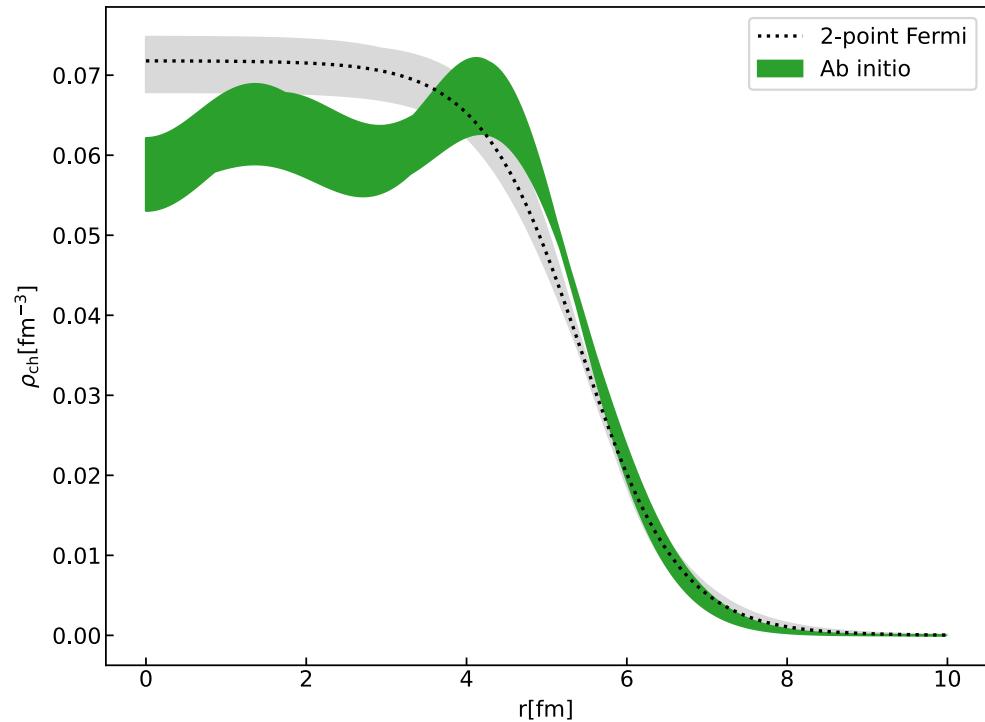
## First *ab initio* calculation past the Sn isotopic line

- Reproduce experimental electron scattering results
- Results meaningful for exp. despite moderate convergence



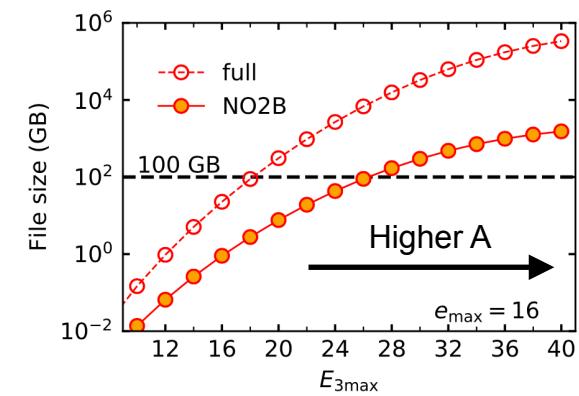


# Progress in numerical methods



## Reduced uncertainties

- Better storage method for the 3NF [Miyagi *et al.*, *PRC* **105** (2022)]
- Truncation on 3NF ME partially lifted
- New Xe densities provided to SCRIT group





