

---

# Spectral function of the $\eta'$ meson in nuclear medium

---



Shuntaro SAKAI<sup>(a)</sup>, Daisuke JIDO<sup>(B)</sup>

<sup>(a)</sup>Research Center for Nuclear Physics, Osaka University

<sup>(b)</sup>Department of Physics, Tokyo Institute of Technology

Reference: S. Sakai, DJ, in preparation

ELPH 研究会 「ハドロン分光に迫る反応と構造の物理」

2022.12.6-7

---

# Contents

---

- introduction
- preliminaries
  - spectral function
  - $T\rho$  approximation
  - simple scattering amplitude
- two phenomenological models
  - (coupled channels model)
  - $N^*$  dominance model
- summary

# Introduction

partial restoration of chiral symmetry

$\eta'$  meson in nuclear medium

# Introduction

---

- spontaneously broken chiral symmetry may be restored in nuclear medium with reduction of chiral condensate

## **partial (incomplete) restoration of ChS in nuclear medium**

### **quark condensate does decrease in nuclear medium**

- phenomenological proof by analysis of pionic atom and low energy  $\pi$ -A scattering
- 30-40 % reduction at saturation density, if believe linear extrapolation

K. Suzuki et al.  
PRL92, 072302, (04);  
Friedman et al., PRL93, 122302 (04);  
DJ, Hatsuda, Kunihiro, PLB 670, 109 (08).

- such phenomenon can be observed by hadrons in nuclei
- natural that hadron properties are modified in nuclear medium due to the strong interaction between hadrons
- significant to identify the origin of the in-medium modification
- observe how much hadrons are modified

# $\eta'$ meson

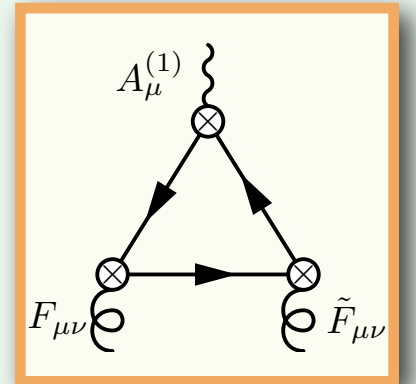
- degraded from NG boson due to  $U_A(1)$  anomaly

**flavor singlet**

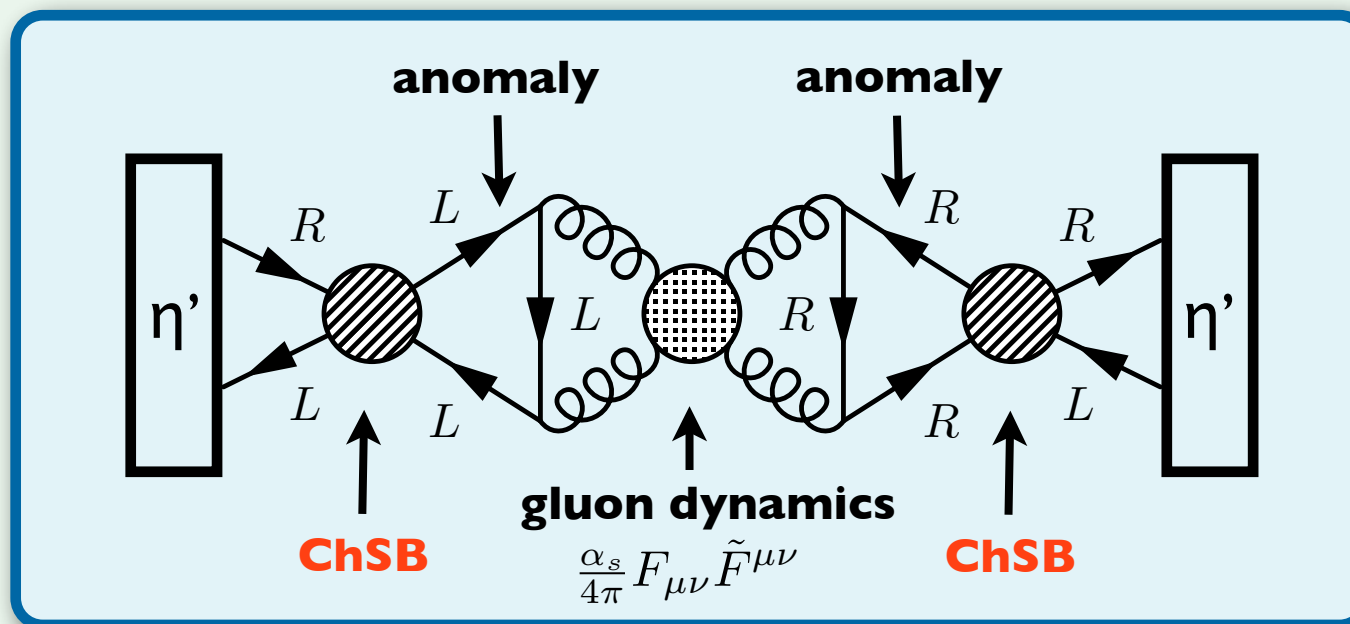
**(small) PCAC**

**anomaly**

$$\partial^\mu A_\mu^{(0)} = 2i(m_u \bar{u} \gamma_5 u + m_d \bar{d} \gamma_5 d + m_s \bar{s} \gamma_5 s) + \frac{3\alpha_s}{8\pi} F_{\mu\nu}^a \tilde{F}_a^{\mu\nu}$$



- $U_A(1)$  anomaly contributes to  $\eta'$  mass only through chiral symmetry breaking



DJ, Nagahiro, Hirenzaki,  
PRC85 (12) 032201(R)