# Why new low-resolution interactions?

## Need for good reproduction of radii and densities

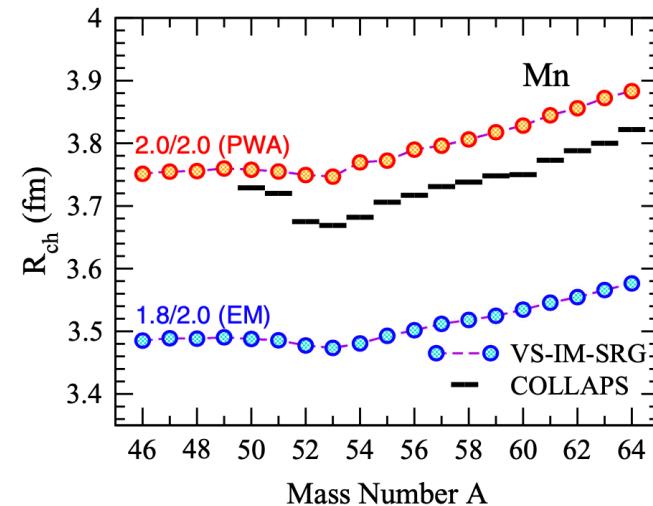
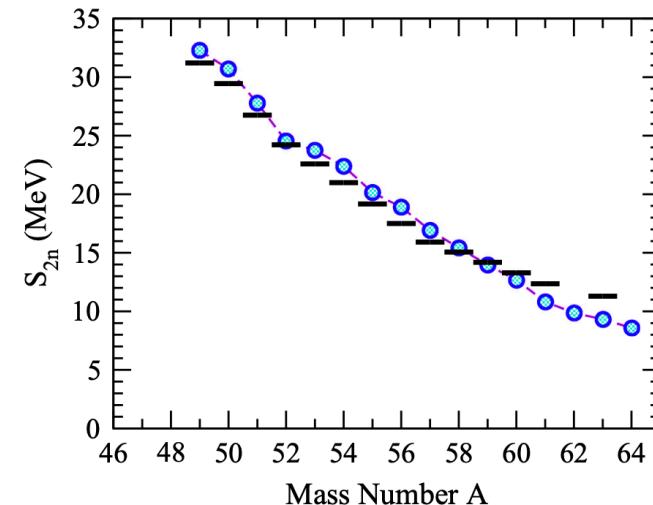
- NNLOsat very successful with radii
- But underbinds and too hard for heavy nuclei
- Other interactions that scale well underbind radii

## Sufficient to describe bulk properties of nuclei

- Better convergence properties through softened interaction
- Proved successful for binding energies with the 1.8/2.0 (EM)  
[Hebeler *et al.*, PRC 83 (2011)]