- expects 80 MeV mass reduction at normal density

S. Sakai, DJ, Phys. Rev. C88, 064906 (13)

- mass reduction should be observed as an attractive potential in nucleus

# Preliminaries

spectral function

in-medium mass

$T\rho$  approximation

# Spectral function

- $\eta'$  meson decays into two gamma  
when observing invariant mass spectrum of two gamma,  
essence is given by  $\eta'$  spectral function

- spectral function

$$S_{\eta'} = -\frac{1}{\pi} \text{Im} D_{\eta'}$$

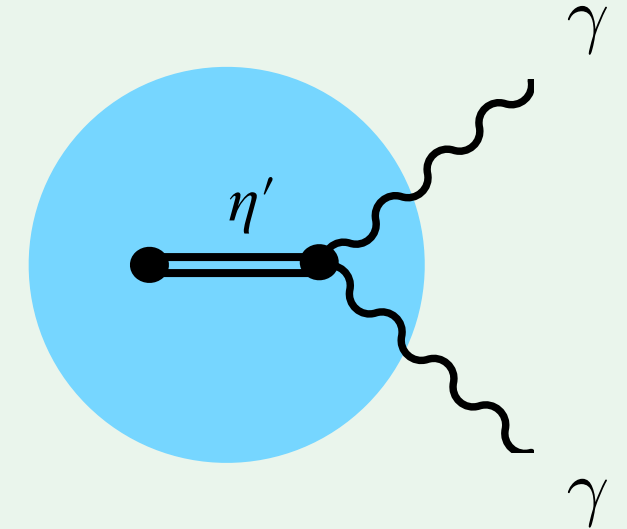
- in-medium propagator

$$D_{\eta'}(\omega, \mathbf{p}; \rho) = \frac{1}{\omega^2 - \mathbf{p}^2 - m_{\eta'}^2 - \Pi_{\eta'}(\omega, \mathbf{p}; \rho) + i\epsilon}$$

$\eta'$  self-energy  $\Pi_{\eta'}(\omega, \mathbf{p}; \rho)$

function of energy  $\omega$ , momentum  $\mathbf{p}$ , density  $\rho$

- obtain properties of self-energy



# In-medium mass

---

- describes interaction between  $\eta'$  meson to nuclear medium  $\Pi_{\eta'}(\omega, \mathbf{p}; \rho)$
- in-medium mass is given by pole position for eta' at rest

$$D_{\eta'}^{-1}(\omega_P, \mathbf{0}; \rho) = \omega_P^2 - m_{\eta'}^2 - \Pi_{\eta'}(\omega_P, \mathbf{0}; \rho) = 0$$

parametrize as  $\omega_P^2 = m_*^2 - im_*\Gamma_*$  (mass:  $m_*$ , width:  $\Gamma_*$ )

$$m_*^2 = m_{\eta'}^2 + \text{Re} \left( \Pi_{\eta'}(\omega_P, \mathbf{0}; \rho) \right),$$

$$\Gamma_* = -\frac{1}{m_*} \text{Im} \left( \Pi_{\eta'}(\omega_P, \mathbf{0}; \rho) \right)$$

$$\omega_P = m_* - i\frac{\Gamma_*}{2}$$



# Self-energy with finite momentum

- spectral function depends on spatial momentum

$$S_{\eta'}(\omega, \mathbf{p}; \rho) = -\frac{1}{\pi} \text{Im} D_{\eta'}(\omega, \mathbf{p}; \rho)$$

- pole position depends on the momentum  
→ dispersion relation

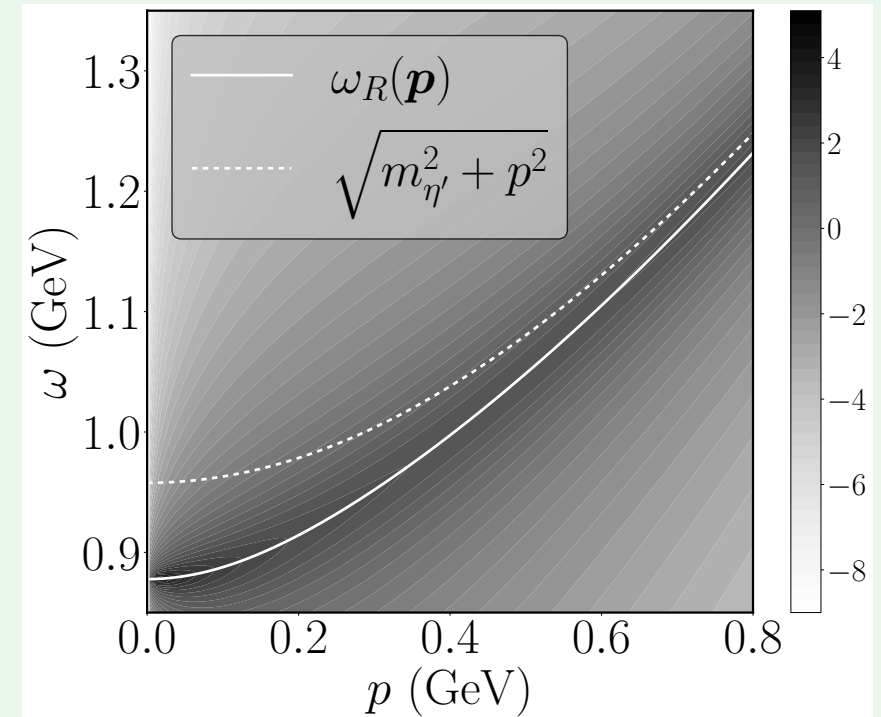
$$\omega_P^2(\mathbf{p}) - \mathbf{p}^2 - m_{\eta'}^2 - \Pi_{\eta'}(\omega_P(\mathbf{p}), \mathbf{p}; \rho) = 0$$