## The 1.8/2.0 approach

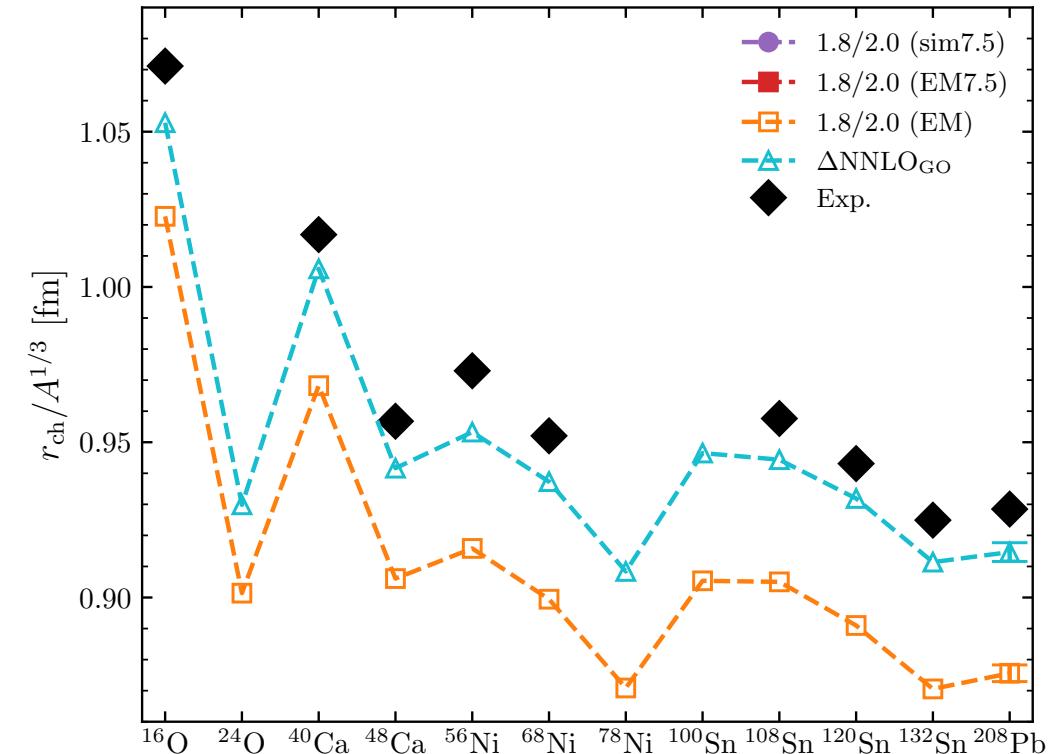
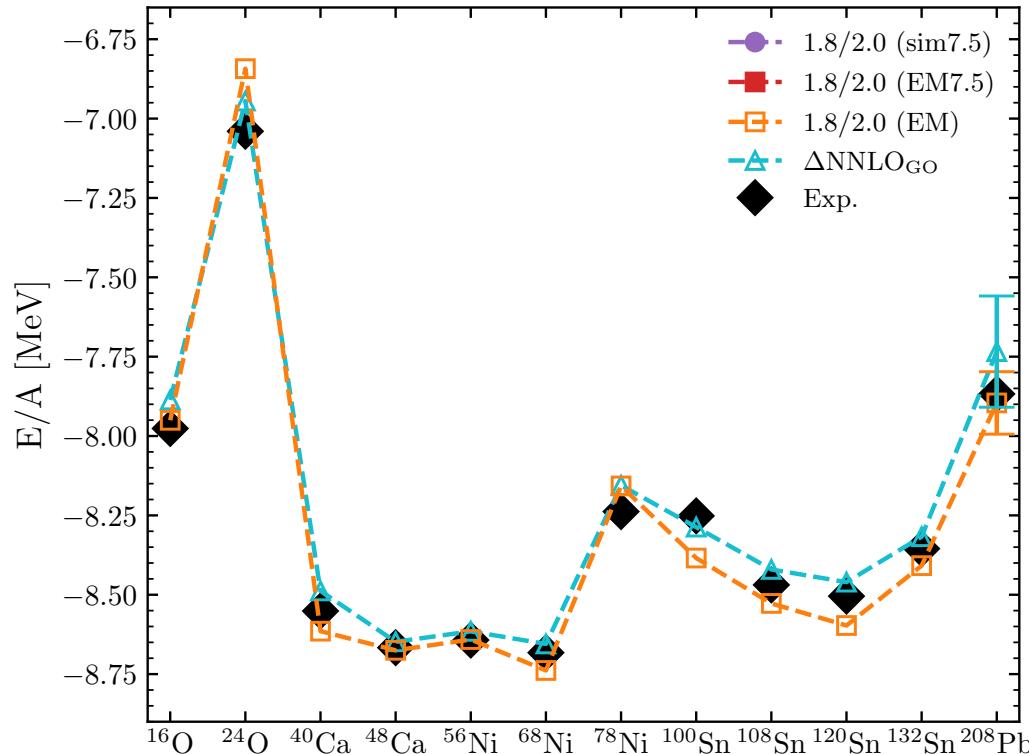
- NN force SRG-evolved to  $1.8 \text{ fm}^{-1}$
- 3N force with  $c_D, c_E$  refitted with a cutoff of  $2.0 \text{ fm}^{-1}$