- invariant mass  $p_{\eta'}^2 = \omega^2 - \mathbf{p}^2$  at pole position  $\omega^2 = \omega_P^2$

$$p_{\eta'}^2 = m_{\eta'}^2 + \Pi_{\eta'}(\omega_P(\mathbf{p}), \mathbf{p}; \rho) = m_*^2 - im_*\Gamma_* + \left( \Pi_{\eta'}(\omega_P(\mathbf{p}), \mathbf{p}; \rho) - \Pi_{\eta'}(\omega_P(\mathbf{0}), \mathbf{0}; \rho) \right)$$

depends on spatial momentum

not necessarily at in-medium mass squared



# $T\rho$ approximation

---

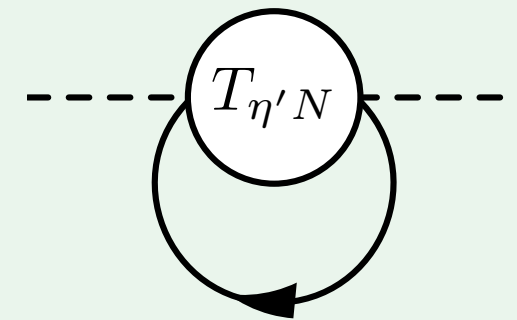
- $\eta'$ -nucleus interaction is not well-known yet  
 $\eta'N$  interaction is relatively better known

- focus on one-nucleon process  
self-energy is evaluated by

$$T\rho \text{ approximation: } \Pi_{\eta'}(\omega, \mathbf{p}; \rho) = T_{\eta'N}(\sqrt{s}) \rho$$

(low density)

- the  $\eta'N$  scattering amplitude determines  $\eta'$  self-energy
- consider spin-isospin symmetric uniform nuclear matter



# Simple exercise

a minimal scattering amplitude

# Simple exercise

- scattering length + elastic unitarity

$$T_{\eta'N}(W) = -\frac{8\pi W}{2m_N} \frac{1}{1/a_{\eta'N} - ip}, \quad \eta'N \text{ scattering length } a_{\eta'N}$$

- three examples of scattering length

(positive sign corresponds to attractive self-energy)

- **【theory】** linear sigma model (80 MeV mass reduction)

$$a_{\eta'N} = 0.87 \text{ fm}$$

S. Sakai, DJ, Phys. Rev. C88, 064906 (13)

- **【experiment】** low-energy  $pp \rightarrow pp\eta'$  data

E. Czerwinski et al., Phys. Rev. Lett. 113, 062004 (14)

$$a_{\eta'N} = (0_{-0.43}^{+0.43} + i0.37_{-0.16}^{+0.40}) \text{ fm} \rightarrow \text{obtained by } N^* \text{ dominance model}$$

- **【phenomenology】** coupled channels model

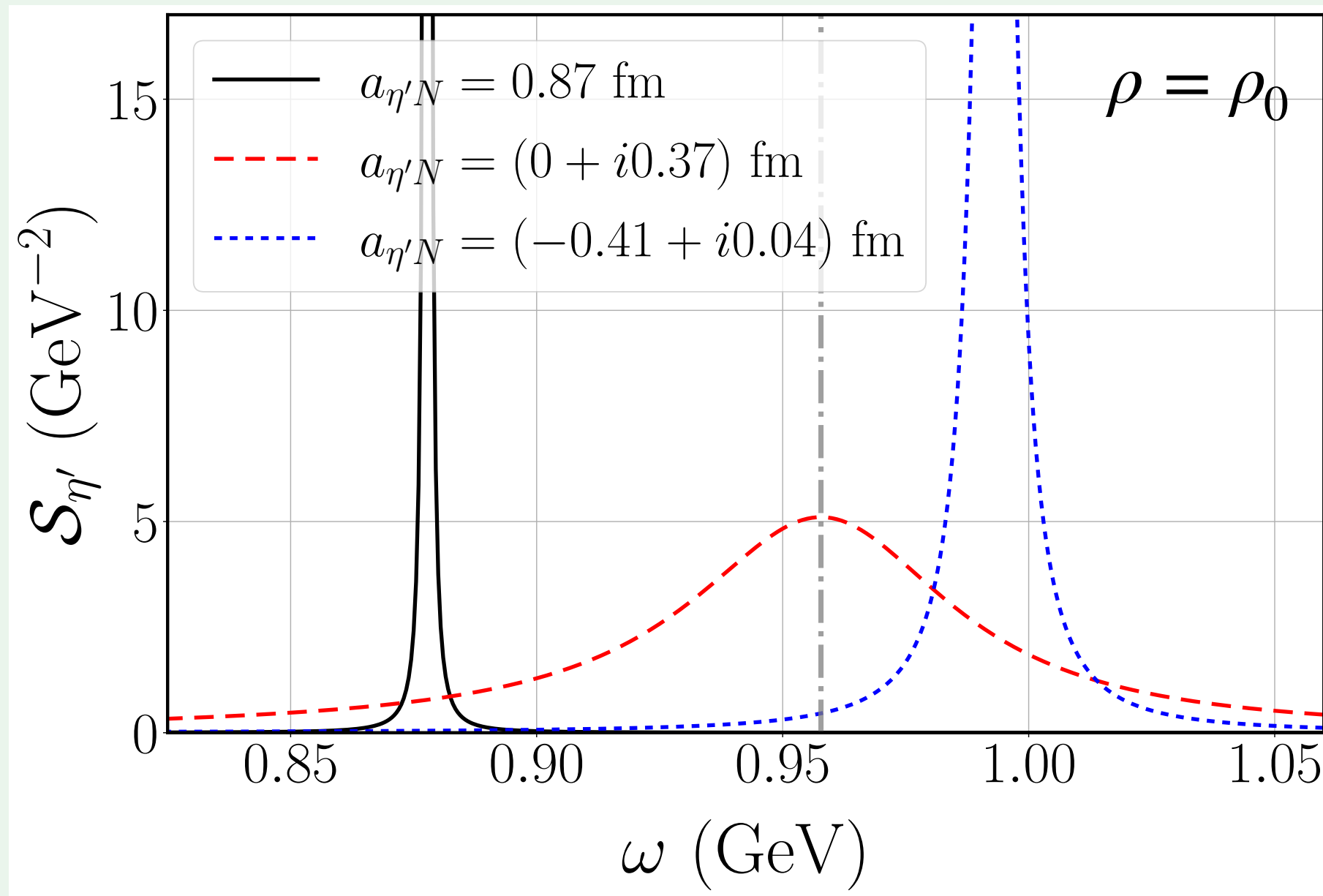
$$a_{\eta'N} = (-0.41 + i0.04) \text{ fm}$$