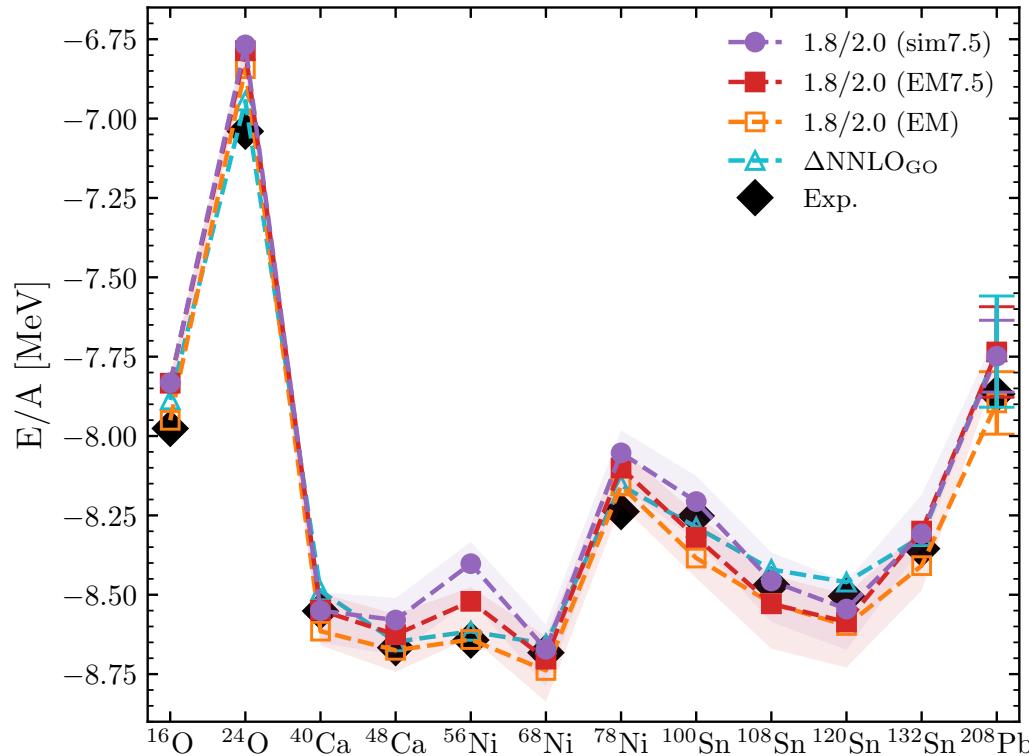


[Simonis *et al.*, PRC 96 (2017)]

# Ground-state accuracy towards heavy systems

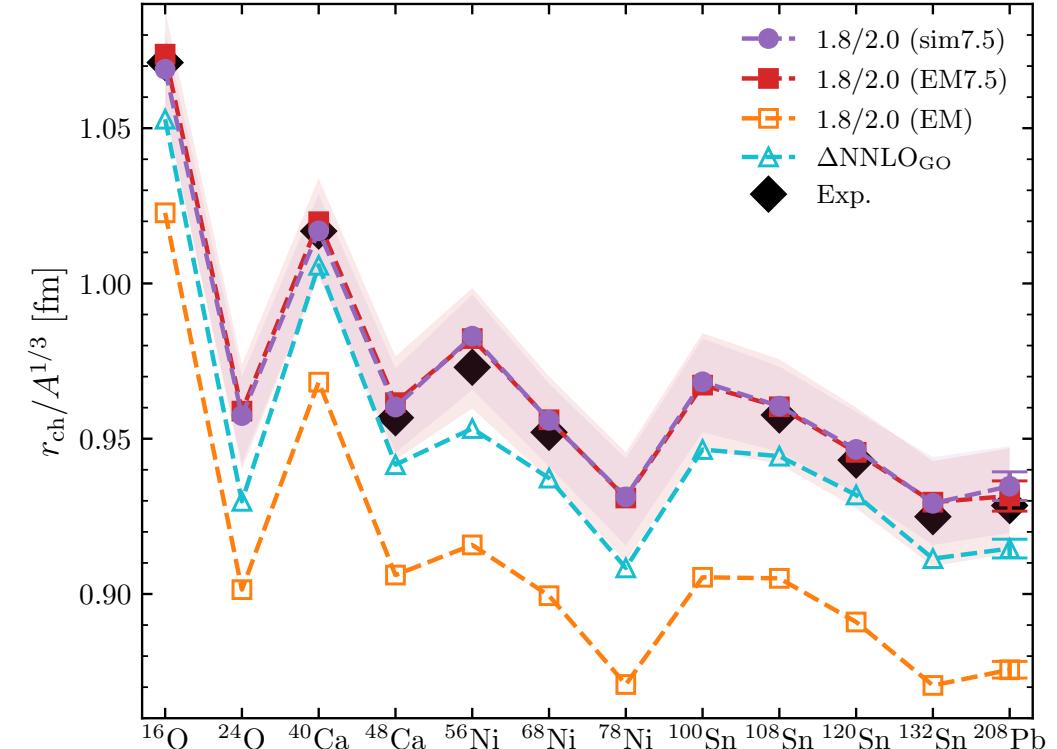
[Arthuis, Hebeler, Schwenk, arxiv:2401.06675]