P. C. Bruns, A. Cieply, Nucl. Phys. A992, 121630 (19)



# Simple exercise

- spectral function of  $\eta'$  at rest in normal nuclear medium ( $p = 0$ )

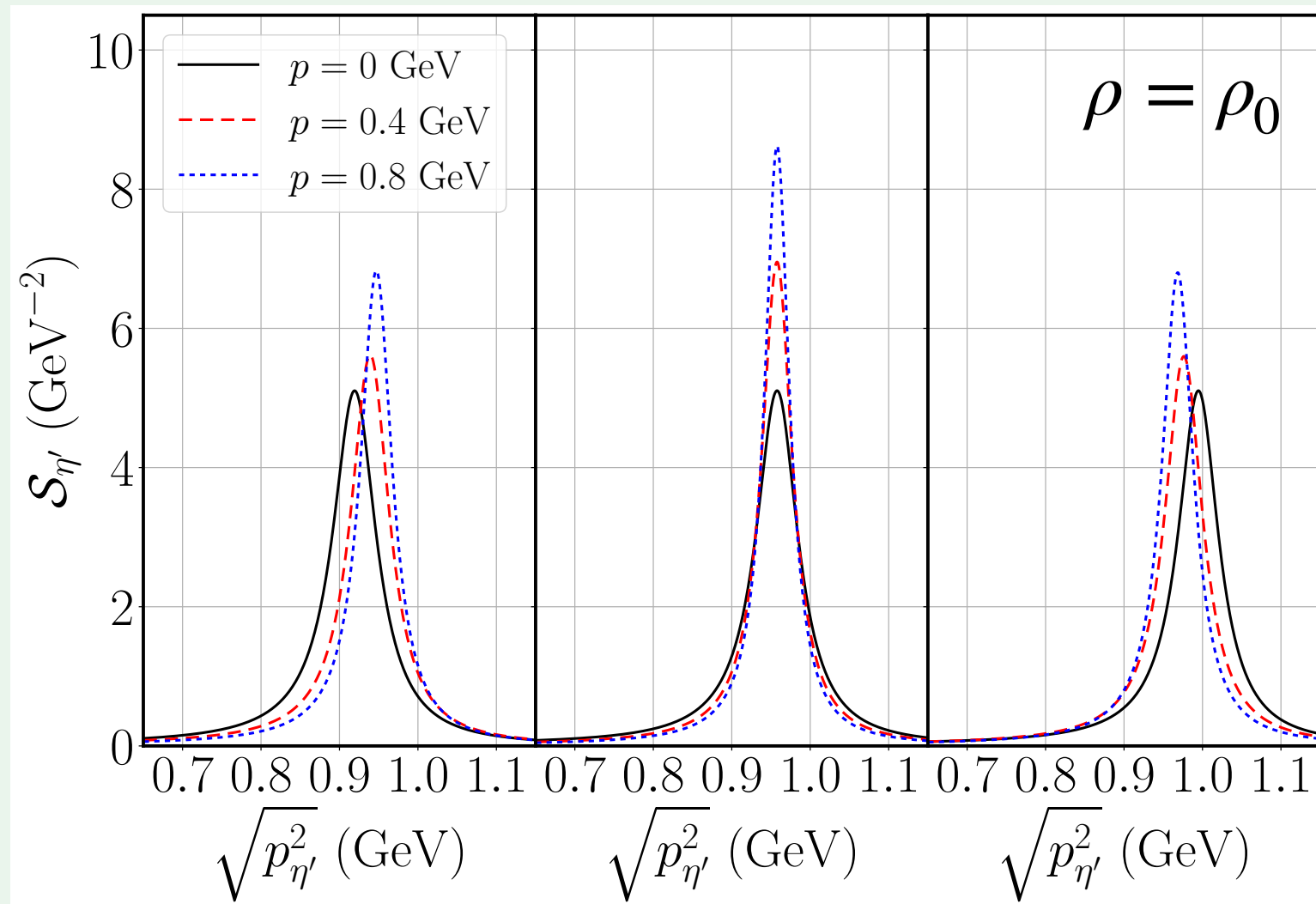


# Simple exercise

- spectral function of  $\eta'$  with finite momentum at  $\rho = \rho_0$

low-energy  $pp \rightarrow pp\eta'$  data:  $a_{\eta'N} = (0^{+0.43}_{-0.43} + i0.37^{+0.40}_{-0.16})$  fm

$a_{\eta'N} = (+0.43 + i0.37)$  fm    $(0 + i0.37)$  fm    $(-0.43 + i0.37)$  fm



$$T_{\eta'N}(W) = -\frac{8\pi W}{2m_N} \frac{1}{1/a_{\eta'N} - ip}$$

medium effect on mass gets less noticeable for finite momentum

$N^*$  dominance model

# two phenomenological models

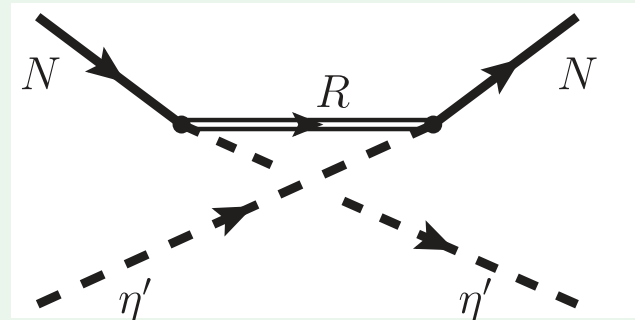
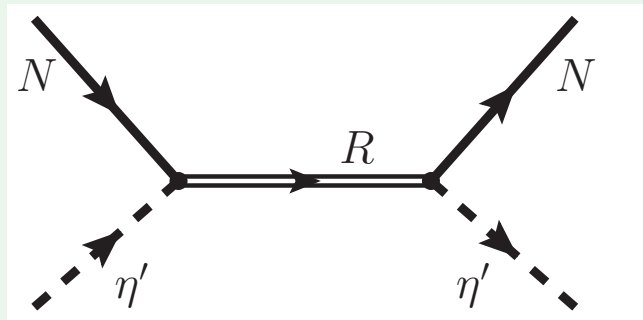
- $N^*$  dominance model

$N(1895)$  is located just below the  $\eta'N$  threshold

has spin  $1/2^-$ , s-wave coupling to  $\eta'N$

$\eta'N$  threshold at 1896 MeV

$N^*$  at 1894 MeV



$$T_{\eta'N}(\sqrt{s}) = \frac{g_{\eta'N}^2}{\sqrt{s} - E_{N^*} + i\Gamma_{N^*}/2} + \frac{g_{\eta'N}^2}{-E_{\eta'} + E_N - E_{N^*} + i\Gamma_{N^*}/2}$$

use isobar model parameters

L. Tiator, et al. (EtaMAID2018), Eur. Phys. J. A54, 210 (18)

$$m_{N^*} = 1894.4 \text{ MeV}, \quad \Gamma_{N^*} = 70.7 \text{ MeV}, \quad g_{\eta'N} = 1.4$$

provides  $a_{\eta'N} = (-0.02 + i0.43) \text{ fm}$

assume no medium effects on  $N^*$

## $N^*$ dominance model for $\eta$ meson

H.C. Chiang, E. Oset, L.C. Liu, Phys. Rev. C44, 738 (91).

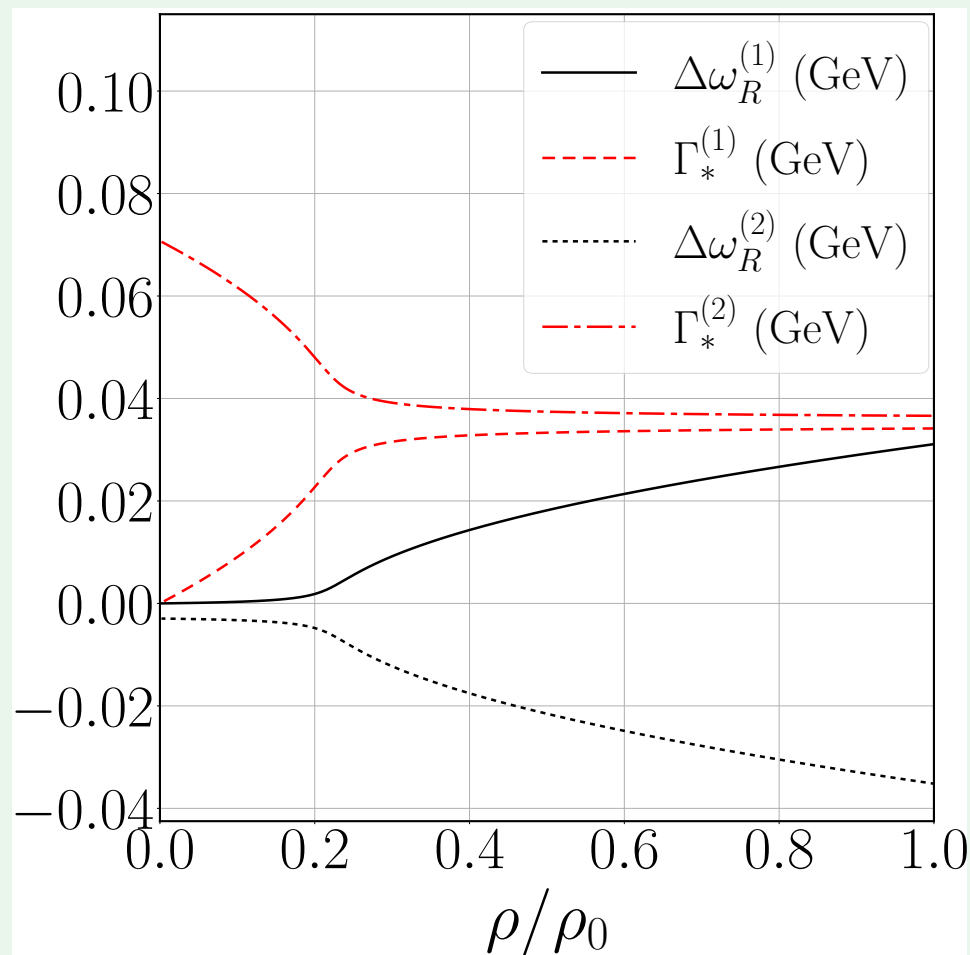
D.J., H. Nagahiro, S. Hirenzaki, Phys. Rev. C66, 045202 (02),