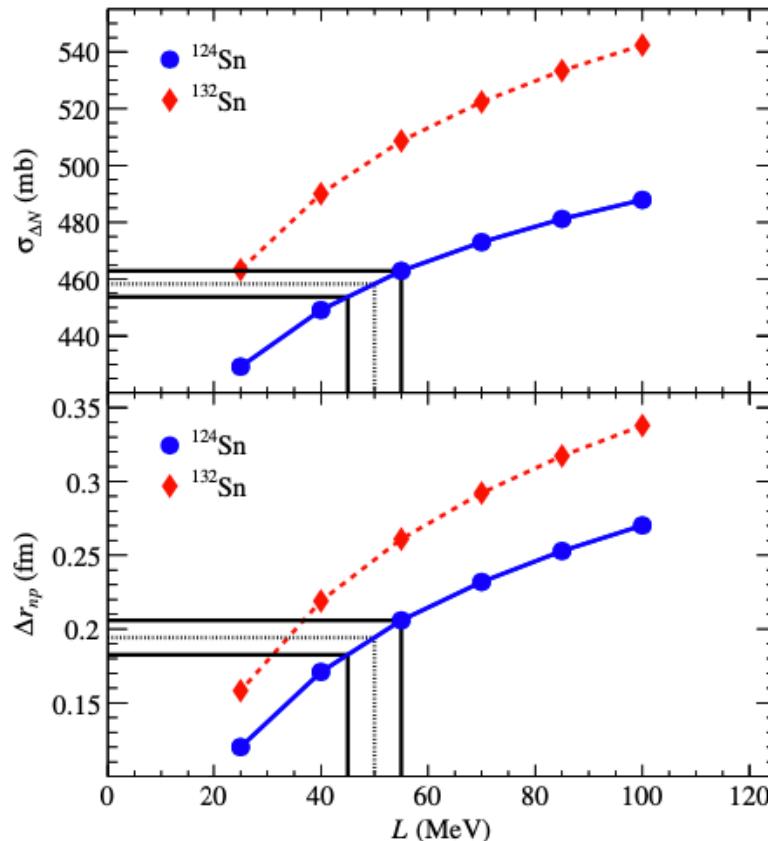
## Binding energy

- Reasonable reproduction of experimental values
- Slight improvement for heavy systems w.r.t. 1.8/2.0 (EM)



## Charge radius

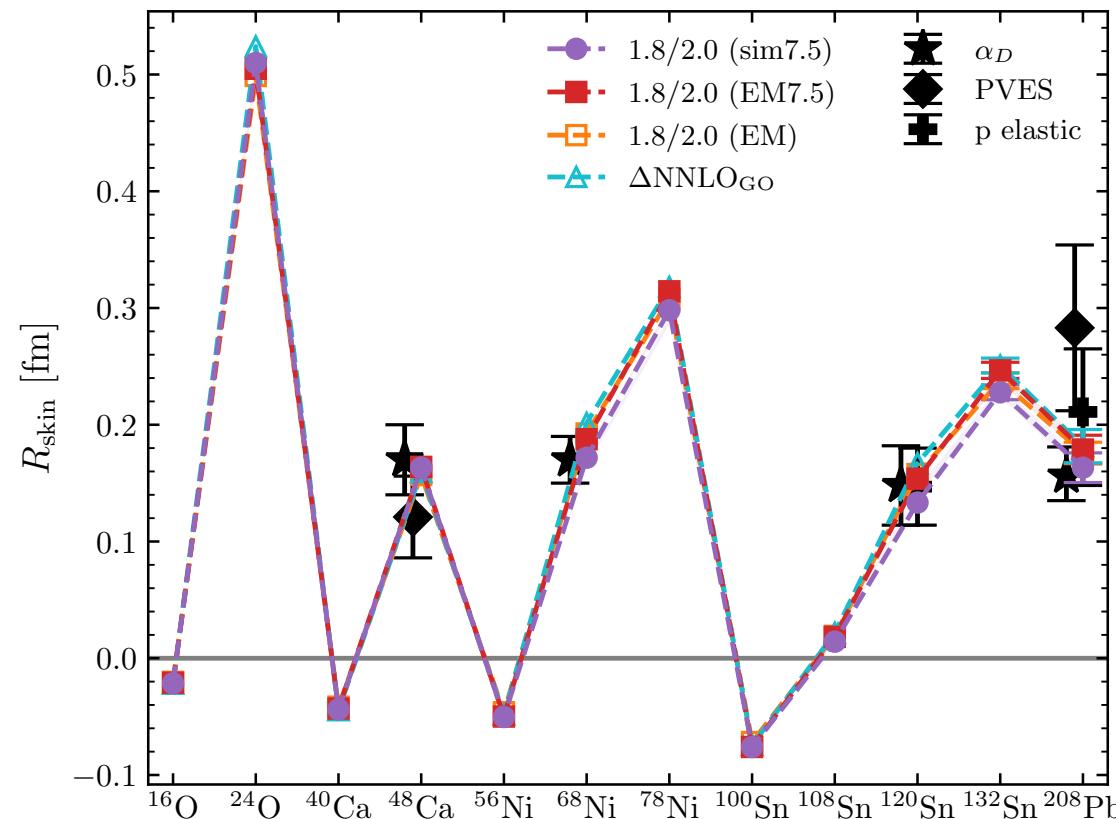
- Quasi-exact reproduction over complete mass range
- Excellent combined reproduction of charge and mass