D.J., E.E. Kolomeitsev, H. Nagahiro, S. Hirenzaki, Nucl. Phys. A811, 158 (08)



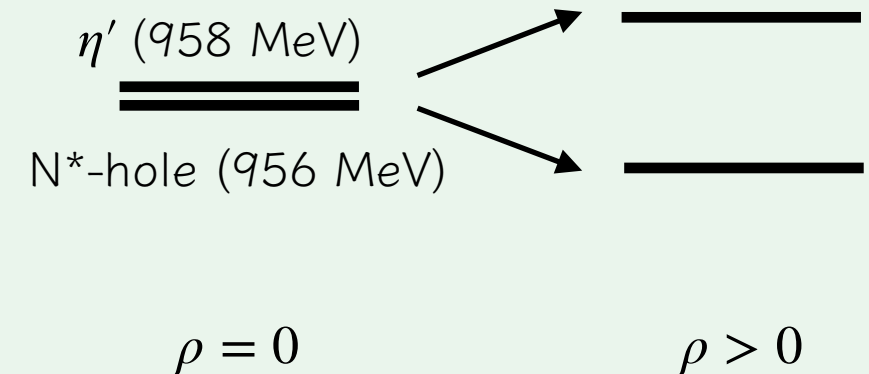
# N\* dominance model

- there are two poles in in-medium propagator  
one comes from  $\eta'$  mode, the other comes from N\*-hole mode
- in-medium masses and widths of two modes