[Aumann et al., PRL 119 (2017)]

## Neutron removal off Sn isotopes @ R3B/GSI

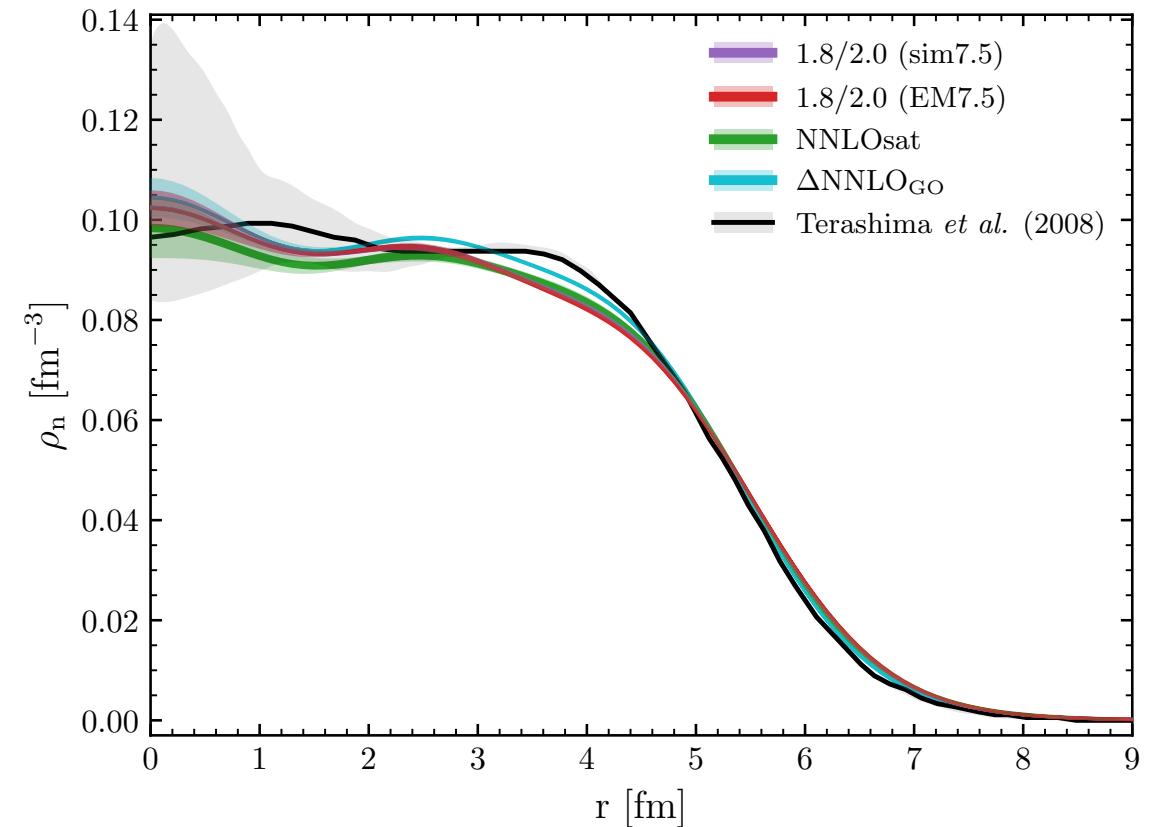
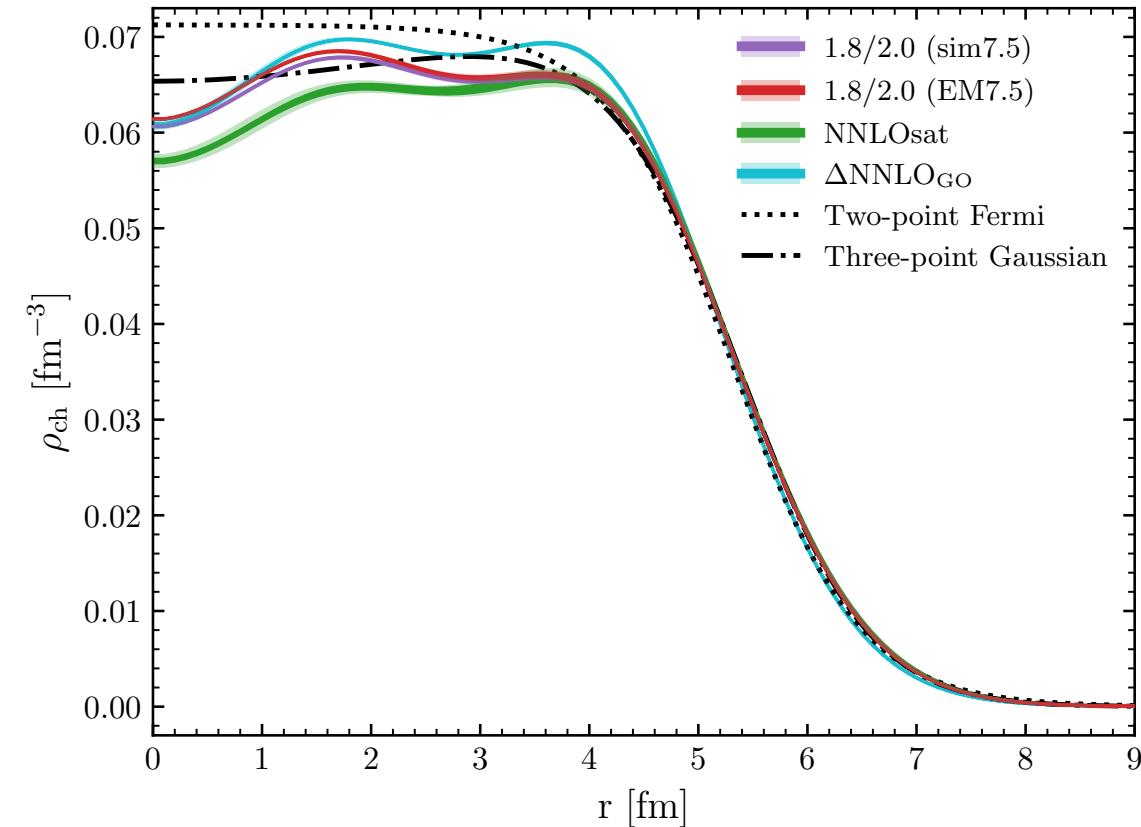
- Access  $L$  through the cross-section, need for theory input
- $L$  correlated to neutron skin too: Great test case