$\Gamma_*$

$\Delta m_*$

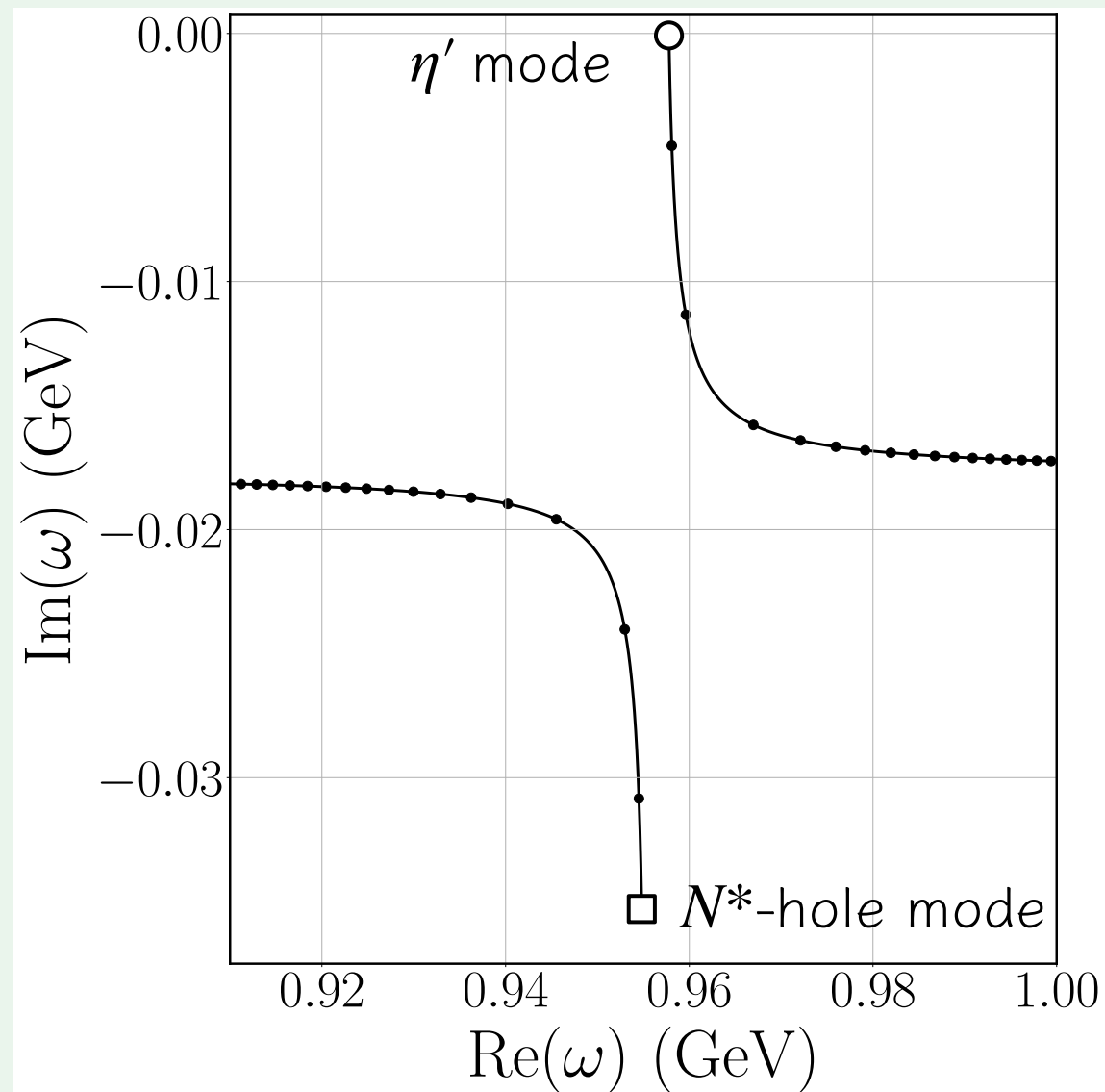


in-medium masses are around  $m_{\eta'} \pm 30$  MeV at  $\rho = \rho_0$

# $N^*$ dominance model

S. Sakai, DJ, in preparation

- pole trajectory against nuclear density



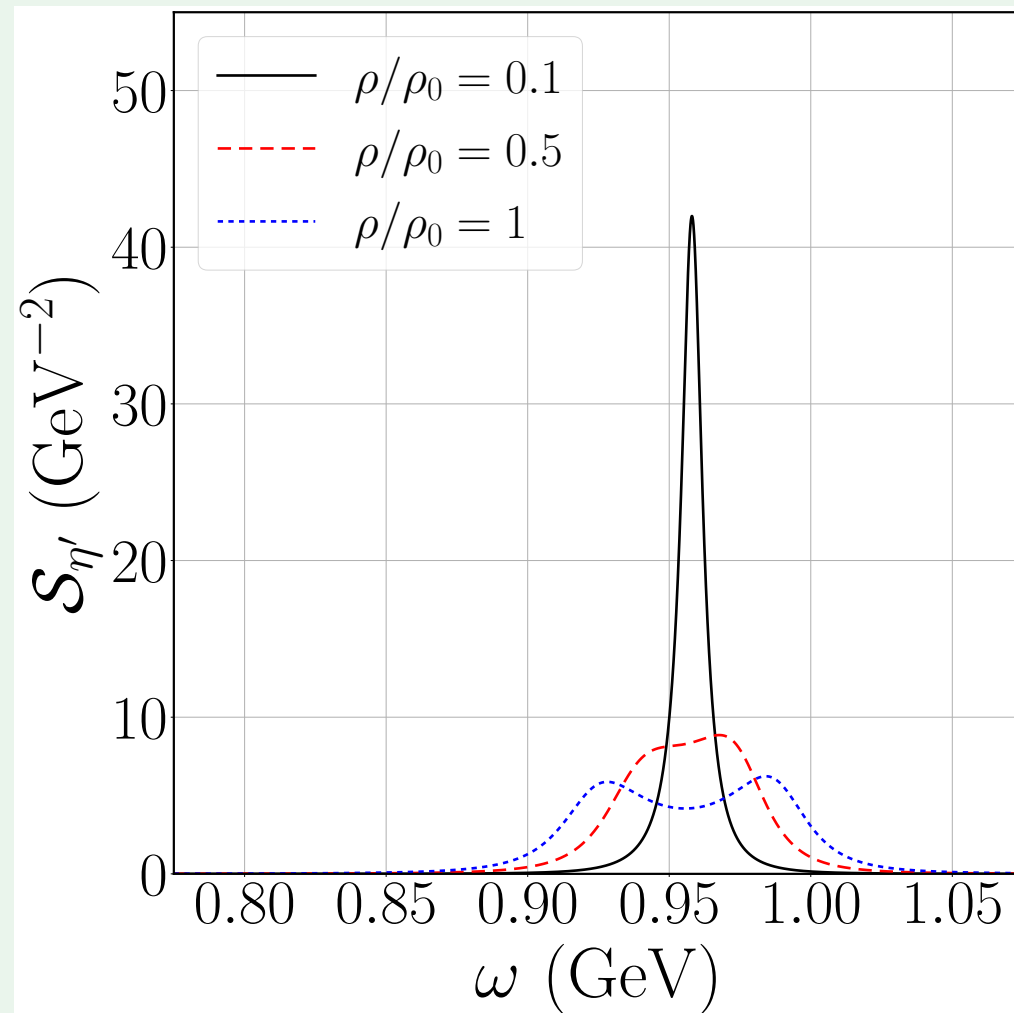
dots are plotted at every  $0.1\rho_0$

- exceptional point:  $\rho_{\text{EX}} = (0.22 - i0.03)\rho_0$

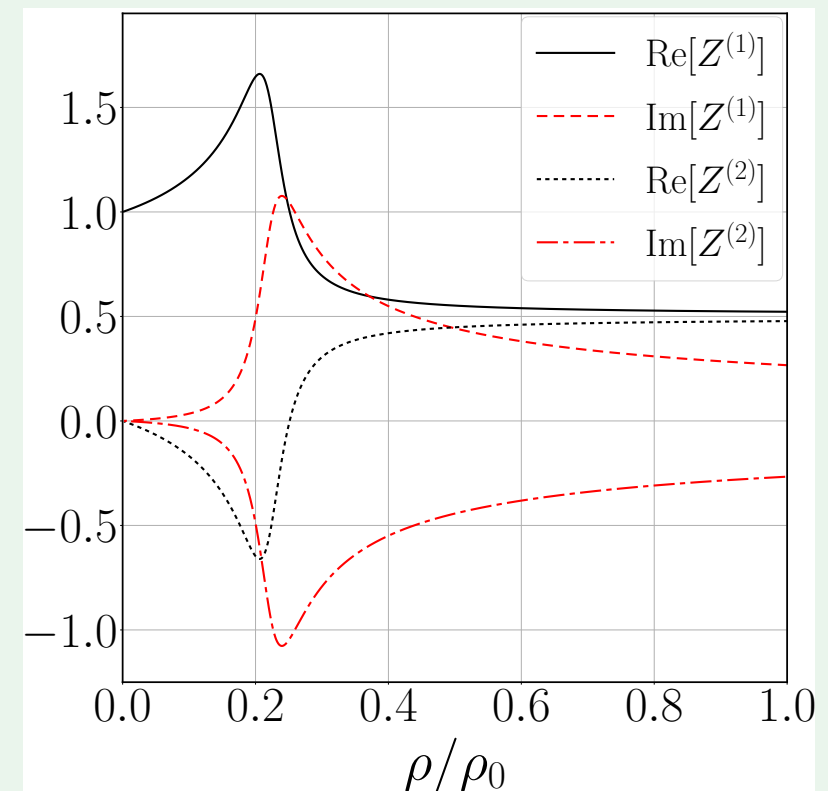
# $N^*$ dominance model

S. Sakai, DJ, in preparation

- spectral function of  $\eta'$  at rest,  $\rho = 0.1\rho_0, 0.5\rho_0, \rho_0$



wave function renormalization



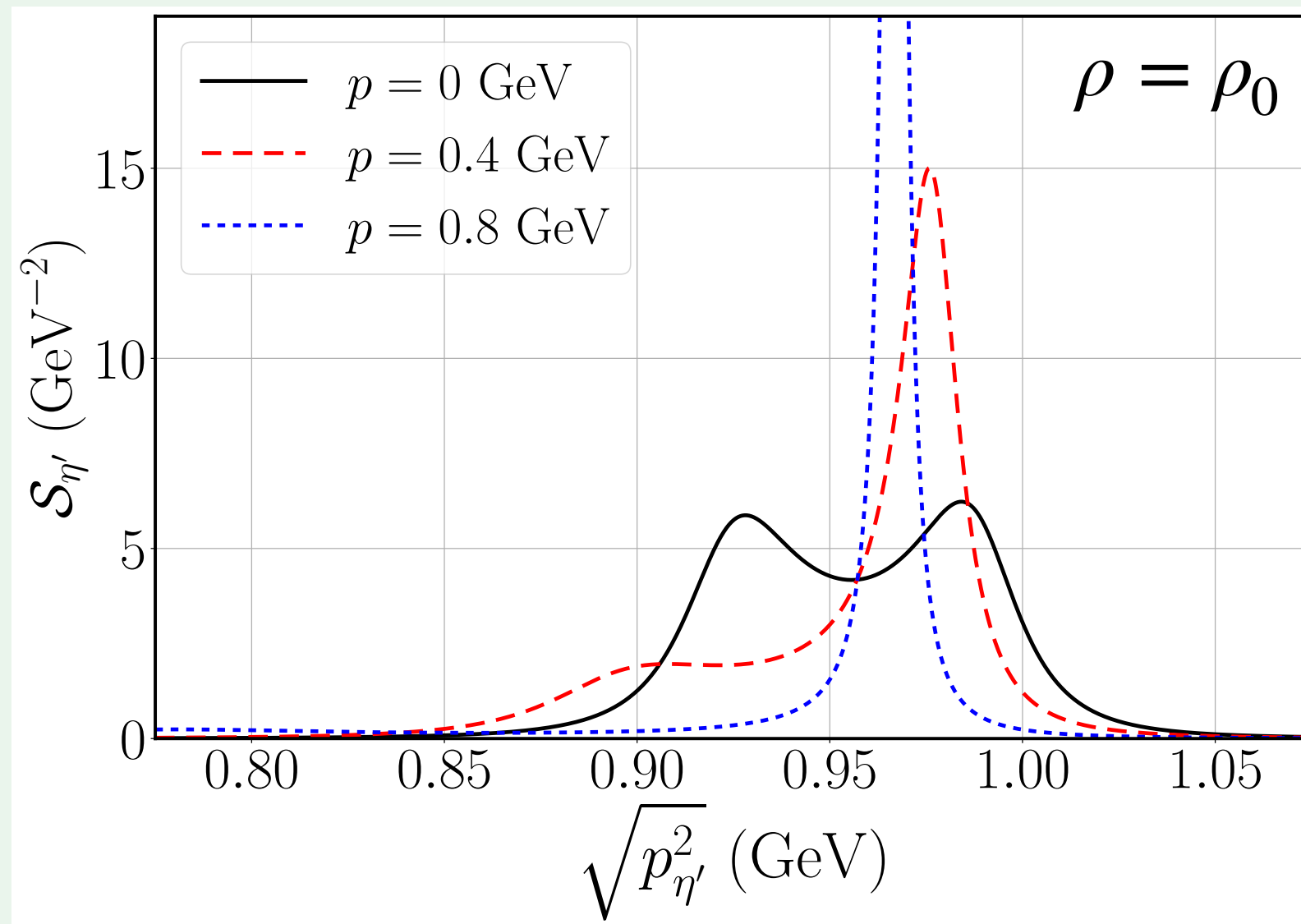
two peaks appear at higher density

peak positions are around  $m_{\eta'} \pm 30 \text{ MeV}$  at  $\rho = \rho_0$

$\text{Re}[Z^{(1)}]$  and  $\text{Re}[Z^{(2)}]$  approach to 0.5 for  $\rho > 0.4\rho_0$

# $N^*$ dominance model

- spectral function with finite momentum at  $\rho = \rho_0$



higher peak goes down, and lower peak gets less distinct

# Summary

---

- investigate spectral function of in-medium  $\eta'$  meson in  $T\rho$  approximation  
 $\eta'N$  scattering amplitude determines in-medium behavior of  $\eta'$  meson
- for attractive (repulsive) scattering length, peak of spectral function goes down (up) for  $p = 0$  as one expects
- peak position in finite density approaches to one in vacuum with increase of spatial momentum  
medium effect on mass gets less noticeable for finite momentum
- momentum dependence of spectral function is important for better understanding
- if  $N^*$  strongly couples to  $\eta'N$ , two peaks may appear in spectral function
- clarification of interaction mechanism of  $\eta'$  and nucleon is an important piece to understand in-medium properties of  $\eta'$  meson