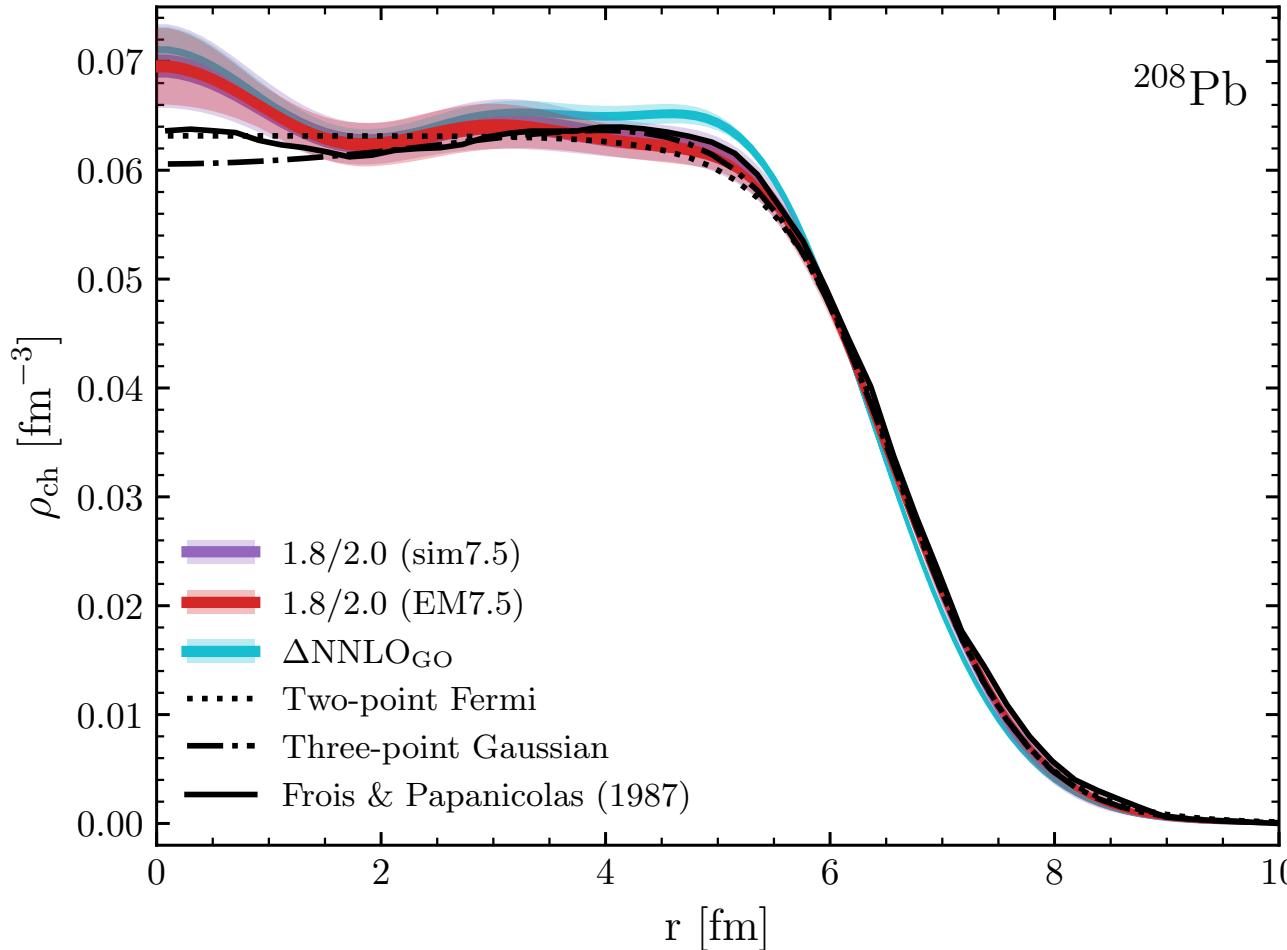
# Ab initio densities for heavy systems: $^{120}\text{Sn}$

[Arthuis, Hebeler, Schwenk, arxiv:2401.06675]



## Excellent reproduction of $^{120}\text{Sn}$ densities

- Consistent picture over the different interactions
- Very moderate uncertainties



### Charge density for $^{208}\text{Pb}$

- Consistent picture over the different interactions
- 1.8/2.0s give excellent surface profile
- Inner density not fully converged yet

New interactions consistent over the nuclear chart



## Conclusion and outlook

### **Ab initio methods now mature**

- Reach up to the Pb isotopic chain
- Systematically improvable many-body method and interaction
- Diversity of nuclear properties reproduced

### **Ab initio radii and densities**

- Novel interactions with good convergence properties
- Consistent results over the whole nuclear chart
- Meaningful input for experimental collaborations (SCRIT, R3B, ...)

### **Future plans**

- Investigation of Ar isotopes: experiment-theory back-and-forth
- Densities as meaningful checks for interaction developments
- Looking forward to new experimental results

**See V. Lapoux' talk**



# Acknowledgments



Funded by  
the European Union



## Thank you for your attention!



**V. Lapoux**  
**V. Somà**



UNIVERSITÀ  
DEGLI STUDI  
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DARMSTADT

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**K. Hebeler**  
**A. Schwenk**



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